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MRI quantification of diffusion and perfusion in bone marrow by intravoxel incoherent motion (IVIM) and non-negative least square (NNLS) analysis.

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Running Head: IVIM and NNLS in bone marrow.

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Abstract

Object To assess the feasibility of measuring diffusion and perfusion fraction in vertebral bone marrow using the intravoxel incoherent motion (IVIM) approach and to compare two fitting methods, i.e., the non-negative least squares (NNLS) algorithm with the more commonly used Levenberg-Marquardt (LM) non-linear least squares algorithm, for the analysis of IVIM data..

Materials and Methods MRI experiments were performed on fifteen healthy volunteers, with a diffusion-weighted echo-planar imaging (EPI) sequence at five different b-values (0, 50, 100, 200, 600 s/mm²), in combination with a STIR module to suppress the lipid signal. Diffusion signal decays in the first lumbar vertebra (L1) were fitted to a bi-exponential function using the LM algorithm and further analyzed with the NNLS algorithm to calculate the values of the apparent diffusion coefficient (ADC), pseudo-diffusion coefficient (D*) and perfusion fraction.

Results The NNLS analysis revealed two diffusion components only in seven out of fifteen volunteers, with $ADC = 0.60 \pm 0.09$ (10^{-3} mm²/s), $D^* = 28 \pm 9$ (10^{-3} mm²/s) and perfusion fraction = 14 ± 6 %. The values obtained by the LM bi-exponential fit were: $ADC = 0.45 \pm 0.27$ (10^{-3} mm²/s), $D^* = 63 \pm 145$ (10^{-3} mm²/s) and perfusion fraction = 27 ± 17 %. Furthermore, the LM algorithm yielded values of perfusion fraction in cases where the decay was not bi-exponential, as assessed by NNLS analysis.

Conclusion

The IVIM approach allows for measuring diffusion and perfusion fraction in vertebral bone marrow; its reliability can be improved by using the NNLS, which identifies the diffusion decays that display a bi-exponential behaviour.

Keywords: Intravoxel incoherent motion, IVIM, diffusion, bone marrow, perfusion, NNLS.

Introduction

Measurements of the water apparent diffusion coefficient (ADC) and tissue perfusion in vertebral bone marrow are of interest for investigations of a number of pathologies (1-3). Water diffusion provides a means for tissue microstructure characterization (4-7) and it has been shown that the water diffusivity in bone marrow allows to distinguish between benign and malignant lesions and to monitor myeloma infiltration (8, 9). Of relevance in clinical and research studies is also the assessment of bone marrow perfusion, for tumor response to therapy and for evaluation of compression fractures and metastasis (10-13).

Bone marrow consists of two tissue components: the yellow adipose marrow, which is composed mostly of fatty tissue and accounts for up to 80% of bone marrow in a healthy adult, and red marrow, which consists mostly of hematopoietic cells, but also contains up to 40% of fatty tissue (14). The large amount of lipids represents a confounding factor in the measurement of the water ADC (15) and tissue perfusion in bone marrow (16), thus it is preferable to employ fat suppression techniques.

Measurements of both ADC and tissue perfusion can be achieved with the MRI approach of the intravoxel incoherent motion (IVIM), introduced by Le Bihan more than two decades ago (17). The IVIM approach has been recently ‘rediscovered’ as an attractive method for assessing perfusion fraction in different organs (18-26). In IVIM measurements, images are acquired with different diffusion-sensitizing gradients (i.e., at different ‘b-values’) to measure tissue microcapillary perfusion and water diffusivity using the signal decay at relatively small ($0-100 \text{ s/mm}^2$) and large ($100-1000 \text{ s/mm}^2$) b-values, respectively. The calculation of the perfusion fraction within the IVIM model relies on the assumption that the diffusion signal decay is bi-exponential. To date, data analysis approaches based on the non-linear least squares algorithm have been investigated to extract the perfusion fraction from the bi-exponential diffusion decay (7, 27). However, in certain experimental conditions the low signal-to-noise ratio (SNR) as well as motion artifacts and other factors might affect the data quality and thus the signal decay might not necessarily display two diffusion components. As the knowledge of diffusion decay characteristics (specifically, the number of diffusion components) is a fundamental prerequisite for calculating the perfusion fraction, it is important to employ appropriate methods of data analysis. In this respect, the non-negative least square (NNLS) technique (28) could be of interest

for the analysis of IVIM data. In fact, the NNLS technique does not require a priori assumptions about the the number of components in a given decay and in recent years it has been extensively used to investigate the multi-exponential characteristics of transverse relaxation decays (29-34).

Given the clinical interest in diffusion and perfusion measurements in vertebral bone marrow, and the challenges related to both data acquisition and analysis, the aim of this study was twofold: first, to assess the feasibility of measuring diffusion and perfusion fraction in vertebral bone marrow using the IVIM approach, combined with fat suppression; secondly, to compare two fitting methods, i.e., the NNLS with the more commonly used Levenberg-Marquardt (LM) non-linear least squares algorithm, for the analysis of IVIM data.

Materials and Methods

MR Imaging

All experiments were conducted according to the procedures approved by the local institutional review board. A group of fifteen healthy women volunteers (age between 18 and 30 years) was examined on a 1.5 T scanner (Siemens Healthcare, Erlangen, Germany). This population sample was chosen because women with regular menstruations have more red marrow than men and therefore higher bone marrow perfusion (). A urine pregnancy test was performed before inclusion and pregnant women were not included in the study. The body coil was used for transmission. The spine-coil and a phased array coil that was positioned on the torso of the volunteers were used for reception.

Multi-planar scout gradient-echo images and coronal T2-weighted short-TI inversion recovery (STIR) images were acquired prior to diffusion MRI. Diffusion-weighted echo-planar imaging (EPI) was performed at five different b-values (0, 50, 100, 200, 600 s/mm²) with a STIR module to suppress the lipid signal. The STIR method was chosen because it provides robust fat suppression, though at the expenses of SNR. Other imaging parameters were: TR/TE = 10900/75 ms, inversion time TI = 170 ms, FOV of 312 mm × 500 mm, slice thickness of 4 mm, 40 slices, matrix size of 269x384 and 2 averages, total scan time of 6 min 22 s. The diffusion sensitization gradients were applied along three directions and trace diffusion-weighted images were generated. The minimum b-value available (with the exception of the b-value = 0 s/mm²) was 50 s/mm² and only b-values multiple of 50 s/mm² were feasible. Vendor-supplied sequences were used for all measurements.

A dedicated Plexiglas™ support of a cradle-like shape was designed and built for the current study (Figure 1). During the MR experiment, the support was positioned on the spine coil. Four cylindrical phantoms (diameter = 3.5 cm, length = 40 cm) were integrated in this support. Two phantoms were filled with distilled water and the other two phantoms with distilled water and 25% Polyethylene glycol (PEG). These phantoms, employed to verify the performance of the experimental apparatus, allowed for the measurement of the signal decay in water and PEG, which is known to decrease mono-exponentially with increasing b-values.

Data Analysis

A region of interest (ROI) was drawn to encircle the first lumbar vertebra (L1) on the MR diffusion image at the b-value = 0 s/mm². The mean signal intensity and standard deviation was calculated at all b-values for the same ROI. The average area of the ROI over all volunteers was 1.8 ± 0.3 cm². As a reference, ROIs were also drawn in the water and PEG phantoms to measure the ADC of these substances.

Fitting multi-exponential decay curves is a notorious problem in MRI and in many other fields of science (36, 37). Here, we employed two methods: the NNLS and the LM non-linear least squares algorithm.. Within the NNLS framework (28), the signal intensity as a function of b-values is written as:

$$y(b_i) = \sum_j \exp(-b_i D_j) s(D_j) = \sum_j A_{ij} s_j; \quad i = 1, 2, \dots, N; \quad j = 1, 2, \dots, M \quad [1]$$

where b_i is the i th b-value, $y(b_i)$ the mean signal intensity of the ROI, $s(D_j)$ the unknown amplitude of the component with diffusion coefficient D_j , N the number of b-values, M the number of allowed diffusion components and A is the matrix containing the exponential kernel functions. The amplitudes s_j that minimize the least-squares misfit are determined by the following equation:

$$\sum_i (\sum_j A_{ij} s_j - y_i)^2 + \mu \sum_i (\sum_j H_{ij} s_j)^2; \quad i = 1, 2, \dots, N; \quad j = 1, 2, \dots, M \quad [2]$$

where μ is the regularizer parameter (29) and H is the identity matrix. Thus, the NNLS algorithm calculates the number of diffusion components in a given decay curve and provides the value of the diffusion coefficient and amplitude of each diffusion component. Using the NNLS results, the perfusion fraction was calculated as the normalized amplitude of the faster diffusion component. Furthermore, fits of the signal decay with b-values to a bi-exponential function were performed using a Levenberg-Marquardt (LM) non-linear least squares algorithm. The bi-exponential function was $S = (f) \exp(-b_n \cdot D^*) + (1-f) \exp(-b_n \cdot ADC)$ where f and $(1-f)$ are relative fractions of the amplitudes of the fast and slow diffusion components with diffusion values D^* and ADC , respectively. It should be noted here that f represents the perfusion fraction and the ADC is the tissue diffusion coefficient that is typically measured with diffusion MRI.

The data analysis was performed with Matlab (MathWorks, Natick, MA, USA). Data are expressed as mean $\pm$ standard deviation.

Results

MR images of one volunteer are shown in Figure 2. On the MR coronal image (Figure 2, left) the location of an axial diffusion-weighted image (Figure 2, right) is illustrated by the horizontal line. The ROI for the analysis of the diffusion decay in the L1 vertebra is indicated on the axial image (Figure 2, right). The graph of Figure 3 shows an example of a fat-suppressed diffusion decay from an ROI in the vertebral bone marrow (L1) of one volunteer. The results of the NNLS analysis of the same diffusion decay are shown in Figure 4. The NNLS analysis revealed two diffusion components: a fast component with diffusion coefficient (D^*) of $\sim 20 \times 10^{-3} \text{ mm}^2/\text{s}$ and a slow component with diffusion coefficient (ADC) of $\sim 0.7 \times 10^{-3} \text{ mm}^2/\text{s}$ (Figure 4). The perfusion fraction calculated by NNLS analysis was 14 %. The NNLS analysis of the diffusion decay in the phantoms yielded a single component (Figure 5), with NNLS peaks at $\sim 2.1 \times 10^{-3} \text{ mm}^2/\text{s}$ and $\sim 1.2 \times 10^{-3} \text{ mm}^2/\text{s}$ for water and PEG, respectively.

The results of the NNLS analysis are provided in Table 1. For comparison purposes, the results of the bi-exponential fit performed with the LM algorithm are listed as well in the same table. The NNLS analysis of diffusion decays revealed two diffusion components in seven out of fifteen volunteers, with (mean $\pm$ standard deviation) $\text{ADC} = 0.60 \pm 0.09 (10^{-3} \text{ mm}^2/\text{s})$, $D^* = 28 \pm 9 (10^{-3} \text{ mm}^2/\text{s})$ and perfusion fraction = $14 \pm 6 \%$ (Table 1). The mean values obtained by the LM bi-exponential fit were: $\text{ADC} = 0.45 \pm 0.27 (10^{-3} \text{ mm}^2/\text{s})$, $D^* = 63 \pm 145 (10^{-3} \text{ mm}^2/\text{s})$ and perfusion fraction = $27 \pm 17 \%$. It should be noted that in the experiments where the NNLS yielded two diffusion components (volunteer # 3, 5, 6, 8, 10, 12, 13) the NNLS-derived values of ADC, D^* and perfusion fraction were similar to the correspondent LM-derived values. In all cases, NNLS analysis yielded a single component for diffusion decay in the water and PEG phantoms.

Discussion

In the current study, the feasibility of measuring the water ADC and perfusion in vertebral bone marrow was investigated on a 1.5 T clinical scanner with the IVIM approach, in combination with the NNLS data analysis. It is well established that MRI has become the modality of choice for abdominal imaging and in particular for assessing non-invasively a number of vertebral bone marrow disorders with T1, T2 and diffusion-weighted MR images. In addition, it has been shown that quantitative diffusion measurements provide an added value to the MR examination, especially in the case of longitudinal studies or group comparisons.

A relatively large range of values for the water ADC in vertebral bone marrow is found in the literature. This is mainly due to the inter-scanner variability and to the differences in pulse sequences -EPI, stimulated-echo (STE), fast spin-echo (FSE), line-scan diffusion imaging (LSDI)- used in each study (3, 7, 38, 39). In studies where the diffusion-weighted EPI sequence with fat suppression was employed, the measured values of the water ADC ranged from $0.23 \times 10^{-3} \text{ mm}^2/\text{s}$ (40) to $1.66 \times 10^{-3} \text{ mm}^2/\text{s}$ (41), with most studies yielding values close to $0.50 \times 10^{-3} \text{ mm}^2/\text{s}$, as in the study by Hatipoglu et al., ($0.46 \pm 0.03 \times 10^{-3} \text{ mm}^2/\text{s}$, (42)), by Griffith et al. ($0.46 \pm 0.08 \times 10^{-3} \text{ mm}^2/\text{s}$, (3)), and by Yeung et al. ($0.50 \pm 0.09 \times 10^{-3} \text{ mm}^2/\text{s}$, (7)), for instance. The value of the water ADC of vertebral bone marrow measured in the current study is close to the values found in most of these studies.

In addition to quantitative diffusion measurements, perfusion measurements are of interest in bone marrow for investigations of osteoporosis, tumor, metastases and compression fractures. It has been recently shown that perfusion could also serve as a parameter of early response of myeloma to anti-angiogenic therapy (11). In most cases, perfusion in bone marrow has been measured with dynamic contrast-enhanced (DCE) MRI (1, 3) and only a limited number of studies have employed other approaches such as IVIM (7) and arterial spin labeling, ASL (11). In the IVIM study by Yeung et al., fat-suppressed diffusion-weighted images were acquired at 'low' ($0\text{-}100 \text{ s/mm}^2$) and 'high' ($100\text{-}500 \text{ s/mm}^2$) b-values to measure bone marrow perfusion and diffusion of the third lumbar vertebra (7). The value of ADC found by Yeung et al. in the current study is in good agreement with the value of ADC found in the current study; however, values of the perfusion fraction were not reported by Yeung et al. because, as the authors explained, no reliable estimate could be made. In the current study, perfusion measurements

yielded reliable results -as assessed by NNLS analysis- only in seven out of fifteen subjects. Thus, the results of the current study confirm in part the findings of the work by Yeung et al., i.e., the low reliability of the IVIM approach for perfusion measurements in vertebral bone marrow, within the constraints of a clinical protocol.

The NNLS technique gives an important aid in the data analysis of signal decays, since it does not require a priori assumptions about the number of decay components.. The NNLS analysis has been extensively employed to investigate the multi-component characteristics of transverse relaxation (T2 and T2*) decays. Most of these studies have been focused on brain, for myelin quantitation (44-46). Other applications have included the analysis of the T2 relaxation decay in muscle (47, 48) and nerve (49).

In the current study, the values of perfusion fraction obtained by the NNLS and by the LM bi-exponential fit were $14 \pm 6 \%$ and $27 \pm 17 \%$, respectively. As indicated by Le Bihan and Turner (50) the IVIM perfusion fraction is the fractional volume of capillary blood flowing in each voxel. Thus, taking a fat fraction of 0.3 for healthy young female (51), and a tissue NMR-visible water fraction of 0.8 (50), one can estimate an average value of capillary blood volume of $\sim 7,8$ mL/min/100 g and $\sim x,x$ mL/min/100 g, obtained by the NNLS and by the LM bi-exponential fit, respectively. The value estimated by the NNLS is close to the value of blood volume of 5.9 ± 2.6 mL/100 mL found by Biffar et al. (16).

Furthermore, in subjects where the NNLS did not provide evidence for the presence of two components -Table 1, subject 15, 9, 7, 1, for instance- the perfusion fraction yielded by the LM bi-exponential fit was 50, 43, 57, 36 %, respectively, which in turn corresponds to a capillary blood volume in the range of 20 to 31 mL/100 g. These values of blood volume appear higher than the physiological range for healthy subjects (16).

It should be noted that simple range criterions could be used to discard the results of the LM bi-exponential analysis in healthy subjects, where typically the range of physiologically plausible values is known.. On the other hand, this might not be the case in pathological conditions thus a method without a priori assumptions about the number of diffusion components, such as the NNLS, is relevant. In the current study, the bi-exponential behavior of the diffusion signal decay in the L1 was detectable in seven out of fifteen volunteers. In each experiment, diffusion signal decays were also measured in the water and PEG phantoms positioned next to the volunteers, to check the performance of the experimental apparatus in order to rule out that the bi-exponential

feature could originate from mis-adjustments. In all cases, the NNLS analysis yielded a single component for the diffusion signal decay in water and PEG. This suggests that the bi-exponential behavior observed *in vivo* in the vertebral bone marrow could not be ascribed to mis-calibrations or measurements pitfalls.

When comparing the different methods (DCE-MRI, IVIM and ASL) that have been employed for perfusion measurements in bone marrow, it can be stated that the advantage of both IVIM and ASL over DCE-MRI is that they do not require administration of contrast agent and therefore they are less invasive. Thus, both IVIM and ASL could be an attractive alternative to the more established DCE-MRI -though, at this stage, DCE-MRI measurements appear to be more robust than IVIM and ASL. It should be also noted, however, that due the large amount of lipids a quantitative measure of perfusion with DCE-MRI is more challenging in bone marrow than in other tissues and the lipid content needs to be known and taken into account in the data analysis for a proper interpretation of the DCE-MRI data (2).

IVIM measurements in vertebral bone marrow with the STIR fat suppression suffer from an intrinsic low SNR. On the other hand, due to the large fat content in the vertebra (60-80% of the total tissue), it is preferable to suppress the signal of fat in order to investigate the water diffusion and the perfusion fraction. As shown by Mulkern et al. (15), even small percentages of lipid within a voxel can drastically affect diffusion coefficient measurements in bone marrow; the same applies to perfusion, as shown by Biffar et al. (16). Further studies will be required in order to test IVIM measurements with lipid suppression techniques other than the STIR approach, which results in a significant loss of signal.

One limitation of this study is that the imaging protocol was designed for a clinically acceptable scan time and with a spatial coverage that is consistent with standard clinical protocols. This relatively large spatial coverage comes at the penalty of increased scan time and therefore a decreased number of b-values. Future studies will include a more detailed coverage of the water diffusion decay, i.e., the acquisition of additional b-values, especially small b-values, in order to improve the quantification of perfusion (52). Furthermore, there was a limitation on the choice of b-values in the pulse sequence used in this study. Recently, a new pulse sequence provided by the vendor allows for a more flexible choice of b-values that will significantly improve the sampling of the fast-decaying component. Overall, it should be stressed that additional studies will be necessary to improve the measurement reliability. Improvements in coil design, pulse

sequences, motion correction and fat suppression methods will contribute to ameliorate the diffusion decay curve and therefore increase reliability of the IVIM approach in vertebral bone marrow.

Conclusion

The IVIM approach allows for measuring diffusion and perfusion fraction in vertebral bone marrow. The NNLS method, which identifies the diffusion decays that display a bi-exponential behaviour, , provides an added value in the analysis of the IVIM data.

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Figure Legends

Figure 1. Plexiglas support for the water and PEG phantoms. The support consists of two separate parts that can be adjusted to the anatomy of the patient. The cylindrical phantoms are integrated into the support. The schematic and a photo of a single element are shown on the top left panel and top right panel, respectively. The support is positioned on the spine coil and the volunteer lies supine on the support during the MR experiment.

Figure 2. Representative MR images of one volunteer. A coronal T2-weighted image (left) and an axial diffusion-weighted image acquired at the $b\text{-value} = 50 \text{ s/mm}^2$ (right) are shown. In both acquisitions, a STIR-preparation module was used to suppress the lipid signal. The horizontal line on the coronal image indicates the position of the axial slice. The elliptical region of interest centered on the first lumbar vertebra (L1) is illustrated on the diffusion-weighted image.

Figure 3. Example of intravoxel incoherent motion (IVIM) data acquired on one volunteer. The fat-suppressed diffusion decay from an ROI in the vertebral bone marrow (L1) and from an ROI in the noise are shown. As indicated by the curvature of the decay on the semi-log plot, the diffusion signal in bone marrow displays a bi-exponential behavior with a fast-decaying component for $b\text{-values}$ between 0-100 s/mm^2 and a slow-decaying component for $b\text{-values}$ between 100-600 s/mm^2 . The NNLS analysis of this diffusion decay is shown in Figure 4.

Figure 4. The NNLS spectrum of a fat-suppressed diffusion decay from an ROI in the vertebral bone marrow (L1) of one volunteer. The NNLS spectrum is plotted on a logarithmic scale with diffusion values equally spaced between 10^{-1} and 10^2 ($\times 10^{-3}$) mm^2/s . The NNLS spectrum exhibits two peaks at $\sim 0.7 \times 10^{-3} \text{ mm}^2/\text{s}$ and $\sim 20 \times 10^{-3} \text{ mm}^2/\text{s}$, with a perfusion fraction of 14%. The diffusion coefficient of the slow component ($\sim 0.7 \times 10^{-3} \text{ mm}^2/\text{s}$) is consistent with the water ADC value of vertebral bone marrow. Similarly, the value of diffusion coefficient of the fast component ($\sim 20 \times 10^{-3} \text{ mm}^2/\text{s}$) is consistent with pseudo-diffusion values related to tissue micro-capillary perfusion.

Figure 5. The NNLS spectra of the diffusion decay in the water (top) and Polyethylene glycol (PEG, bottom) phantoms. A single diffusion peak is observed in water at $\sim 2.1 \times 10^{-3} \text{ mm}^2/\text{s}$ and in PEG at $\sim 1.2 \times 10^{-3} \text{ mm}^2/\text{s}$.

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Table 1. Values of ADC, D* and perfusion fraction of vertebral bone marrow obtained by the bi-exponential curve fit (Bi-exp) and the non-negative least square (NNLS) analysis in fifteen volunteers. The bi-exponential curve fit was performed using the Levenberg-Marquardt non-linear least squares algorithm. The NNLS analysis provided a bi-exponential behavior in seven out of fifteen volunteers. In the last row, the mean values and standard deviation are indicated.

	Bi-exp ADC ($10^{-3} \text{ mm}^2/\text{s}$)	Bi-exp D* ($10^{-3} \text{ mm}^2/\text{s}$)	NNLS ADC ($10^{-3} \text{ mm}^2/\text{s}$)	NNLS D* ($10^{-3} \text{ mm}^2/\text{s}$)	Bi-exp Perfusion Fraction (%)	NNLS Perfusion Fraction (%)
1	0.01	3.01			36	*
2	0.64	--			**	*
3	0.48	22.34	0.49	22.50	16	16
4	0.74	44.36			43	*
5	0.55	22.35	0.56	22.56	17	17
6	0.57	25.73	0.58	25.90	12	12
7	0.67	63.02			57	*
8	0.76	18.67	0.77	18.75	18	18
9	0.01	2.76			33	*
10	0.44	29.88	0.56	29.78	14	14
11	0.01	3.57			16	*
12	0.67	41.79	0.67	43.11	2	2
13	0.59	39.19	0.58	39.30	21	21
14	0.60	566.03			50	*
15	0.11	2.99			50	*
	0.45 ± 0.27	63 ± 145	0.60 ± 0.09	28 ± 9	27 ± 17	14 ± 6

* Volunteers where NNLS did not provided two components.

** Volunteer where bi-exponential fit did not provided two components.