Modeling of entorhinal cortex and simulation of epileptic activity: insights into the role of inhibition-related parameters.

Etienne Labyt, Paul Frogerais, Laura Uva, Jean-Jacques Bellanger, Fabrice Wendling

To cite this version:


HAL Id: inserm-00183634
http://www.hal.inserm.fr/inserm-00183634
Submitted on 30 Oct 2007
Modeling of entorhinal cortex and simulation of epileptic activity: insights into the role of inhibition related parameters

E Labyt, P Frogerais, L Uva⁺, JJ Bellanger, F Wendling

Laboratoire Traitement du Signal et de L'Image, Inserm U642, Rennes University 1, 35042 Rennes, France

⁺: Department Experimental Neurophysiology, Istituto Nazionale Neurologico, via Celoria 11, 20133 Milan, Italy

Key words: Computational model, neuronal population, parameter identification, epilepsy, entorhinal cortex, experimental model

Corresponding author:
Doctor Fabrice Wendling
Laboratoire de Traitement du Signal et de l’Image (LTSI)
INSERM U642 - Campus Beaulieu
Université de Rennes 1
35042 Rennes cedex
phone: +33 3 23 23 65 30; fax: +33 3 23 23 69 17
e-mail: fabrice.wendling@univ-rennes1.fr
Abstract

This paper describes a macroscopic neurophysiologically-relevant model of the entorhinal cortex (EC), a brain structure largely involved in human mesio-temporal lobe epilepsy. This model is intervalidated in the experimental framework of ictogenesis animal model (isolated guinea-pig brain perfused with bicuculline). Using sensitivity and stability analysis, an investigation of model parameters related to GABA neurotransmission (recognized to be involved in epileptic activity generation) was performed. Based on spectral and statistical features, simulated signals generated from the model for multiple GABAergic inhibition related parameter values were classified into eight classes of activity. Simulated activities showed striking agreement (in terms of realism) with typical epileptic activities identified in field potential recordings performed in the experimental model. From this combined computational/experimental approach, hypotheses are suggested about the role of the different types of GABAergic neurotransmission in the generation of epileptic activities in EC.
I. Introduction

In mesio-temporal lobe epilepsy (MTLE), a subtype of temporal lobe epilepsy (TLE) [1], stereo-electroencephalographic (SEEG, intracerebral depth electrodes) recordings in intractable patients showed that seizures may originate from the entorhinal cortex (EC) [2]. More recently, this brain structure has been shown to play an important role in the interictal/ictal transition in MTLE [1, 3].

Several evidences arguing that EC is largely involved in MTLE have also been obtained from field potential recordings in experimental animal models [4-7]. These animal models are particularly adapted to investigate the role of the EC in epileptic activity generation because this structure belongs to the “paleocortex”, a well conserved part of the cortex during the species evolution. So, it can be assumed that the intrinsic organization of EC is very similar between animal species and humans and consequently, studies from epilepsy acquired animal models can be very informative about human epilepsy pathophysiology.

SEEG signals and field potentials can be considered as macroscopic recordings. Both reflect overall dynamics rising from interconnected populations of principal neurons and interneurons. Actually, an important issue consists in relating these macroscopic recordings to circuit and synaptic transmission mechanisms (type of post-synaptic receptors involved, kinetics of postsynaptic responses, efficacy of synaptic transmission) underlying epileptic activities. This issue can be addressed using a computational modeling approach based on cytoarchitectonic and neurobiological knowledge about the anatomical structure under analysis. In the present study, we describe a realistic model of the EC which offers the possibility to investigate the simulated field potential activity as a function of the temporal dynamics of its postsynaptic components. Bifurcation and stability analysis of the model are then used to generate hypotheses about synaptic mechanisms involved in the transition from normal to epileptic activity in an in vivo model (guinea-pig isolated brain preparation).
II. Background and objectives

The purpose of this study is to interpret epileptic activities (interictal and ictal) recorded from the EC in an animal model: the isolated guinea-pig brain perfused with bicuculline [8, 9] through realistic modeling of field potential activity. The model is based on EC cytoarchitectonic and neurobiological data reported in literature and summarized in appendix. In this work, we focused on the analysis of GABAergic synaptic interactions between principal cells and interneurons populations included in the model. Indeed, an important role in generation of epileptic activities (interictal and ictal) has recently been attributed to GABA-mediated neurotransmission. This hypothesis is issued from several studies investigating epileptic activities recorded from hippocampus in experimental models [10-12] and in epileptic patients [11, 13, 14]. Additional evidences have also been obtained from different modeling approaches validated with combined real recordings. Using the modeling (at cellular level) of a neuronal network, Traub et al showed that GABAa receptor-mediated inhibition was crucial for shaping gamma oscillations [15]. In another study [16], a physiologically-relevant macroscopic model of hippocampus permitted to reveal that fast onset ictal activity was explained by the impairment of dendritic GABA\textsubscript{a} receptor-mediated inhibition with slow kinetics. Based on experimental animal recordings, a role of GABAergic inputs from interneurons has also been suggested in production of epileptic activities within the EC [5, 17, 18].

Consequently, we specifically studied GABAergic synaptic interaction related parameters in the model. We performed both sensitivity and stability analysis in order to identify model parameter evolutions which explain observed transitions of dynamics in real signals (for example, from interictal spikes to fast activity at seizure onset and from fast onset to ictal burst activity).
III. Computational model

A. Level of modeling

A macroscopic modeling approach (neuronal population level) was chosen because this level allows simulation of signals that can be directly compared to real signals (field potentials reflect overall dynamics rising from interconnected populations of principal neurons and interneurons). Theoretical description of the approach is described in [19] and its first use for electrophysiological data interpretation were reported by Freeman [20] and Lopes Da Silva [21, 22]. More recently, this class of models was exploited in various neurophysiological or clinical studies [23, 24] [16, 25] [26].

This macroscopic approach differs from Traub’s [15] which uses a large number (up to more than one thousand) of neurons and interneurons (each one represented by a complex multi compartmental model) for each subpopulation. Indeed, in macroscopic models, populations of cells composed by different subpopulations (typically principal cells and interneurons) which interact via synaptic connections are considered. In other words, each subpopulation may be seen as a unique ‘lumped-parameter neuron model’ while a population model is obtained from interconnection of these neuron models. The complexity of the corresponding mathematical model is hence dramatically decreased.

Each lumped-parameter model includes inputs (either inhibitory or excitatory) interpreted as average firing rates of action potentials (averaged on both time and space). Inputs are simply defined by a lowpass linear filters whose output represent the average postsynaptic potential and whose time constant can be specifically adapted to the kinetics of receptors present in the postsynaptic membrane. The output of the model is interpreted as a mean frequency of action potentials fired at the soma. It is obtained from the weighted summation of postsynaptic potentials fed into a static nonlinear operator which accounts for threshold and saturation effects.
B. Entorhinal cortex computational model

Based on available data about the cellular and network organization of the EC (see appendix, figure 1 and table 1), we introduced i) NP specific subpopulations of neurons (pyramidal cells, stellate cells) and interneurons which are encountered in deep and superficial layers of this brain structure and ii) a set of intra-layer and inter-layer interaction links between these NP subpopulations (Figure 1 A).

Regarding synaptic interactions in this network, we distinguished excitatory postsynaptic activities (glutamatergic) from inhibitory postsynaptic activities (GABAergic or glycineic). GABAergic transmission is itself mediated by GABAa (with slow and fast kinetics) and GABAb receptors.

In the model, the dynamics of the set of the NP interconnected subpopulations correspond to the state trajectory of a system of NP interconnected differential equation subsystems (one subsystem per subpopulation). Each subsystem equation corresponds to a multiple input/one output system (as represented in figure 1 B for subpopulation number \( p \)) and that can be described by equation (1). For the subpopulations influenced by noise, the term \( n_p \) in (1) is a random input (positive mean gaussian white noise) which models non specific afferences on principal cells only (i.e. pyramidal - \( P_1 \), \( P_2 \) - and stellate - \( St \) – subpopulations). Otherwise, if no 'external noise' acts on the subpopulation, a zero value must be substituted for variable \( n_p \) in (1):

\[
\frac{d}{dt} y_p(t) = f_p^{\theta_p} [\{y_p(t), \omega_k(t), k \in I_p \}, n_p(t)], y(t) \in R^{2|\omega|}, t \in R^+, p = 1..NP \\
(1)
\]

\[
f_p^{\theta_p} : R^{2|\omega|} \times |\theta|^{-1} \rightarrow R^{2|\omega|} \\
(2)
\]
where \( p \) denotes the considered subpopulation index, \( y_p \) denotes the state vector of this subpopulation, \( \{o_k(t), k \in I_p\} \) is the list of outputs from afferent subpopulations and \( |I_p| \) (cardinal of \( I_p \)) is the number of afferent subpopulations.

As illustrated in figure 1-B, for given subpopulation number \( p \), the relationship between presynaptic afferent input(s) \( \{o_k\} \) and \( n_p \) or \( \{o_k\} \) only and population firing output \( (o_p) \) can be defined as in equation (3) and (4):

\[
o_p(t) = S^{\mu_p}(x_p(t)) \quad (3)
\]

\[
x_p(t) = \sum_{k \in I_p} C_k^p (o_k * h_k^p)(t) + (n_p * h_{np})(t) \quad (4)
\]

where \( C_k^p \) accounts for the average number of synaptic contacts from population \( k \) to population \( p \), \( x_p(t) \) represents the input potential at the soma which is a summation (symbol * denotes the convolution product) of linearly filtered versions of afferent inputs \( o_k(t) \) and of the input noise \( n_p \) (if present). Filters are themselves defined by their respective impulse responses detailed in equations (5) and (6):

\[
h_k^p(t) = M_k^p \frac{t}{\tau_k^p} \exp(-t/\tau_k^p) \text{ if } t \geq 0, = 0 \text{ otherwise } , k \in I_p \quad (5)
\]

\[
h_{np}(t) = M_{np}^p \frac{t}{\tau_{np}} \exp(-t/\tau_{np}) \text{ if } t \geq 0, = 0 \text{ otherwise } . \quad (6)
\]

where \( M_k^p \) is a positive (excitatory input) or negative (inhibitory input) constant equal to the product of maximal value of \( h_k^p(t) \) and of the neperian logarithm basis \( e \) (the larger \( M_k^p \), the more efficient the synaptic link \( k \to p \) ) and \( \tau_k^p \) is a time constant (the larger \( \tau_k^p \), the smoother the input) which accounts for the rise and decay time of postsynaptic potentials, in accordance with receptor kinetics and propagation delays along dendritic trees.
The function $S^{\mu_p}$ defined by equation (7) and which appear in the right part of figure 1 B,

$$S^{\mu_p}(x) = \frac{2e_0^p}{1 + \exp(r^p(v_0^p - x))} \in [0.e_0^p, x \in R, \mu_p = (r^p, e_0^p, v_0^p)$$  (7)

is a sigmoid function (nonlinear positive increasing function) which models nonlinear threshold (minimum pre-somatic mean potential level for action potential firing) and saturation (maximal firing rate) effects as constants $2e_0^p$, $v_0^p$ and $r^p$ respectively define the maximum firing rate, the post-synaptic potential corresponding to a firing rate equal to $e_0^p$ and $r^p$ the steepness of the sigmoid.

The link between convolution kernels $h_k^p$ or $h_{n_k}^p$ in (5) and (6) and differential equation systems (1) is given by the equivalence between on one hand $z_{k,1}^p(t) = (h_k^p * o_k)(t)$ and $z_{n_k}^p(t) = (h_{n_k}^p * n_p)(t)$ and on other hand the order two differential equation systems:

$$\begin{cases}
\frac{d}{dt} z_{k,1}^p(t) = z_{k,2}^p(t) , \quad \frac{d}{dt} z_{k,2}^p(t) = -\frac{2}{\tau_k^p} z_{k,2}^p(t) - \frac{1}{(\tau_k^p)^2} z_{k,1}^p(t) + \frac{M_k^p}{\tau_k^p} o_k(t) \\
\frac{d}{dt} z_{n,1}^p(t) = z_{n,2}^p(t) , \quad \frac{d}{dt} z_{n,2}^p(t) = -\frac{2}{\tau_{n_p}^p} z_{n,2}^p(t) - \frac{1}{(\tau_{n_p}^p)^2} z_{n,1}^p(t) + \frac{M_{n_p}^p}{\tau_{n_p}^p} n_p(t)
\end{cases}$$  (8)

where the pair of 'local' states variables $\{z_{k,1}^p(t), z_{k,2}^p(t) = \frac{d}{dt} z_{k,1}^p(t)\}$, $k \in I_p$ and $\{z_{n,1}^p(t), z_{n,2}^p(t) = \frac{d}{dt} z_{n,1}^p(t)\}$ (if noise present) are introduced and pooled to form the subpopulation state vector $y_p$:

$$y_p^T = [z_{k,1}^p, z_{k,2}^p, \ldots, z_{k,1}^{p_1}, z_{k,2}^{p_1}, 0, 0]$$  (10)

$$y_p^T = [z_{n,1}^p, z_{n,2}^p, \ldots, z_{n,1}^{p_1}, z_{n,2}^{p_1}, z_{n,1}^{p_2}, z_{n,2}^{p_2}]$$  (11)

Here, the last two components $z_{n,1}^p, z_{n,2}^p$ in (11) denote the two state variables associated with the convolution kernel $h_{n_k}^p$, similarly as in (8) but with $n_p$ in place of $o_k$. These 2 components are taken into account only if input noise is present, i.e. only for index $p$. 
corresponding to subpopulations P1, P2 and St. Otherwise, they are set to zero as in equation (10).

The conjoint activity of all subpopulations is represented by the time evolution of the global state vector \( \underline{y} = [y^1_p, ..., y^p_n'] \) in \( \mathbb{R}^{\text{dim}(y)} \) with \( \text{dim}(y) = \sum_{p=1}^{N_p} \text{dim}(y^p) \).

Parameters set \( \theta^p \) in \( f^\theta_p \) is \( \theta^p = \{\mu_p, ((M^p_k, C^p_k, \tau^p_k), k \in I_p) \} \); \( \{M^p_n, \tau^p_n \} \) (if noise present) or \( \theta^p = \{\mu_p, ((M^p_k, C^p_k, \tau^p_k), k \in I_p) \} \) (if noise not present)

Finally the overall system of equations may be written as:

\[
\frac{d}{dt} \underline{y}(t) = f^\theta[\underline{y}(t), \underline{n}(t)], \underline{y}(t) \in \mathbb{R}^{\text{dim}(y)}, t \in \mathbb{R}^+, \underline{y}(0) = \underline{y}_0
\]

(12)

where \( \underline{y}_0 \) denotes the initial state vector value and where the global vector parameter \( \theta \) is the concatenation of the \( \theta^p, p = 1, ..., N_p \).

C. Stochastic nature of the model

In this time-continuous model (12), the input vector \( \underline{n}(t) \) is a positive mean Gaussian noise vector that pools the noise inputs \( n_p(t) \) and that models non specific affereces from surrounding neuronal groups whose individual influences are not ‘organized’, i.e. not synchronous. Consequently, the model is governed by a set of stochastic nonlinear ordinary differential equations. However, if \( \underline{n}(t) \) is substituted by the statistical mean of the input \( M_n \) in (3), we obtain a deterministic system of nonlinear ordinary differential equations:

\[
\frac{d}{dt} \underline{y}(t) = f^\theta[\underline{y}(t), M_n], \underline{y}(t) \in \mathbb{R}^{\text{dim}(y)}, t \in \mathbb{R}^+, \underline{y}(0) = \underline{y}_0
\]

(13)

which can be studied for stability (see results section).

D. Model output

In order to explore real data recorded with a field electrode, we must establish a correspondence between the electrode signals, say \( X(t) \), and vector \( \underline{y}(t) \) in (13). The
classical approach is to use the approximation \( X(t) \approx h^T \tilde{y}(t), h \in R^{\dim(y)} \) where the non null components of column parameter vector \( h \) are such that \( h^T \tilde{y}(t) \) is equal to a weighted sum of functions \( x_p(t) \) (postsynaptic potentials) in which index \( p \) corresponds to pyramidal cell subpopulations [27]. This choice is relevant because spatial alignment of pyramidal neurons (‘in palissades’) implies that vector summation of dendritic current dipoles corresponds to the summation of their modules in this case.

**E. Model parameters**

As mentioned in section II (Background and objectives), we only focus on GABAergic interactions. Consequently, variations of maximal postsynaptic potential parameters \( M_k^p \) will be considered only when index \( k \) corresponds to GABAergic neurotransmission (\( I_1, I_2 \) or \( I_3 \)). Standard values of \( I_1, I_2, I_3, I_4 \) (glycine mediated neurotransmission) and \( E \) (glutamate mediated neurotransmission) as well as corresponding time constants \( \tau_k^p \) are given in table 2.

For each subpopulation with non specific afferences, \( \tau_{n_p}^p \) will be set to \( \tau_e \) value given in table 2.

Furthermore, for two connections \( (k \rightarrow p) \) and \( (k' \rightarrow p') \) on target subpopulations \( p \) and \( p' \), we impose \( M_k^p = M_k^{p'} \) if \( k \) and \( k' \) correspond to the same type of neurotransmission.

The other parameters in \( \theta \) remain fixed. Regarding connectivity parameters \( C_k^p \), values are given in table 3. The value of \( \mu_p = (r_p^n, e_0^n, v_0^n) \) is independent of \( p \) and is equal to \((0.56 \text{ mV}^{-1}, 2.5 \text{ s}^{-1}, 6 \text{ mV})\). Finally in the sequel we will denote \( \theta_0 = (I_1, I_2, I_3) \) the triplet of free parameters.
IV. Model parameter identification

Model parameter identification (or parameter estimation) is a difficult problem. It can be approached by elaborating a mapping procedure $T$ which associates an observed sampled signal $X(t), t \in \{0, \Delta, \ldots, (N-1)\Delta\} = X$ an estimated value $\hat{\theta}_0 = T(X)$ for unknown parameter $\theta_0$ with an estimation error criterion (like a mean square error, for example) that is expected as low as possible.

In order to build $T$, we introduced a K-dimensional feature vector $X \rightarrow \hat{F} = G(X) \in R^K$ and we defined $T$ by minimization of a square error norm: $\hat{\theta}_0 = T(X) = \arg \min_{\theta} \| \hat{F} - F(\theta) \|^2$

where $F(\theta) = E_{\theta}^{\theta_0}(\hat{F})$ ($\theta_0$-dependant mathematical expectation of $\hat{F}$, so $\hat{F}$ is an unbiased estimator for $F$). The interesting aspect of this method is that the choice for $\hat{F}$ is open. The drawback is that computation of $F(\theta)$ calculus is generally intractable.

To overcome this difficulty, a possibility is to evaluate $\theta \rightarrow F(\theta)$ by means of simulated observations $X^\theta_S(n)$ (where index $S$ refers to 'Simulation' and where $n$ is the random input noise vector in the model). For sufficient signal duration (number of samples) the evaluation $G(X^\theta_S(n))$ can then be put in place of $F(\theta)$ in $\| \hat{F} - F(\theta) \|^2$ to search $\hat{\theta}$ optimal value by mean of an optimization algorithm, under the assumptions that $\hat{F}$ is informative about the true value $\theta^*$ of $\theta$ (i.e. $\hat{F}$ must not be too different from $G(\theta)$) and that $\left| \frac{\partial}{\partial \theta} G(\theta^*) \right|$ is sufficiently large.

A. Activity maps

Assuming the two above conditions, we used a feature vector $\hat{F}$ and the error function $\| \hat{F} - G(X^\theta_S(n)) \|^2$ to uncover, from simulations, disjoint regions in the space of free
parameters \((\theta_0 \in R^3)\), each region being associated to a particular type of model activity.

Then, activities reflected in real signals as well as transitions between activities are interpreted as possible paths connecting corresponding regions in the space of free parameters. As this space is of dimension 3, paths are displayed on the \((I_1, I_2)\) plane, for different values of \(I_3\). In the results section, \((I_1, I_2)\) planes are referred to as ‘activity maps’.

**B. Classification procedure**

Activity maps are obtained from a supervised classification procedure. This procedure starts from a partitioning of the domain of possible values of \(\theta_0\) in \(N_C\) classes \(\{C_1, ..., C_{NC}\}\) defined from the similarity between simulated and real activity (one class per activity). This partitioning provides a set \(\{\tilde{F}_1, ..., \tilde{F}_{NC}\}\) (\(\tilde{F}_i \in R^3\)) of reference values in the feature space.

Then, for a large set \((\theta_{0k}, \eta_k)\), \(k = 1, ..., N\) \((N\) depending on the discretization of \(\theta_0\)) such that \(\theta_{0k}, k = 1, ..., N\) constitutes a ‘sufficiently dense’ exploration of the \(\theta_0\) space and where \(\eta_k, k = 1, ..., N\) are independent realizations of the input noise in the model, the procedure affects \(\theta_{0k}\) to class \(C_j\) if and only if the square distance

\[
d^2(\tilde{F}_i, G(\mathbf{X}_S^{\theta_i}(\eta_i))) = \lVert \tilde{F}_j - G(\mathbf{X}_S^{\theta_i}(\eta_i)) \rVert^2, i = 1, ..., NC,\]

is minimum for \(j = i\).

This approach was motivated by two considerations: 1) in experiments, visual inspection of real signals reveals a limited number of types of activity and 2) in a large amount of simulations with different values of \(\theta_k\), simulated signals displayed only a small number (equal to 8) of types of dynamics.

**C. Determination of reference centers \(\{\tilde{F}_1, ..., \tilde{F}_{NC}\}\)**

NC reference values \(\theta_{01}^*, ..., \theta_{0NC}^*\) for which characteristic dynamics are obtained, when \(X(t)\) is simulated, are first retained. Let \(\{\mathbf{X}_S^{\theta_{0r}}(\eta_r), r \in J_k\}, k = 1, ..., N_C\) be \(N_C\) sets of independently simulated signals (eq. 4) where, for each \(k\), \(\theta_{0r}, r \in J_k\) are randomly selected in a sphere of
radius $R$ centered on $\theta^*_{0k}$. Then, for each class $C_k$, feature reference $\tilde{F}_k$ is chosen to be equal to the arithmetic mean of the $T(X_{SR}^{(r)}, n_r), r \in J_k$.

**D. Definition of feature vector** $\hat{F} = (\hat{F}_1, \hat{F}_2, \hat{F}_3, \hat{F}_4, \hat{F}_5, \hat{F}_6)^T$

Both morphological and spectral signal characteristics were used in the definition of feature vector $\hat{F}$. The former are essentially based on the amplitude distribution of signals which was assumed to be discriminant as it varies from one type of activity to another (figure 2, last column). The first three features were obtained from partitioning of the amplitudes of signals normalized by the maximum of their modulus. Number of bins and thresholds were optimized in terms of separation between different classes of activity. This procedure led to define three amplitude intervals, $[-0.6, -0.05]$, $[-0.05, 0.05]$ and $[0.05, 0.6]$. Features $\hat{F}_1$, $\hat{F}_2$, and $\hat{F}_3$ correspond to the percentage of samples whose amplitude value are included in the above intervals, respectively.

Let $\underline{X} = X_0, \ldots, X_{N-1}$ be $N$ samples taken in the observed or simulated signal, and let $\underline{Xr} = Xr_0, \ldots, Xr_{N-1}$ be the “rescaled” signal where: $Xr_k = \frac{X_k}{\max_{0 \leq k \leq N-1} \{X_k\}} \in (-1,1)$

We introduce $\hat{F}_1 = FR(\underline{Xr}, -0.6, -0.05)$, $\hat{F}_2 = FR(\underline{Xr}, -0.05, 0.05)$ and $\hat{F}_3 = FR(\underline{Xr}, 0.05, 0.6)$

where $FR(Y, \alpha, \beta) = \frac{1}{N} \text{card} \{ Y_k / \alpha < Y_k \leq \beta \}, \ 0 < \alpha < \beta < 1$, for any real sequence $Y = Y_0 \ldots Y_{N-1}$.

The last three features were defined to characterize the frequency content of signals and more particularly, their power into specific frequency sub-bands. As for amplitude features, tests were performed to determine the number of frequency sub-bands and boundaries. Best results were obtained for 3 sub-bands, $[3, 12]$, $[13, 17]$ and $[18, 50]$ Hz. Features $\hat{F}_4$, $\hat{F}_5$, and $\hat{F}_6$...
correspond to the signal power in the above intervals obtained from computation of the power spectral density (PSD, figure 2, middle column) using the averaged periodogram method.

Let us consider $\overline{P_{ER}}(X, f), f \in \{0,1,...,255\}$ as the block averaged periodogram obtained with 256 points FFT and 50% overlap between adjacent blocks (which is an estimator of the PSD).

We then define, for $0 \leq f_1 < f_2 \leq 127$, the normalized band power on $\{f_1, ..., f_2\}$ as

$$NBP(f_1, f_2) = \left( \sum_{f_1 \leq f \leq f_2} \overline{P_{ER}}(X, f) \right) / \left( \sum_{0 \leq f \leq 127} \overline{P_{ER}}(X, f) \right)$$

and the last three features as

$$\hat{F}_4 = NBP(3,12) \quad \hat{F}_5 = NBP(13,17) \quad \text{and} \quad \hat{F}_6 = NBP(18,50).$$

Finally the feature vector is defined as $\hat{F} = (\hat{F}_1, \hat{F}_2, \hat{F}_3, \hat{F}_4, \hat{F}_5, \hat{F}_6)^T$.

V. Experimental data

Experimental data were obtained from brains of Hartley guinea pigs (150-200g, Charles River, Calco, Italy) isolated and maintained in vitro by perfusion with a cold (4-10°C) oxygenated (95%) complex saline solution according to the standard procedure described elsewhere [28-30]. Experiments were performed at 32°C after gradually raising the temperature with 0.2°C/min steps. Extracellular recordings were performed in deep layers of the EC with 16-channels silicon probes (100 µm contact separation, provided by Jamille Hetcke, CNCT, University of Michigan, Ann Arbour, MI) inserted perpendicularly to EC lamination under direct visual control with a stereoscopic microscope. Focal epileptiform discharges in the limbic region were induced by 3-5 minutes arterial applications of the GABA$_a$ receptor antagonist, bicuculline (50 µM; SIGMA) diluted in the perfusion solution [9].

The viability of the isolated brains was tested by recording the responses evoked in the limbic cortices by stimulating the lateral olfactory tract [31-33]. At the end of the electrophysiological experiments, in order to verify the position of the electrodes, an...
electrolytic lesion were made by passing a 30 µA current for 30 seconds between the two deepest contacts of the silicon probe. Further, this lesion was localized on 75-100µm thick coronal sections obtained from the isolated brain under exploration. The experimental protocol was reviewed and approved by the Committee on Animal Care and Use and by Ethics Committee of the Istituto Nazionale Neurologico.

From recordings performed in 10 isolated brains, eight classes of activities (numbered from 1 to 8) have been identified (Figure 3). Corresponding signals simulated by the model are displayed. It can be noticed that they closely resemble real field potentials. Class 1 refers to normal background activity as observed in real recordings before bicuculline perfusion. After injection of bicuculline, infrequent spikes (class 2) appear, and become rhythmic (class 3) before seizure begins. Class 4 corresponds to fast activity usually observed at the onset of seizure. Classes 5 and 6 respectively refer to frequent bursts (class 5) and infrequent (or sporadic) bursts activities which are classically observed during the seizure time-course. Finally, two other types of epileptic activities have been identified: spikes mixed to fast activity (class 7) which can be observed just before the seizure onset and polyspikes (class 8) encountered during ictal period.

VI. Results

Activity maps obtained for different values of $I_3$ (GABA<sub>b</sub> inhibition) are shown in figure 4. These activity maps represent the distribution of the eight classes of activity (detailed above) in the two-dimensional parameter plane $I_1/I_2$ (GABA<sub>a</sub> slow/GABA<sub>a</sub> fast inhibitions). From visual inspection of these maps, we can notice that for high values of $I_3$, the model produces almost only background activity. Epileptic activities start to appear when $I_3$ decreases. All classes of epileptic activities are exclusively produced if $I_3$ is set below a threshold value (6.5 mV). Below this $I_3$ threshold value and considering low values of $I_1$, fast
onset activity, frequent and infrequent bursts are produced for high values of $I_2$ while the different spiking activities (spikes mixed to fast activity, polyspikes, spikes frequent and infrequent) are observed for low values of $I_2$. Beyond the $I_3$ threshold value, fast onset activity disappears while the amount of polyspikes activity increases. Finally, it can be noticed that the amount of frequent spikes as well as frequent burst activities decrease in favor of infrequent spikes and infrequent burst activities when $I_2$ rises. In other words, the frequency of spikes (for low values of $I_2$) and of burst (for high values of $I_2$) is controlled by the $I_3$ value in the model.

Activity maps can also be considered as a representation of bifurcations in the model, corresponding to transitions from one class of activity to another one. However, there are no bifurcations in the model for the transition from infrequent spikes or bursts to frequent spikes or bursts. Indeed, in these cases, the same activity is produced by the model and only the frequency of these activities is different.

We also performed a preliminary study of model stability (eq. 4) by analyzing noise independent properties. The model was recognized as experimentally stable if, for some random initial conditions, the state vector converged to a same fixed point in the absence of input noise fluctuations (standard deviation equal to zero). A more formal study of fixed points is beyond the scope of this paper. Results from stability study provided the limit values in the two-dimensional parameters plane $I_1/I_2$ separating the stable from the unstable parameter regions in the model. This limit (solid line) was superimposed on each activity map. As interestingly observed in figure 4, the unstable zone globally corresponds to values of $I_1/I_2$ parameters for which epileptic activities are produced by the model. The stable zone increases with parameter $I_3$ value.
The knowledge of activity maps generated from the model may be used to interpret temporal dynamics and transitions observed in real field potentials recorded from EC during the transition to seizure in the experimental animal model.

A first example corresponding to the seizure pattern which is encountered in most cases (named as typical) is given in figure 5. Eight steps ($S_1$-$S_8$) are distinguished according the pseudo-stationary nature of the activity reflected by the signal (Figure 5-A): normal background activity ($S_1$), infrequent spikes ($S_2$), more frequent spikes ($S_3$), rhythmic spikes ($S_4$), spikes mixed to fast activity ($S_5$), fast onset activity ($S_6$), frequent bursts ($S_7$) and finally, infrequent bursts ($S_8$). The observed transitions from background to infrequent spikes activity and then, between periods of epileptic activities can be represented on the activity maps as possible paths connecting corresponding regions of activity and which provide to a time-evolution for model parameters $I_1$, $I_2$ and $I_3$. All these paths are oriented from high to low values along the $I_1$ axis, denoting a reduction of GABA$_{\text{slow}}$ inhibition and in a next step, from low to higher values along the $I_2$ axis and along the “virtual” $I_3$ axis, interpreted as an increase of GABA$_{\text{fast}}$ and GABA$_{\text{b}}$ inhibitions.

In order to simulate time-series signals (figure 5-B) which temporal dynamics reproduce those observed in the real field potentials (figure 5-A), we chose one possible path drawn on activity maps shown in figure 5-C. Following this path, starting from standard $I_1/I_2$ values for which a background activity (step $S_1$) is simulated by the model, five successive decreases in $I_1$ value leads the model to generate realistic infrequent spikes ($S_2$) and then, frequency of spikes increases ($S_3$) until rhythmic spikes appears ($S_4$). Next, these rhythmic spikes mix to fast activity ($S_5$) until the emergence of fast activity ($S_6$) corresponding to the seizure onset. Afterwards, frequent burst activity is observed when $I_2$ and $I_3$ values increase ($S_7$). Finally, a
second increase in $I_3$ values leads to a slowing down of burst activity ($S_8$) before the seizure ends.

An interesting feature of the procedure is its capacity to also interpret another seizure pattern less frequently encountered in real recordings and characterized by a lack of rhythmic spikes and fast onset activity when seizure begins (figure 6-A). Using the same procedure, we defined two possible paths characterized by 6 steps ($S_1$-$S_6$) on the activity maps (Figure 6-C and 6-D). Starting from the same standard $I_1/I_2$ values ($S_1$) than in the precedent example, the first path (figure 6-C) leads to hypothesize that $I_1$ value (GABA$_a$ slow inhibition) decreases more abruptly and in a lesser extent ($S_1$ to $S_4$). So, three successive decreases in $I_1$ value result in the appearance of spikes ($S_2$) whose frequency increases ($S_3$) before the emergence of spikes mixed to fast activity ($S_4$). But the $I_1$ value does not sufficiently decrease such that fast activity at seizure onset is observed. Afterwards, as observed in the precedent seizure pattern, frequent burst activity ($S_5$) is generated when $I_2$ and $I_3$ values increase and finally, the burst activity slows down ($S_6$) consecutively to a further increase of parameter $I_3$ value. The second possible path (figure 6-D) leads to the hypothesis that the $I_3$ value (GABA$_b$ inhibition) might be higher in this experiment and remains constant. For this higher $I_3$ value, no fast onset activity is produced by the model. In this case, the three successive decreases in $I_1$ values ($S_1$ to $S_4$) lead the model to generate infrequent spikes ($S_2$), more frequent spikes ($S_3$) and then spikes mixed to fast activity ($S_4$). Appearance of the frequent burst activity is explained in the model by an increase in $I_2$ value and then, a re-increase in $I_1$ value results in the production of an infrequent burst activity before seizure termination. From these inhibition profiles, time-series signals shown in figure 6-B are produced by the model. As in the previous example, it can be noticed that this simulated signal is very realistic compared to the real field potential recording.
VII. Discussion and conclusion

In this study, we proposed a macroscopic computational model which produces vectorial signals corresponding to normal background activity and also to different types of epileptiform activities which are very realistic compared to real signals (extracellular field potentials) recorded from EC in the isolated guinea-pig brain during seizures induced by bicuculline perfusion. The macroscopic modeling level (based on a lumped parameter approach) chosen for this study seems to be particularly suited to the nature of experimental recordings and human intracerebral recordings (i.e. SEEG). Indeed, the model output corresponds to a reflection of ensemble dynamics rising from macroscopic statistical interactions between interconnected neuronal sub-populations (pyramidal cells and interneurons) and therefore, it can be interpreted as extracellular field potentials recorded in animal models or in intractable patients under pre-surgery exploration.

A crucial step in the modeling is to determine parameters values and to validate modeling results. In this study, this step was achieved in interaction with real recordings from experimental guinea-pig model. Because it is very difficult to determine parameters values only from available experimental data, the parameters identification was addressed in this work using a systematic variation procedure of parameters values around standard values. This procedure was coupled to an automatic classification method of simulated signals based on their spectral and statistical features. Here, it needs to notice that this procedure has only been applied to model parameters related to the three types of GABAergic inhibition present in the model, based on convergent evidences that GABAergic synaptic interactions play an important role in generation of epileptic activities [5, 17, 18]. Amplitude of other average post-synaptic potentials (excitatory and Glycine-mediated inhibitory) as well as connectivity values were kept constant. In spite of these restrictions, our classification method resulted in very homogeneous classes of activities as it can be observed on activity maps. This last result
increases model’s confidence as it suggests that there are not several possible parameters sets to generate one given type of activity identified from real recordings. Moreover, from these parameters sets, very realistic signals could be simulated. As exemplified with the two different seizure patterns, they provided a physiologically relevant interpretation of transitions between the different types of activity, either from the background activity to the period preceding the seizure onset (where spikes appears and increase in frequency) or during the seizure time-course itself. In terms of stability, this work also showed that instability in the model (globally corresponding to epileptic activities) was caused by introducing both a decrease of $\text{GABA}_a$ and $\text{GABA}_b$ receptor-mediated inhibitions. Beyond the validation of modeling results from real recordings, the model can also be used to generate testable hypothesis about possible mechanisms underlying the transition from background to epileptic activities. From this study, the role of $\text{GABA}_b$-mediated inhibition in the epileptic activities generation, in the decrease of burst frequency or in the process of seizure termination should be experimentally tested.

The model can also be considered as a valuable tool to advance in the understanding of pathophysiological mechanisms of human epilepsy. Indeed, the computational model integrates several types of knowledge: neurobiological (cellular organization, connections…), pharmacological (types of receptors, types of neurotransmitters, bicuculline effect) and physiological (role in generation of epileptic activities). As presented in this study, using modeling results, it has been possible to interpret field potentials in terms of synaptic interactions for different types of GABA receptors and therefore, to put forward hypothesis about the role of these types of GABA inhibitions in the generation of epileptic activities. For example, in the model, fast onset activity seems to be produced only if $I_2$ parameter value ($\text{GABA}_a$ fast receptor-mediated inhibition) is sufficiently high. The model acts as a bridge between the macroscopic observations (extracellular field potentials) and fine mechanisms at
synaptic level. Thus, this model could offer a good way to progress in the role of EC and mechanisms present within this brain structure involved in human MTLE. Another perspective is to use such models to represent the temporal dynamics of epileptic activity sources located in limbic structures. Indeed, electrical or magnetic potentials observed on electrodes positioned at the surface of the head can be computed, given some information about the spatial distribution of these sources and given a volume conductor model (forward problem). Such an approach could contribute to better interpretation of spatio-temporal dynamics reflected in MEG [34] or EEG [35] signals recorded in temporal lobe epilepsy.

**Appendix: Cellular organization of entorhinal cortex**

According with anatomo-functional description reported in previous works [36, 37], “superficial layers” (superficial to lamina dissecans (layer IV)) and “deep layers” (between lamina dissecans and the white matter) are represented in a superficial EC model and a deep EC model. The global EC model corresponds to superficial EC model interconnected to deep one (figure 1). In the sequel, we describe the cytology and network connectivity of the EC.

**A. Principal excitatory neurons**

Principal excitatory neurons in the entorhinal cortex consist in pyramidal cells localized in superficial layers (mainly in layer III) and deep layer (mainly layer V) and stellate cells localized in superficial layers (mainly layer II) [37-43]. Pyramidal neurons in deep layers project to pyramidal and stellate neurons in superficial layers [44], [45, 46]. In turn, they receive afferent inputs from pyramidal neurons in superficial layers [43].

**B. Interneurons**

The EC model includes two classes of interneurons: inhibitory and excitatory [47, 48]. Based on pharmacological studies, it has been shown that inhibitory interneurons project to four types of post-synaptic receptors: glycine receptors [49] [50]; GABA<sub>b</sub> receptors [51, 52];
and two kinetically distinct subtypes of GABA$_a$ receptors (fast and slow) [53] identified from recording of spontaneous inhibitory synaptic currents in EC interneurons (layers II and V). According with this assumption, spatially segregated synapses (axo-somatic and axo-dendritic) from inhibitory interneurons to pyramidal and stellate cells have been identified [43, 47, 54]. Taken together, these observations suggest that there are dendritic and somatic inhibition in the EC and according to previous works, dendritic inhibition would involve mainly GABA$_a$ slow receptors while somatic inhibition would involve mainly GABA$_a$ fast ones [55, 56].

All interneurons (inhibitory and excitatory) receive afferents excitatory inputs from stellate (only in superficial layers) and pyramidal cells [36, 53, 57]. An additional excitatory afferent input to GABAergic interneurons comes from excitatory interneurons [36, 53, 57]. In turn, excitatory interneurons receive inhibitory feedback from GABA interneurons via GABA$_a$ (slow and fast) receptors [36, 47, 48]. Moreover, glycinergic interneurons receive an inhibitory feedback from GABAergic interneurons via GABA$_a$ slow receptors [50].

C. Extra-entorhinal inputs

Pyramidal (in superficial and deep layers) and stellate cells receive an extrinsic excitatory input from subiculum, pre- and para-subiculum [58] as well as from CA1 [59-62], a subfield of hippocampus. Another extra-entorhinal input comes from neocortex and olfactory cortex [36] as well as subcortical structures [36, 63].

D. Entorhinal outputs

The main output pathway of EC originates from stellate cells and deep pyramidal neurons which give rise to the perforant route, projecting to dentate gyrus and CA3/CA2 hippocampal fields [43, 45, 46, 64]. The second EC output consists in the temporo-ammonic pathway from pyramidal neurons in superficial layers (mainly layer III) which send their axons predominantly to hippocampal field CA1 and the subiculum [36, 65, 66].
Acknowledgement

Experimental recordings were kindly provided by M de Curtis from the Istituto di Neurologica Carlo Besta – Milano. This study was funded by the French Foundation for Epilepsy Research (FFRE).
References


**Legends:**

Table 1: Table of input subpopulation indexes as used for equations writing. Each source subpopulation (P1, P2: pyramidal cells. St: stellate cells. Exc: excitatory. Inh: inhibitory. IN: interneurons) has been conventionally numbered from 1 to 12 and the different types of neurotransmission (I: inhibitory and E: excitatory) are denoted in the first colon, line 3 to line 7 with the corresponding neurotransmitter in brackets. The connectivity oriented graph represented on figure 1-A is encoded in the table cells: an empty cell for no afference, else the list of existing afferences. The last line indicates noise input applied to P1, P2 and St subpopulations.

Table 2: Amplitude of average post-synaptic potentials (initial values for which normal background activity is simulated) and time constants used in the model

Table 3: Local connectivity constants in EC model

Figure 1: (A) Cellular organization (P1, P2: pyramidal cells. St: stellate cells. Exc: excitatory. Inh: inhibitory. IN: interneurons) of the EC established from literature review about cytoarchitectonic and neurobiological data. This was used as the starting point in the EC model design. From generic input/output diagram (B) representing all inputs and the output for any neuronal population and mathematical conversions (transfer functions, sigmoid function), a particularized diagram for the pyramidal subpopulation in deep layers (P2) is given as example (C).
Figure 2: The different types of activity produced by the model and comparison with real field potentials recorded from EC in isolated guinea-pig brain. In figure 4, each type of activity is coded by the color indicated in corresponding box.

Figure 3: For each type of activity, spectral (frequency bands: 3-12 Hz; 13-17 Hz; 18-30 Hz) and statistical (number of points in interval -60/-5 %; -5/5 %; 5/60 %) features included in the features vector used to perform the classification are represented.

Figure 4: Activity maps obtained for model exploration with respect to I₁ (GABA_a slow receptor-mediated inhibition) and I₂ (GABA_a fast receptor-mediated inhibition) parameters corresponding to the synaptic gains in feedback loops from inhibitory interneurons to pyramidal cells in deep layers of EC. Limit values (illustrated by a solid line) in the two-dimensional parameters plane I₁/I₂ separating the stable from the unstable parameter regions in the model (based on stability study) is superimposed on each activity map. Stable (respectively unstable) region appears on the right (respectively left) side of the line. For two maps (I₃=6.5 and I₃=8), closed contours were observed inside which stability was found.

Figure 5: (A) Typical seizure pattern recorded from EC in the isolated guinea-pig brain perfused with bicuculline. Eight phases can be distinguished in this pattern (see details in text). (B) Corresponding simulated signals generated by the model for each phases from synaptic gains profiles defined by the path drawn on activity maps. (C) One possible path on activity maps explaining the transitions of activity observed in the real field potential recording (A).
Figure 6: (A) another seizure pattern characterized by the lack of rhythmic spikes and fast activity at the seizure onset. In this pattern, six phases can be distinguished (see details in text). (B) Corresponding simulated signals produced in the model for each phases from synaptic gains profiles defined by the path drawn on activity maps (see (C)). One possible path on activity maps (C) explaining the transitions of epileptic activity observed in the real field potential recording (A) assuming that $\text{GABA}_a$ receptor-mediated inhibition decreases less abruptly and in a lesser extent. Another possible path on one activity map (D) explaining the transitions observed from background activity to the seizure activities in real recordings (A) with hypothesis that $\text{GABA}_b$ receptor-mediated inhibition is strong.
Figure 3
Figure 4
Figure 6
Table 1:

<table>
<thead>
<tr>
<th>Layers</th>
<th>DEEP</th>
<th>SUPERFICIAL</th>
</tr>
</thead>
<tbody>
<tr>
<td>Neuronal population type</td>
<td>1 2 3 4 5</td>
<td>6 7 8 9 10 11 12</td>
</tr>
<tr>
<td>Neurotransmission type</td>
<td>P2 Exc IN Inh IN Inh IN</td>
<td>P1 St Exc IN Inh IN Inh IN Inh IN Inh IN</td>
</tr>
<tr>
<td>I1 (GABAₐ,slow)</td>
<td>4 4</td>
<td>11 11 11 11</td>
</tr>
<tr>
<td>I2 (GABAₐ,fast)</td>
<td>5 5</td>
<td>10 10 10</td>
</tr>
<tr>
<td>I3 (GABAₐ)</td>
<td>3</td>
<td>12 12</td>
</tr>
<tr>
<td>I4 (Glycine)</td>
<td></td>
<td>9 9</td>
</tr>
<tr>
<td>E (Glutamate)</td>
<td>1, 6 1 1 1, 2 1, 2</td>
<td>1, 6 1, 7 6, 7 6, 7 6, 7, 8 6, 7, 8</td>
</tr>
<tr>
<td>N</td>
<td>n2</td>
<td>n1 n3</td>
</tr>
</tbody>
</table>
Table 2:

<table>
<thead>
<tr>
<th></th>
<th>DEEP</th>
<th>SUPERFICIAL</th>
<th>Time constants (ms)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Average amplitude</strong></td>
<td><strong>Average amplitude</strong></td>
<td><strong>Time constants</strong></td>
<td></td>
</tr>
<tr>
<td>(mV)</td>
<td>(mV)</td>
<td>(ms)</td>
<td></td>
</tr>
<tr>
<td><strong>Excitatory PSP</strong></td>
<td>$E = 6$</td>
<td>$E = 3$</td>
<td>$\tau_e = 10$</td>
</tr>
<tr>
<td>(Glutamate)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Inhibitory PSP</strong></td>
<td>$I_1 = 25$</td>
<td>$I_1 = 25$</td>
<td>$\tau_1 = 30$</td>
</tr>
<tr>
<td>(GABA$_a$, slow)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Inhibitory PSP</strong></td>
<td>$I_2 = 40$</td>
<td>$I_2 = 40$</td>
<td>$\tau_2 = 4$</td>
</tr>
<tr>
<td>(GABA$_a$, fast)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Inhibitory PSP</strong></td>
<td>$I_3 = 5$</td>
<td>$I_3 = 5$</td>
<td>$\tau_3 = 300$</td>
</tr>
<tr>
<td>(GABA$_b$)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Inhibitory PSP</strong></td>
<td><em>Not present</em></td>
<td>$I_4 = 40$</td>
<td>$\tau_4 = 27$</td>
</tr>
<tr>
<td>(Glycine)</td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>
Table 3:

<table>
<thead>
<tr>
<th></th>
<th>P</th>
<th>P₁</th>
<th>P₂</th>
<th>St</th>
<th>IN exc</th>
<th>IN GABA_a,s</th>
<th>IN GABA_a,f</th>
<th>IN GABA_b</th>
<th>IN Gly</th>
</tr>
</thead>
<tbody>
<tr>
<td>P₁</td>
<td>160</td>
<td>4</td>
<td>4</td>
<td>50</td>
<td>50</td>
<td>50</td>
<td>50</td>
<td>50</td>
<td>30</td>
</tr>
<tr>
<td>P₂</td>
<td>3</td>
<td>160</td>
<td>-</td>
<td>50</td>
<td>50</td>
<td>50</td>
<td>50</td>
<td>50</td>
<td>-</td>
</tr>
<tr>
<td>St</td>
<td>-</td>
<td>-</td>
<td>160</td>
<td>50</td>
<td>50</td>
<td>50</td>
<td>50</td>
<td>50</td>
<td>50</td>
</tr>
<tr>
<td>IN exc</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>20</td>
<td>20</td>
<td>20</td>
<td>20</td>
<td>-</td>
</tr>
<tr>
<td>IN GABA_a,s</td>
<td>35</td>
<td>35</td>
<td>35</td>
<td>20</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>10</td>
</tr>
<tr>
<td>IN GABA_a,f</td>
<td>25</td>
<td>25</td>
<td>25</td>
<td>20</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>IN GABA_b</td>
<td>15</td>
<td>15</td>
<td>15</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>IN Gly</td>
<td>-</td>
<td>35</td>
<td>35</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
</tbody>
</table>