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► **To cite this version:**

Emmanuel Guigon, Pierre Baraduc, Michel Desmurget. Coding of movement- and force-related information in primate primary motor cortex: a computational approach.. *European Journal of Neuroscience*, 2007, 26 (1), pp.250-60. 10.1111/j.1460-9568.2007.05634.x . inserm-00212329

HAL Id: inserm-00212329

<https://inserm.hal.science/inserm-00212329>

Submitted on 13 Jun 2008

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Editor: M. Rushworth

Coding of movement- and force-related information in primate primary motor cortex: A computational approach

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Running head: Optimal motor control

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27 pages / 10 figures / 0 table / 20 equations

Number of words: whole = 8247 / abstract = 162 / introduction = 423

Keywords: Neuron; Force; Muscle; Control; Computer

Abstract

Coordinated movements result from descending commands transmitted by central motor systems to the muscles. Although the resulting effect of the commands has the dimension of a muscular force, it is unclear whether the information transmitted by the commands concerns movement kinematics (e.g. position, velocity) or movement dynamics (e.g. force, torque). To address this issue, we used an optimal control model of movement production which calculates inputs to motoneurons which are appropriate to drive an articulated limb toward a goal. The model quantitatively accounted for kinematic, kinetic and muscular properties of planar, shoulder/elbow arm reaching movements of monkeys, and reproduced detailed features of neuronal correlates of these movements in primate motor cortex. The model also reproduced qualitative spatio-temporal characteristics of movement- and force-related single neuron discharges in nonplanar reaching and isometric force production tasks. The results suggest that the nervous system of the primate controls movements through a muscle-based controller which could be located in the motor cortex.

HAL author manuscript inserm-00212329, version 1

Motor control is central to executive functions of the nervous system. It guarantees that planned actions are efficiently translated into appropriate limb displacements. A striking feature of this translation from “ideas of motion” to “mechanical motion” is the paradoxical contrast between the apparent easiness with which movements are performed on the one hand, and the complexity of Newtonian dynamics, and the existence of multiple levels of redundancy, on the other hand (Bernstein, 1967). Since the time of Bernstein, this paradox has been copiously documented and solutions have been proposed to explain how the nervous system can solve such a challenging problem (Bullock & Grossberg, 1988; Uno *et al.*, 1989; Kalaska & Crammond, 1992; Harris & Wolpert, 1998; Todorov & Jordan, 2002; Guigon *et al.*, 2007). Yet the central issue of the nature of *neural control signals* (NCSs) that flow from central motor systems to the periphery during coordinated movements remains open and hotly debated (Kalaska *et al.*, 1989; Caminiti *et al.*, 1991; Fetz, 1992; Feldman & Levin, 1995; Georgopoulos, 1996; Kakei *et al.*, 1999; Georgopoulos & Ashe, 2000; Moran & Schwartz, 2000; Todorov, 2000, 2003; Scott, 2005; Aflalo & Graziano, 2006).

A common method to address this issue is to record NCSs *in vivo*, e.g. using single unit recordings in primary motor cortex (M1) and spinal cord of behaving animals (monkeys), and to perform a correlation analysis in order to reveal preferential relationships between discharge rates and parameters of motor behavior (e.g. direction of movement, velocity, joint torques; Evarts, 1968; Georgopoulos *et al.*, 1982; Kalaska *et al.*, 1989; Moran & Schwartz, 1999). This method has revealed a large repertoire of discharge patterns as well as a large repertoire of correlations which were thought to reflect sometimes kinematic (direction, velocity), sometimes dynamic (forces) representations of motor acts. However, these correlations were time-varying and complex (Ashe & Georgopoulos, 1994; Fu *et al.*, 1995),

and were in general contaminated by real or apparent covariations among parameters (Mussa-Ivaldi, 1988; Todorov, 2000; Scott, 2005). Furthermore, as correlations do not imply causality, neurophysiological data are not sufficient to draw firm conclusions on this issue.

A complementary approach is to define the requisite characteristics of neural control signals based on a model of motor control and to compare requisite and actual properties of these signals (Lan, 1997; Bullock *et al.*, 1998; Todorov, 2000; Haruno & Wolpert, 2005). Here, we exploit an optimal control model which quantitatively accounts for kinematic and dynamic properties of redundant manipulators (Guigon *et al.*, 2007) to address the nature of neural control signals generated by the nervous system to control arm reaching movements.

Materials and Methods

Scope of the model

To properly ascertain the contribution of neural activities to movement control, it is necessary to consider neural and movement data simultaneously. An appropriate animal (monkey) model of this situation is obtained using a mechanical exoskeleton which puts constraints on the degrees of freedom (DOF) involved in the movement (Scott *et al.*, 2001; Graham *et al.*, 2003; Kurtzer *et al.*, 2006). In this case, the mechanical apparatus can be represented by a planar two-joint arm. In other studies of interest (Caminiti *et al.*, 1991; Sergio & Kalaska, 1998; Kakei *et al.*, 1999; Sergio *et al.*, 2005), the movements involved more than 2 DOF. In theory, the model could be used to address these experiments (Guigon *et al.*, 2007). However, not enough kinematic and kinetic data are available in these studies for a thorough comparison between experimental observations and predictions of the model. Accordingly, we thoroughly and quantitatively addressed the neural control of planar two-joint arm

movements. In this framework, we also reproduced qualitative aspects of motor cortical discharge related to nonplanar arm reaching movements (Sergio & Kalaska, 1998; Sergio *et al.*, 2005).

The model described in this article is formally identical to the model used in Guigon *et al.* (2007). Yet the two articles address complementary issues. In the previous article, we described predicted kinematic and dynamic characteristics of upper limb movements. Here, we focus on the nature of the predicted control signals which are responsible for these movements. For clarity, we give below a brief overview of the model, but a thorough presentation can be found in Guigon *et al.* (2007).

Overview of the model

In a schematic view of motor control, a cortical motor center sends a command to a neuromuscular apparatus (motoneuron + muscle) which generates a force to displace a set of articulated segments. Formally, this series of events can be represented by the action of a *controller* upon a *controlled object*. Mathematically, the behavior of the controlled object can be described by a state-dependent dynamics

$$d\mathbf{x}/dt = f(\mathbf{x}(t), \mathbf{u}(t)), \quad (\text{Eq. 1})$$

where \mathbf{x} is the state vector of the object (position, velocity, muscle state, ...), and $\mathbf{u} = \{u_i\}$ ($1 \leq i \leq M$, M number of muscles) the control vector (or *control signal*; CS) transmitted by the controller. A control problem corresponds to the mastering of the controlled object, i.e. find a time series of control $\mathbf{u}(t)$ (t in $[t_0; t_f]$) in order to satisfy to constraints of a *task*, e.g.

$$\mathbf{x}(t_0) = \mathbf{x}_0 \text{ and } \psi(\mathbf{x}(t_f)) = 0, \quad (\text{Eq. 2})$$

where function ψ expresses constraints on the final state of the object.

Once the control problem is solved, the quantities $\mathbf{x}(t)$ and $\mathbf{u}(t)$ can be analyzed and compared to corresponding quantities obtained in experimental studies: position/velocity to movement kinematics, force/torque to movement dynamics, control to cortical activity.

In the framework of this study, an appropriate controller should meet the following requirements: 1. to provide a unique solution in the face of spatial, temporal, kinematic and muscular redundancy; 2. to provide a solution which has realistic kinematic characteristics. We have shown previously that a controller which chooses, among solutions to Eqs. 1 and 2, the unique solution that minimizes overall control magnitude (E , *effort*)

$$E^2 = \int [t_0; t_f] \|\mathbf{u}(t)\|^2 dt, \quad (\text{Eq. 3})$$

where $\|\mathbf{u}(t)\|$ is the norm of vector \mathbf{u} , comply with these requirements (Guigon *et al.*, 2007). Technically, \mathbf{u} is the solution of an optimal control problem. Since the focus of this article is the issue of the nature of neural control signals which are elaborated by the nervous system to produce coordinated movements, we do not intend here to show that this controller is more realistic or efficient than other controllers. The fact that results described below could be obtained with other controllers is not at all detrimental to our purpose.

In general, Eq. 1 includes both dynamic (inertial, velocity-dependent) and static (elastic, gravitational) forces. A series of arguments (reviewed in Guigon *et al.*, 2007) suggests that the nervous systems processes the two types of force separately (*separation principle*), i.e.

$$\mathbf{u}(t) = \mathbf{u}_{\text{dyn}}(t) + \mathbf{u}_{\text{stat}}(t),$$

where $\mathbf{u}_{\text{dyn}}(t)$ is the solution to the optimal control problem without static forces, and $\mathbf{u}_{\text{stat}}(t)$ compensates for applied static forces. In the following, we only address the nature of dynamic CSs, in the absence of static forces. In the following \mathbf{u} corresponds to \mathbf{u}_{dyn} .

The controller is described here as an open-loop controller. However, it should be noted that the model is affiliated with a principled approach to motor control which states that feedback is a necessary component of an appropriate neural controller (Guigon *et al.*, 2007). Thus the controller can be considered as an optimal feedback controller, i.e. a controller which calculates the appropriate command to reach a goal for any estimate of the state of the controlled system (see also Todorov, 2004; Scott, 2004). Such a model can work properly in the presence of noise in sensory and motor pathways, and perturbations on limb or target position (Todorov & Jordan, 2002; Guigon *et al.*, 2007). In practice, the feedback component remains hidden since neither perturbations nor noise were introduced in the simulations. The results described below can be considered as mean data over noise distributions.

Controlled object

The controlled object was a planar, two-joint (shoulder, elbow) arm actuated by two pairs of monoarticular muscles and one pair of biarticular muscles (Fig. 1A). For each muscle, actual force F was calculated following Zajac (1989) and Brown *et al.* (1996). We used

$$F = \Gamma \times \text{PCSA} \times F_a(u) \times (F_v \times F_L + F_p) \quad (\text{Eq. 4})$$

where

- u is a control input (component of vector \mathbf{u} for the corresponding muscle),
- Γ is a tension scaling factor,
- PCSA is the physiological cross-sectional area,
- F_a is a unitless quantity derived from muscle input,

$$F_a = \eta(a)$$

$$v \, da/dt = -a + e \quad (\text{Eq. 5})$$

$$v \, de/dt = -e + u$$

where a and e are muscle activation and excitation, $\eta(z) = [z]^+$ ($[z]^+ = z$ if $z > 0$ otherwise $[z]^+ = 0$), v is a parameter;

- F_p reflects passive forces

$$F_p = c_2 \{ \exp[k_2(L-L_{r2})] - 1 \}$$

where L is the normalized muscle length (the normalization factor is the length L_0 at which maximal isometric force is generated), c_2 , k_2 , L_{r2} are parameters;

- F_L and F_V are related to force-length and force-velocity curves of the muscle,

$$F_L = \exp\{ -[(L^\beta - 1)/\omega]^\rho \}$$

$$F_V = (b_1 - a_1 V)/(V + b_1) \quad \text{if } V < 0 \text{ (shortening muscle)}$$

$$F_V = (b_2 - a_2 V)/(V + b_2) \quad \text{if } V > 0 \text{ (lengthening muscle)}$$

where V is the normalized muscle velocity (in units of L_0/s), β , ω , ρ , a_1 , b_1 , a_2 , b_2 are parameters. The quantity $F_V \times F_L + F_p$ is plotted as a function of L and V in Fig. 1B. (Fig. 11B in Brown *et al.*, 1996).

The muscle forces were translated into joint torques according to

$$T_{sh} = \gamma_{sh}^{FL} \times F_{sh}^{FL} - \gamma_{sh}^{EX} \times F_{sh}^{EX} + \gamma_{bish}^{FL} \times F_{bi}^{FL} - \gamma_{bish}^{EX} \times F_{bi}^{EX}$$

$$T_{el} = \gamma_{el}^{FL} \times F_{el}^{FL} - \gamma_{el}^{EX} \times F_{el}^{EX} + \gamma_{biel}^{FL} \times F_{bi}^{FL} - \gamma_{biel}^{EX} \times F_{bi}^{EX}$$

where γ_{xx}^{YY} are the moment arms of the muscle, with $xx = \{sh, el, bi, bish, biel\}$ and $YY = \{FL, EX\}$, sh = shoulder, el = elbow, bi = biarticular, FL = flexor, EX = extensor.

The controlled object contains two elements which are thought to play an important role in motor control: 1. force-length and force-velocity relationships in muscles (Todorov, 2000); 2. biarticular muscles (van Bolhuis *et al.*, 1998). To address the influence of these elements in the framework of this study, we considered two modified versions of the model: 1. a model (NOLV) without force-length and force-velocity relationships in the muscles (i.e. $F = \Gamma \times \text{PCSA} \times F_a$ in Eq. 4); 2. a model (NOBI) without biarticular muscles ($\gamma_{bi}^* = 0$).

Neural control signals

The control problem (Eqs. 1,2,3) was modified to account for the fact that there are many more neurons potentially involved in motor commands than muscles. We assumed that 1. the number s of control signals was larger than the number M of muscles; 2. each control signal was defined by a fixed synergy of muscles (Eq. 7); 3. the s synergies were uniformly distributed in muscular space (Eq. 7). Formally, the problem was similar to the problem defined by Eqs. 1,2,3 with the following change. The goal was to find minimum control $\mathbf{U}(t) = \{U_j(t)\}$ ($1 \leq j \leq s$), i.e the unique solution that minimizes

$$E^2 = \int_{[t_0; t_f]} \|\mathbf{U}(t)\|^2 dt, \quad (\text{Eq. 6})$$

and is appropriate to displace the articulated segments between given initial and final positions, the muscular control vector $\mathbf{u}(t) = \{u_i(t)\}$ ($1 \leq i \leq M$) being defined by

$$u_i(t) = \sum_{j=1..s} \beta_{ij} U_j(t), \quad (\text{Eq. 7})$$

where β_{ij} are random coefficients drawn from a uniform distribution in $[-1;1]$. The control signals $\{U_j(t)\}$ are called neural control signals (NCSs).

Tasks

To simulate arm movements, the torques (T_{sh}, T_{el}) were translated into displacements using the dynamics of the articulated segments (Newtonian dynamics; Guigon *et al.*, 2007). The control vector was

$$\mathbf{u}(t) = [u_1, u_2, u_3, u_4, u_5, u_6]$$

i.e. the control for the shoulder flexor, shoulder extensor, elbow flexor, elbow extensor, biarticular flexor, biarticular extensor, in this order. For a *movement* task, the state vector was

$$\mathbf{x}(t) = [q_1, q_2, dq_1/dt, dq_2/dt, a_1, a_2, a_3, a_4, a_5, a_6, e_1, e_2, e_3, e_4, e_5, e_6],$$

where q_1 and q_2 are the shoulder and elbow angles, dq_1/dt and dq_2/dt the shoulder and elbow velocities. The boundary conditions (Eq. 2) were the initial and final arm postures with zero initial and final velocity, activation and excitation (i.e. $\mathbf{x}(t_0) = \mathbf{x}_0$ and $\psi = \mathbf{x}(t_f) - \mathbf{x}_f$), where

$$\mathbf{x}_0 = [q_{10}, q_{20}, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]$$

and

$$\mathbf{x}_f = [q_{1f}, q_{2f}, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0].$$

To simulate *isometric force production*, the torques were translated into endpoint force (Φ) using

$$\mathbf{T} = \mathbf{J}(\mathbf{q})^T \Phi,$$

where $\mathbf{T} = [T_{sh} \ T_{el}]^T$, and $\mathbf{J}(\mathbf{q})$ is the Jacobian matrix of the kinematic transformation at position $\mathbf{q} = [q_1 \ q_2]^T$. The state vector was

$$\mathbf{x}(t) = [a_1, a_2, a_3, a_4, a_5, a_6, e_1, e_2, e_3, e_4, e_5, e_6].$$

A force trajectory was specified by initial and final forces (Φ_0 and Φ_f). The boundary conditions were

$$\mathbf{x}_0 = [a_{10}, a_{20}, a_{30}, a_{40}, a_{50}, a_{60}, e_{10}, e_{20}, e_{30}, e_{40}, e_{50}, e_{60}]$$

and

$$\psi(\mathbf{x}(t_f)) = \mathbf{T}(t_f) - \mathbf{T}_f$$

where $\mathbf{T}_f = \mathbf{J}(\mathbf{q})^T \Phi_f$. For simulations, $(q_1, q_2) = (q_{10}, q_{20})$.

Solution to the optimal control problem

The problem defined by Eqs. 1,2,3 or Eqs. 1,2,6,7 was solved numerically using a gradient method (Bryson, 1999; Guigon *et al.*, 2007). The results were obtained as $\mathbf{x}(t_k)$, $\mathbf{u}(t_k)$, (or $\mathbf{U}(t_k)$) for

$$t_k = t_0 + (t_f - t_0)k/n \quad (\text{Eq. 8})$$

with $k = 0 \dots n$, and $n = 50$.

Data analysis

The CSs and NCSs can be considered as inputs to motoneurons (Eq. 4), and could correspond to activities in subsets of cortical and spinal neurons. They were analyzed as if they were the discharge of motor cortical neurons, i.e. by quantifying their directional tuning using regression analysis (Georgopoulos *et al.*, 1982). For each NCS, preferred directions (PDs) were calculated at each timestep t_k ($0 \leq k \leq n$). The main PD was defined as $\text{PD}(t = t_0)$. Population vectors were calculated following classical techniques. Bimodal distributions were frequently encountered, and were quantified by a preferred axis as defined by principal

component analysis. Electromyographic (EMG) activity was defined as $[e]^+$ (e , excitation; Eq. 5).

Parameters and comparison with experimental data

The model was built for a direct comparison with experimental data in monkeys (Scott *et al.*, 2001; Graham *et al.*, 2003; Kurtzer *et al.*, 2006). Thus, a number of parameters were directly taken from monkey data. Biomechanical parameters (segment inertia I in kg m^2 , mass m in kg , center of mass cof in % of the length, length L in m) were taken from Cheng & Scott (2000) for *Macaca mulatta*. Indexes 1 and 2 are used for upper arm and forearm, respectively. We used $I_1 = 0.00126$, $m_1 = 0.699$, $\text{cof}_1 = 0.5$, $L_1 = 0.144$, $I_2 = 0.00621$, $m_2 = 0.781$, $\text{cof}_2 = 0.375$, $L_2 = 0.257$. Muscular parameters were taken from Brown *et al.* (1996): $c_2 = -0.02$, $k_2 = -18.7$, $L_{r2} = 0.79$, $\beta = 2.3$, $\omega = 1.26$, $\rho = 1.62$, $a_1 = 0.17$, $b_1 = -0.69$, $b_2 = 1.8$, $a_2 = pL^2 + qL + r$, $p = -5.34$, $q = 8.41$, $r = -4.7$. Muscle time constant was $\nu = 0.05 \text{ s}$ (van der Helm & Rozendaal, 2000). The moment arms (Graham & Scott, 2003) are shown in Fig. 1C.

Parameters which are less well defined are the tension scaling factor Γ (Buchanan, 1995), and the PCSAs which depend on the muscles which are actually involved at a given articulation. We chose $\Gamma = 35 \text{ N/cm}^2$, and the PCSAs were used as free parameters, and were adjusted according to the following criteria: 1. Each PCSA is in a reasonable range ($1\text{-}15 \text{ cm}^2$); 2. Movement trajectories have a direction-dependent curvature (Fig. 1 in Graham *et al.*, 2003); 3. Spatial selectivity of the muscles is as close as possible as that described by Kurtzer *et al.* (2006). Yet, as the model entails a number of simplifications, we thought that the search of an exact fit of the data would be meaningless. Thus, we used a set of PCSAs which provide a good description of experimental observations. The PCSAs (in cm^2) were (for shFL, shEX,

eIFL, eEX, biFL, biEX): 10, 10, 11, 11, 9.9, 9.9.

For comparison between outcomes of the model and experimental data, we either reproduce an original figure, or indicate in the text a reference to one or more published figures.

Results

Properties of planar, 2-DOF reaching movements

Mechanical, muscular and neural characteristics of planar, 2-DOF reaching movements have been thoroughly studied by Scott *et al.* (2001), Graham *et al.* (2003), and Kurtzer *et al.* (2006) (noted Scott, Graham and Kurtzer below). In these experiments, monkeys performed radial reaching movements toward 16 targets. Movement amplitude was 6 cm, and movement duration was ~ 600 ms (576 ms in Scott; Figs. 1,2 in Graham; Figs. 1,2 in Kurtzer). Initial posture was $\sim (30^\circ, 90^\circ)$ in Graham and Kurtzer (Fig. 2C in Graham; p 3221 in Kurtzer), but was not reported in Scott. In this latter case, we used $(30^\circ, 80^\circ)$ which provides a good fit to the data. We simulated similar movements with the model, and we obtained movement kinematics (trajectories), movement kinetics (torques, power), muscular activities and neural control signals.

Kinematics and kinetics

Trajectories are shown in Fig. 2A, and Fig. 1A,B,C in Graham for comparison. Note that the model accounted for directional variations in movement curvature (see also Guigon *et al.*, 2007). The model also reproduced the anisotropy in motion at shoulder and elbow joints (Fig. 2B,C,D,E,F; Fig. 3A,C,D,E,F in Graham, Fig. 2C in Kurtzer). The kinetic data reported

by Graham concerned active torques, i.e. the combination of passive torques generated at shoulder and elbow and voluntary muscular torques. Active torques were obtained with the model by subtracting modeled passive torques (from Fig. 3C,D in Graham) from actual torques generated by the controller. The results are shown in Fig. 3. The model reproduced directional variations in peak active torque (Fig. 3A,B,C; Fig. 5A,B,C in Graham, Fig. 2C in Kurtzer) and peak joint power (Fig. 3D,E,F; Fig. 8A,B,C in Graham). A difference between the experiment and the model was found for the spatio-temporal profile of active shoulder torques (Fig. 3B; Fig. 5B in Graham). A possible reason for this difference is related to approximations in the representation of the passive torques. Similar results were obtained with the modified models (NOLV and NOBI).

Muscular activity

Peak muscular activities varied with movement direction (Fig. 4A; Fig. 6 in Kurtzer). The monoarticular muscles behave as found experimentally [130°-309° (model) vs 130°-319° (Kurtzer) axis for the shoulder muscles; 271°-73° (model) vs 275°-70° (Kurtzer) axis for the elbow muscles]. We could not reproduce the observations of Kurtzer on the activities of the biarticular muscles. The origin of this discrepancy is unclear. We first note that the search over PCSAs has never lead to activities of the biarticular muscles as predicted by Kurtzer. Furthermore, similar results were reported by Li (2006) with a closely related model (her Fig. 5.7; see also Todorov & Li, 2005). Thus our results could hardly be ascribed to some errors in the simulations of the model. To deepen this issue, we have plotted the preferred axis of the 6 muscular types obtained by Kurtzer in monkeys, by Li (2006) and by us in an optimal control model, and by Welter & Bobbert (2002) in humans (Fig. 4D). We observed that the tuning of the monoarticular muscles is consistent across the studies, but there is a noteworthy

discrepancy between Kurtzer and the other studies for the biarticular muscles (* in Fig. 4D). We also note that the model proposed by Kurtzer to explain their data does not reproduce the tuning of the biarticular muscles (their Fig. 11C). The discrepancy between the model and the data does not prevent the model to explain the characteristics of neural control signals (see below).

Neural control signals

We analyzed the NCSs ($s = 500$) corresponding to movements from initial posture ($30^\circ, 80^\circ$). We calculated the main preferred direction of each NCS (see **Materials and Methods**) and the distribution of main PDs over the NCSs. This distribution was anisotropic with a preferred axis along $123-303^\circ$ (Fig. 5A; $118-298^\circ$, Fig. 3 in Scott). The population vector systematically deviated from movement direction (Fig. 5B; Fig. 2A in Scott). We explored the relationship between PD distribution and direction-dependent variations in peak angular velocity, peak joint torque, and peak joint power. The best correlation was found with peak joint power (Fig. 5D; Fig. 4 in Scott).

The PD distribution remained anisotropic for different orientations of the arm and the forearm, and its orientation rotated with both shoulder and elbow angles (Fig. 6A,B). These results can be considered as predictions since the corresponding experiment has not been performed with a mechanical exoskeleton. Yet, they are consistent with results obtained with other kinematic chains (Caminiti *et al.*, 1991; Kakei *et al.*, 1999).

Similar results were obtained with the modified models (NOLV and NOBI). However, the correlations with peak joint power were weaker (not shown), and the PD distribution rotated more steeply with elbow angle (Fig. 6B).

Other movements

Complementary information on the nature of NCSs can be found in other studies which analyzed the temporal structure of motor cortical discharges during reaching movements and isometric force production (Sergio & Kalaska, 1998; Sergio *et al.*, 2005). However, as neither kinematics nor kinetics were quantitatively described in these studies, we only addressed qualitative features of neural discharges. Furthermore, as we found that all the NCSs were qualitatively similar, we only analyzed the 6 CSs (one per muscle).

The raw temporal profile of the shoulder extensor control is shown in Fig. 7 for movements in 8 directions (Fig. 7, center). The control had: 1. an early phasic component followed by a depression for the rightward/downward movements; 2. a delayed phasic component for a movement in the opposite directions. We note that quantitatively similar results were obtained with the NOLV model (Fig. 7, *gray lines*). Similar temporal profiles were found for the other muscles, each with its preferred directional tuning (not shown). For comparison with experimental data, we have replotted the control for the shoulder extensor in a different format which can be read as a mean discharge frequency (Fig. 8A). Data from single unit recording in primate primary motor cortex are reproduced (Fig. 1 in Sergio & Kalaska, 1998; Fig. 8B). Visual inspection revealed a close correspondence between real and simulated profiles although a difference was visible at the end of the movement (see **Discussion**). We note that the large phasic transient near the end of the movement (Fig. 7; Fig. 8A) is due a strict boundary condition (Eq. 2): the movement must finish at a given time and position. This type of boundary condition was chosen for simplicity, but requires large controls to guarantee the exact fulfillment of spatial and temporal constraints. Yet real movements do not in general terminate abruptly, but end up smoothly, e.g. with oscillations.

A more realistic movement could be obtained in the presence of noise. In this case, estimated limb position is in general different from actual limb position so a nonzero residual error should always be present to drive movement corrections. This case is illustrated in Fig. 1D of Guigon *et al.* (2007).

For comparison, we applied the model to the production of isometric forces in different directions. Since the calculated control signals are related to dynamic forces, they are not responsible for static force exertion after the dynamic period. To obtain more realistic control signals, we added a static component necessary for the maintenance of a steady final force. For a 150-ms force increase from 0 to 1.5 N, the temporal profile of the shoulder extensor control signal had a phasic excitation for a rightward-directed force (Fig. 9A, *right*) and a phasic inhibition for a leftward force (Fig. 9A, *left*). Data from single unit recording in primate primary motor cortex are reproduced (Fig. 1 in Sergio & Kalaska, 1998; Fig. 9B).

Preferred directions of the CSs were calculated every 10 ms and displayed in a circular plot (Fig. 10). In the movement task (Fig. 10A; from top to bottom, sh, el, bi; *black circle*: flexor; *gray circle*: extensor), the PD reverted during the movement. In contrast, the isometric controls did not revert their PDs (Fig. 10B). For comparison, data from Sergio & Kalaska (1998) are reproduced in Fig. 10C.

Discussion

The present article describes a model-based approach to the nature of neural control signals generated by the nervous system of monkeys to control arm movements. The model reproduces detailed features of movement kinematics and kinetics, and quantitative characteristics of single neuron and population discharges in primate motor cortex. The

results support the idea that 1. the motor system controls movement using a muscle-based controller; 2. this controller could be located in the motor cortex.

Nature of the model

The model is an optimal controller, i.e. a controller which calculates appropriate control signals to displace a controlled object using a complete knowledge of the properties of the object (here, the dynamics of the arm and the characteristics of the muscles), and an optimality criterion. Recent reviews have thoroughly advocated this type of model to address behavioral and neural characteristics of goal-directed movements (Todorov, 2004; Scott, 2004). We refer the reader to these reviews for a detail discussion of optimal control models.

The present model is not fundamentally different from previous models which applied optimal control techniques to determine the spatio-temporal nature of command signals which should enter a neuromuscular system to drive a limb toward a goal (Happee, 1992; Lan & Crago, 1994; Lan, 1997; Harris & Wolpert, 1998; Haruno & Wolpert, 2005; Todorov & Li, 2005; Li, 2006). A common result of these models is that optimal control of a low-pass filtering force generating system leads to reasonably realistic EMG and neural control signals. The originality of this work is not to describe a new, more efficient model, but to deepen our understanding of neural information processing in motor cortex using a model-based approach, which proves that observed discharge characteristics of single neurons and populations recorded during movements in M1 can be quantitatively explained by observed characteristics of the movements. In fact, previous models have addressed properties of neurons, but not properties of limb movements (Lan, 1997; Bullock *et al.*, 1998; Todorov, 2000; Haruno & Wolpert, 2005; Trainin *et al.*, 2007).

Limitations

There are at least three limitations to the present model. First, although the model appropriately produces the expected results, the issue of its validity in a broader framework remains open. The model was actually tested in various conditions, and was found to be consistent with experimental observations (Guigon *et al.*, 2007). Yet some data, e.g. highly nonsymmetric velocity profiles, cannot be explained by the model. Second, the way optimal feedback control can be computed by brain circuits remains elusive. A third and related limitation is the absence of relationship between the computational processes advocated by the model and organizational features of the motor cortex (connectivity, intrinsic properties, ...). The two latter issues raise the problem of neural information processing subserving motor control. This problem has been addressed for initial directional commands of reaching movements (Baraduc *et al.*, 2001), but remains open for the whole spatiotemporal commands.

Motor cortical physiology

Single cell recordings in M1 have revealed a large repertoire of discharge patterns. In fact, the greater part of movement parameters, ranging from exerted force (low-level muscle control) to serial order of stimuli (cognitive motor control) have been found to influence the discharge of motor cortical neurons (Ashe, 1997; Georgopoulos, 2000). This paradox is hotly debated (Georgopoulos & Ashe, 2000; Moran & Schwartz, 2000; Todorov, 2000). A central issue of the debate is the interpretation of correlation analyses which are used to quantify neuronal activities. For instance, Todorov (2000) defends the view that M1 neurons calculate muscular activation patterns, and suggests that many correlations between kinematic quantities and neural discharges in M1 can be explained by this hypothesis (i.e. they are artifacts). In this

framework, a series of studies by Scott and collaborators have attempted to circumvent the weakness of correlation analysis (Scott *et al.*, 2001; Graham *et al.*, 2003; Kurtzer *et al.*, 2006). They reported a systematic description of planar two-joint arm movements and neural correlates of their execution. They found that anisotropic characteristics of movement dynamics and muscular selectivities were associated with a similar anisotropy in neural selectivities. Our model reproduces a similar relationship between mechanical, muscular and neural quantities, and supports the contention of Scott of a tight link between neural populations in M1 and the motor apparatus. The model further shows that the spatio-temporal profile of the NCSs is qualitatively similar to the activity in a subpopulation of motor cortical neurons (located primarily in caudal M1) whose discharge tightly follows the time course of required task dynamics (Sergio & Kalaska, 1998; Sergio *et al.*, 2005). Taken together, these results suggest that a subset of M1 neurons could actively participate to a muscle-based representation of movements (Todorov, 2000, 2003; Sergio *et al.*, 2005). Although a number of arguments concur to this conclusion (Scott, 1997; Todorov, 2000, 2003), our model provides the first realistic demonstration that muscle-based coding can account simultaneously for movement kinematics, movement kinetics, EMGs, and cortical discharges.

If our conclusions are correct, the origin and function of other types of neuron (e.g. those related to visuospatial and kinematic representations of movements) remain to be explained. There are at least two hypotheses. The *first* is related to the idea of *sensorimotor transformations* (Kalaska & Crammond, 1992; Scott, 2005). The assumption is that the nervous system performs sequential operations which progressively translate spatial information on the goal of the movement into appropriate commands, going through kinematic, dynamic, and muscular stages. In this case, quantities related to desired movement

kinematics, in particular desired movement velocity, should be found in M1 (Moran & Schwartz, 1999). This explanation relies on the questionable idea that motor control is based on trajectory tracking (Todorov & Jordan, 2002; Guigon *et al.*, 2007). The second hypothesis ensues from the model. As discussed in the **Materials and Methods**, the controller can be considered as an optimal feedback controller, i.e. an optimal controller coupled with a state estimator. We have described properties of the signals elaborated by the controller. Yet other signals should be available to indicate the goal and the estimated state. This latter signal should convey information related to predicted position, velocity, force, ... Such a predictive (rather than desired) signal could be a source of kinematic information in motor cortex. For instance, cortical velocity signals have been described in M1 which lead actual velocity by 120-150 ms (Moran & Schwartz, 1999; Wang *et al.*, 2007). As the control signals reported in other studies lead movement onset by 100-200 ms (Kalaska *et al.*, 1989; Sergio & Kalaska, 1998; Sergio *et al.*, 2005), it is possible that the velocity signals derive from the control signals through a forward model. However, these data could also be interpreted to support the presence of a desired velocity signal.

Todorov (2000) has proposed that the dependence of muscle force on length and velocity has a substantial influence on neural information processing in motor cortex. Kurtzer *et al.* (2006) have suggested that these intrinsic muscular properties are necessary to account for the directional tuning of muscular activities. Our model does not concur with these ideas. First, the temporal profile of our control signals did not resemble a velocity profile (Fig. 7; Fig. 2 in Todorov, 2000). In fact, low-pass filtering renders the control signals much more “phasic” than velocity, even in the presence of a force/velocity relationship in the muscles. Second, muscular tuning was only weakly influenced by force/length and force/velocity relationships

(Fig. 4).

According to the separation principle (Guigon *et al.*, 2007), a complete motor command involves both a static and a dynamic component. Although such components have been observed experimentally in M1 (Cheney & Fetz, 1980; Kalaska *et al.*, 1989; Kurtzer *et al.*, 2005), the discharge of many motor cortical neurons appears to carry simultaneously static and dynamic commands (Cheney & Fetz, 1980; Kalaska *et al.*, 1989; Sergio & Kalaska, 1998; Kurtzer *et al.*, 2005; Sergio *et al.*, 2005). For instance, phasic-tonic neurons recorded by Sergio & Kalaska (1998) have an early component that could be related to the control of dynamic forces (compare Fig. 8A and 8B), and a late component that could be related to the maintenance of posture against a steady force. In fact, Sergio & Kalaska (1998) have found phasic, tonic, and phasic-tonic neurons in equal proportions (~30%), and it is possible that their phasic neurons (not described in detail) are closer to our NCSs than the phasic-tonic neurons. In this case, the phasic and tonic neurons would represent the actual dynamic and static commands as defined by the model. This issue remains to be tested experimentally.

Models of motor control

The debate on the nature of motor cortical representations of movement is part of a more general debate on the nature of motor controllers in the brain (Kawato, 1999; Ostry & Feldman, 2003; Todorov, 2003). On the one hand, *position control* models exploit viscoelastic properties of muscles and peripheral reflex loops to define limb movements as a series of stable equilibrium postures (Bizzi *et al.*, 1992; Feldman & Levin, 1995). The corresponding descending commands can be viewed as kinematic signals as they need not take into account biomechanical or muscular characteristics of the moving limb (Flanagan *et*

al., 1993; Georgopoulos, 1996). By construction, the temporal profile of these commands is monotonic. Computer simulations have shown that triphasic EMG patterns can be obtained from monotonic commands that act to modify the recruitment threshold of muscles rather than the force developed by the muscles (St-Onge *et al.*, 1997; Suzuki & Yamazaki, 2005). On the other hand, *force control* models have been developed, based on the idea that the nervous system explicitly computes time-varying control signals to achieve a desired movement (Kawato *et al.*, 1987; Uno *et al.*, 1989; Todorov, 2000; Franklin *et al.*, 2003). Although this type of model has been questioned based on the posture/movement paradox (Ostry & Feldman, 2003), it has proven highly efficient to account for a large range of characteristics of motor control (trajectory formation, EMG). The force control models predict that the neural control signals should have nonmonotonic (acceleration-like, torque-like, EMG-like) profiles. The present model, which is affiliated to the force control models (in the sense that the control signals are directly transmitted to a force-generating system), shows that the predicted nonmonotonic NCSs are quantitatively related to the spatio-temporal characteristics of a population of motor cortical neurons. There is no corresponding study of the control signals predicted by position control models and their relationship to cortical physiology. In particular, the origin and role of nonmonotonic discharge patterns in the framework of position control models remain unclear (Todorov, 2003). Although our model cannot directly settle the controversy between force and position control, it gives a physiological basis to the force control models, and contributes to a series of arguments which support these models (Kawato, 1999; Todorov, 2000, 2003; Guigon *et al.*, 2007).

Acknowledgments

We thank Marc Maier for fruitful discussions.

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Figure captions

Figure 1. *A.* Model of a planar, two-joint arm equipped with two pairs of monoarticular antagonist muscles, and one pair of biarticular muscles. Muscle names are indicated for correspondence with the study of Kurtzer *et al.* (2006). *B.* Length-velocity force curve. *C.* Moment arms at shoulder (*left*) and elbow (*right*) for the monoarticular (*thin black line*) and biarticular (*thick gray lines*) muscles (positive for flexors; negative for extensors).

Figure 2. *A.* Trajectories and velocity profiles for movements in 16 directions. R: right, A: away, L: left, T: toward. Initial posture was $(30^\circ, 90^\circ)$. *B.* Polar plot of peak shoulder (*black line*) and elbow (*green line*) velocity. Arrows indicate the mean bimodal distribution (*dashed lines* from Graham, Fig. 2C). *C.* Spatial map of instantaneous angular velocity at shoulder at each location in space along the movement. *D.* Same as *C* for elbow velocity. *E.* Change in joint joint in joint angle coordinates. Colors are used to indicate the 4 cardinal directions. *F.* Change in joint velocity in joint angle coordinates.

Figure 3. *A.* Polar plot of peak shoulder (*black line*) and elbow (*green line*) torque. Arrows indicate the mean bimodal distribution (*dashed lines* from Graham, Fig. 5A). *B.* Spatial map of instantaneous shoulder torque at each location in space along the movement. *C.* Same as *B* for elbow torque. *D.* Same as *A* for peak shoulder and elbow joint power (*dashed lines* from Graham, Fig. 8). *E.* Same as *B* for shoulder joint power. *F.* Same as *E* for elbow joint power.

Figure 4. *A. (Top)* Polar plot of peak shoulder muscle flexor (*black*) and extensor (*gray*) activity. Arrows indicate the preferred axis of the distribution (*dashed lines* from Kurtzer,

Fig. 6). The dashed line for the shoulder flexor is exactly behind the arrow. (*Middle*) Same as *Top* for the elbow flexor and extensor. (*Bottom*) Same as *Top* for the biarticular flexor and extensor. *B*. Same as *A* for the model NOLV. *C*. Same as *A* for the model NOBI. *D*. Orientation of the preferred axis of muscles obtained from 4 sources. For each muscle, four results are given (black: experiment; gray: model): 1. data of Kurtzer (their Fig. 6); 2. model of Li (2006) (her Fig. 5.7c). As initial posture was (45°,90°), we subtracted 15° to the reported orientations; 3. our results (*A*); 4. data of Welter & Bobbert (2002) (their Fig. 5). As initial posture was (0°,90°), we added 30° to the reported orientations. * indicates a noteworthy discrepancy.

Figure 5. *A*. Frequency distribution of the preferred directions of the NCS ($s = 500$; mean $R^2 = 0.91$). Radial axis is the number of NCSs in a bin (16 bins, bin size is 22.5°). *Solid arrow* is the preferred axis of the distribution. *Dashed arrow* from Scott. *B*. Population vector (*arrow*) vs movement direction (*gray*) for the 16 directions. *C*. Difference between the direction of the population vector and the movement direction as a function of movement direction. *D*. Relationship between NCSs count and peak joint velocity (*top*), peak joint torque (*middle*), and peak joint power (*bottom*) for data in *A*. The regression line is shown. From *top* to *bottom*: $R^2 = 0.46, 0.07, 0.75$.

Figure 6. *A*. Preferred axis of the PD distribution as a function of the shoulder angle (10-50°). Elbow angle was 90°. Slope was 0.98 ($R^2 = 1$). *Gray lines*: results obtained with the model NOLV (*square*) and the model NOBI (*diamond*). Inset: initial arm postures. *B*. Preferred axis of the PD distribution as a function of the elbow angle (70-130°). Shoulder angle was 30°. Slope was 0.61 ($R^2 = 0.98$). *Gray lines*: see *A*. Inset: initial arm postures.

Figure 7. Temporal profile of the shoulder extensor NCS for movements in 8 directions. The NCS is depicted with a *black* surface, and takes both positive (above the gray surface) and negative (with in the gray surface) values. The *gray* lines are the results obtained with the model NOLV. Time scale is in ms. The trajectories are shown in the middle.

Figure 8. A. Temporal profile of the shoulder extensor NCS for a leftward (*left*) and a rightward (*right*) movement. Same data as in Fig. 7, but in a different format. *Gray line*: endpoint force (shifted in time by 100 ms for correspondence with experimental data). B. Reproduced from Sergio & Kalaska (1998), Fig. 1.

Figure 9. A. Same as Fig. 8A for an isometric force production (0 to 1.5 N in 150 ms). The time course of force variation is shown in *gray*. Inset: force trajectory (open square: origin; open circle: extremity). B. Reproduced from Sergio & Kalaska (1998), Fig. 1.

Figure 10. A. Time course of preferred directions of CSs in the reaching task. Time is indicated by the distance from the center (-300 ms) to the external circle (900 ms). PD is indicated by an angular position. (*Top*) Shoulder flexor (*black*), shoulder extensor (*gray*). (*Middle*) Elbow flexor (*black*), elbow extensor (*gray*). (*Bottom*) Biarticular flexor (*black*), biarticular extensor (*gray*). B. Same as A for the isometric force production task. The two insets indicate the timing for A (*top* inset) and B (*middle* inset). C. Reproduced from Sergio & Kalaska (1998), Fig. 2.

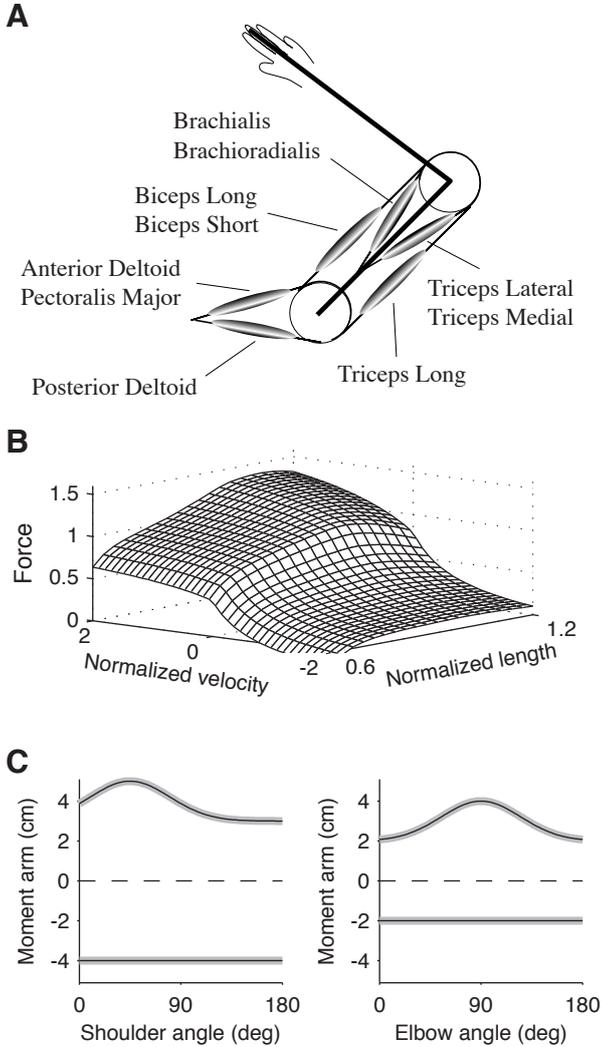


FIGURE 1

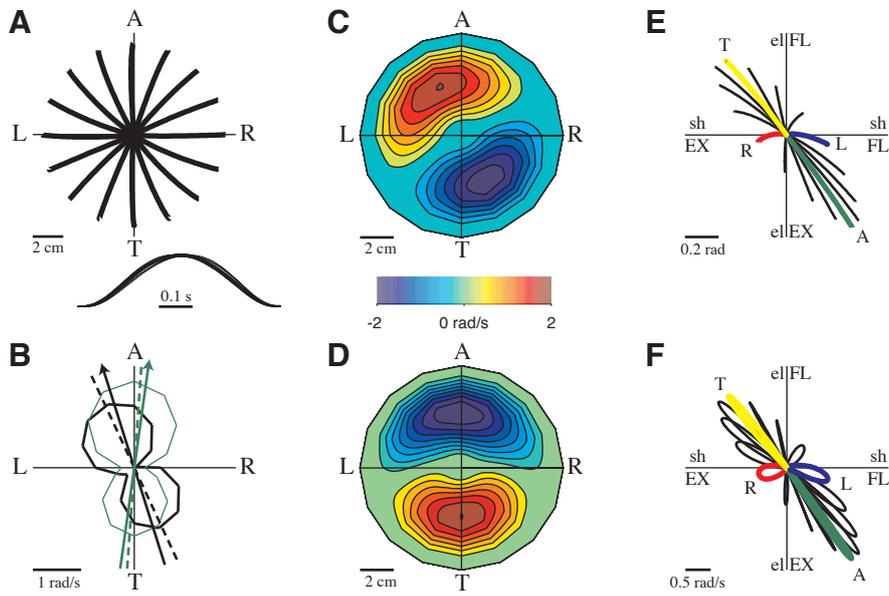


FIGURE 2

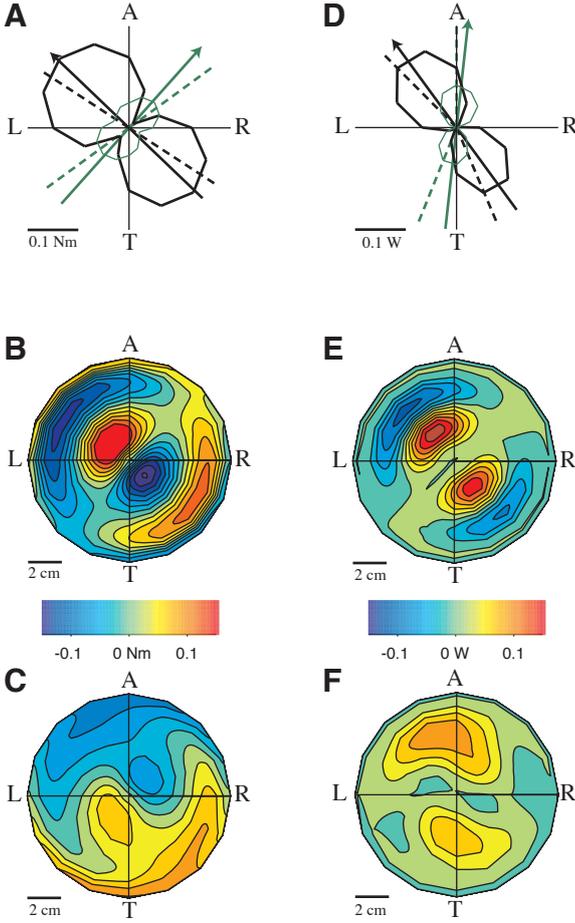


FIGURE 3

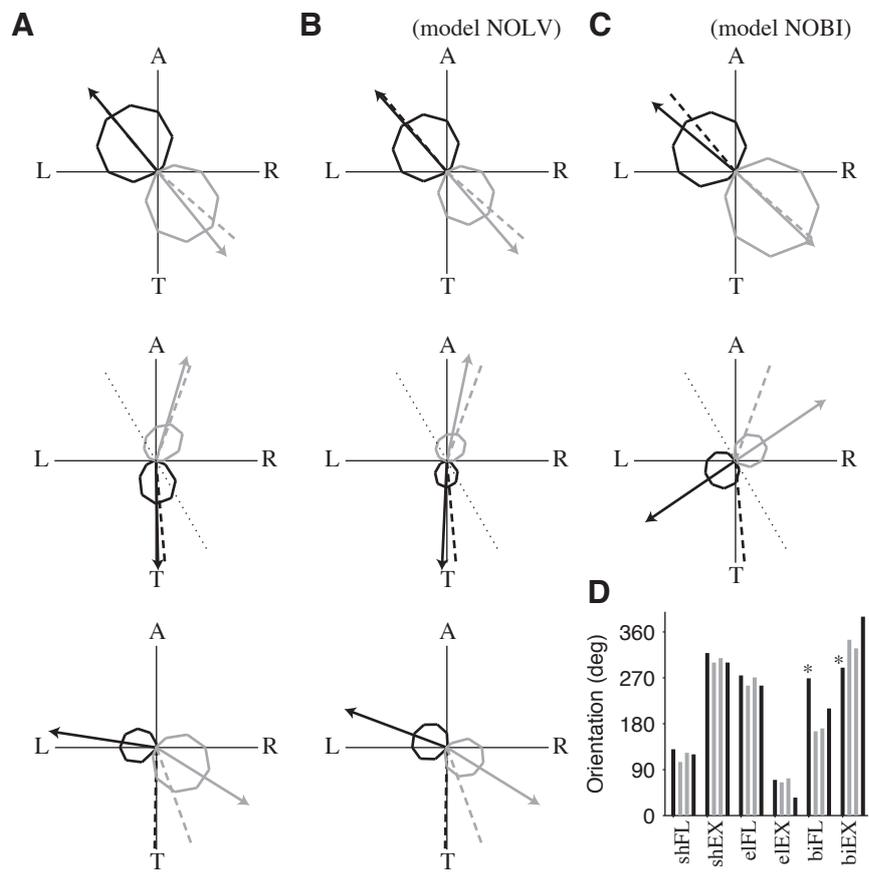


FIGURE 4

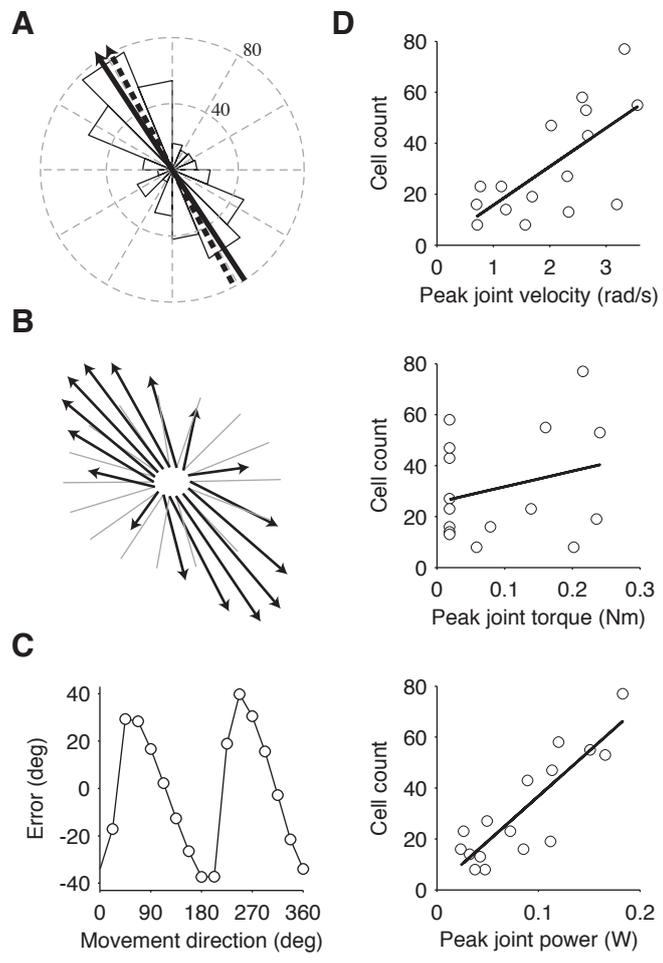


FIGURE 5

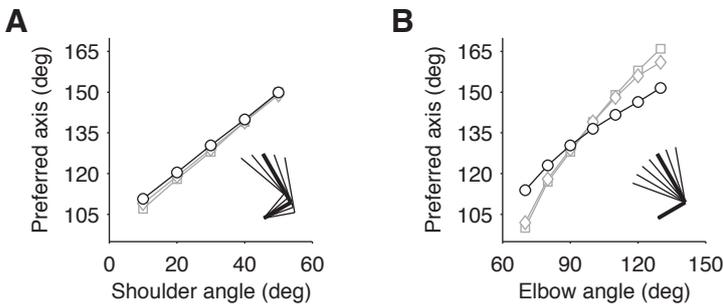


FIGURE 6

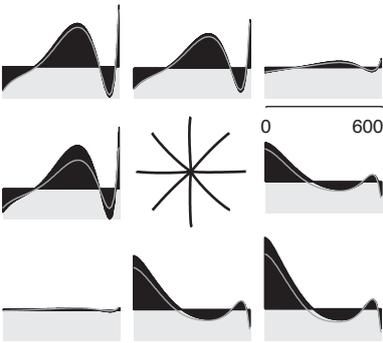


FIGURE 7

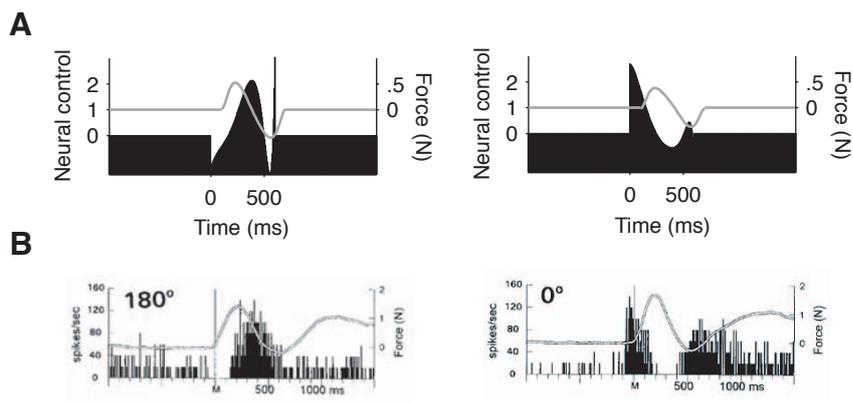


FIGURE 8

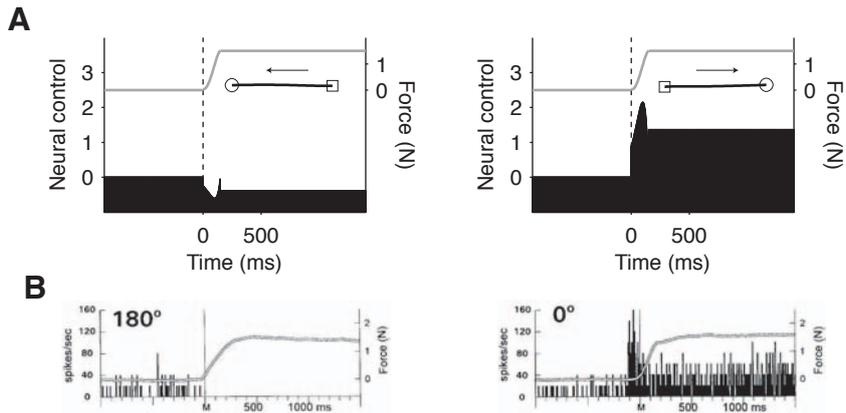


FIGURE 9

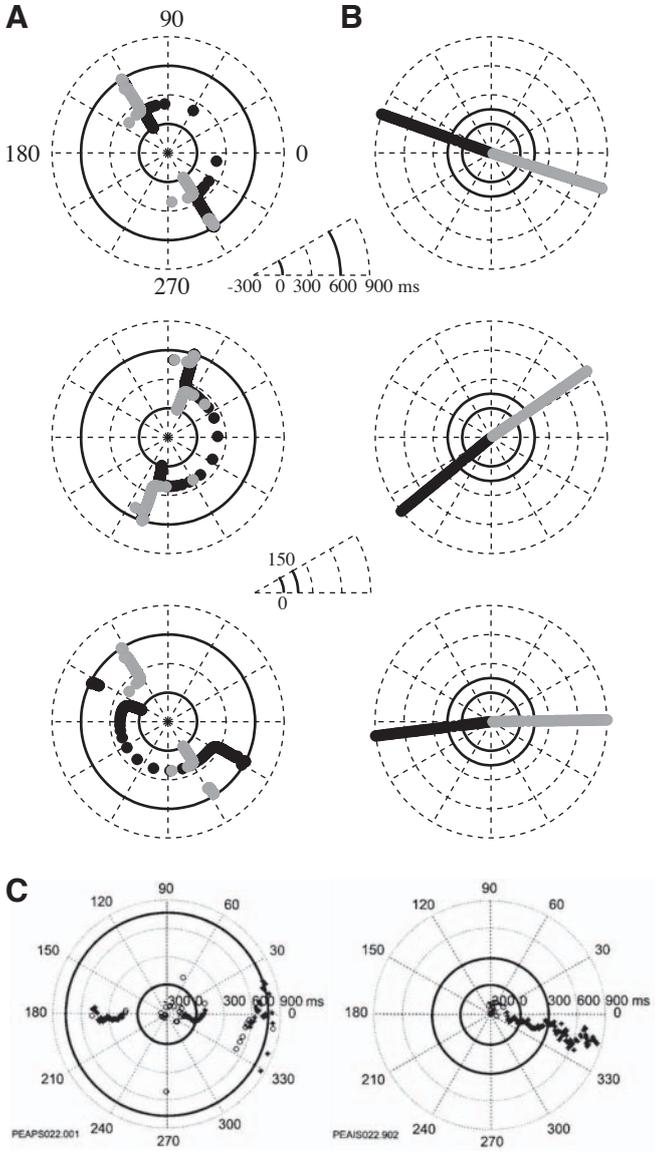


FIGURE 10