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Spatio-temporal Registration of 2D US and 3D MR images for the Characterization of Hypertrophic Cardiomyopathy

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Abstract. A spatio-temporal registration procedure of speckle-tracking echocardiography (STE) and cine magnetic resonance (MR) images is presented. It aims to fuse the mechanical information in STE with the tissue information in MR late-gadolinium-enhanced image (LGE-MR), in order to describe the relationship between left ventricular myocardial strain and macroscopic fibrosis in patients with hypertrophic cardiomyopathy (HCM). The registration was performed between the four-chambers-view STE contours (at rest), and the endocardial surfaces of the left ventricle (LV) from cine-MR short-axis-view sequence. The dynamic LV geometries were described by their Fourier descriptors. This spatio-temporal representation of LV geometries was exploited to avoid the lack of dissimilarity between static geometries. To accomplish this goal, the temporal alignment was performed with the dynamical time warping method. The registration was evaluated on four HCM patients with myocardial fibrosis. First results suggest a relationship between myocardial fibrosis and the modification of the strain curve.

1 Introduction

Hypertrophic cardiomyopathy (HCM) is a common genetic cardiovascular disease with a worldwide prevalence of 0.2% [7]. HCM is characterized by left ventricle (LV) hypertrophy. It is usually recognized by maximal LV wall thickness ≥ 15 mm based on echocardiography, although cardiovascular magnetic resonance (MR) is now used with increasing frequency [2]. Many studies have now documented that approximately half of patients with HCM have late gadolinium enhancement (LGE) suggestive of areas of fibrosis [8]. Previous studies demonstrated that the extent of LGE was correlated with LV systolic and diastolic dysfunction as well as adverse cardiac events such as sudden cardiac death, fatal arrhythmia or worsening heart failure in patients with HCM [1]. Myocardial strain is a sensitive parameter of ventricular systolic function [3]. Two-dimensional speckle-tracking echocardiography (STE) had shown to provide an angle-independent, rapid and accurate method for strain measurement [6]. Some

previous studies reported that regional myocardial strain and wall thickening were affected by regional myocardial fibrosis in patients with HCM [9]. The description of the relationship between myocardial strain and the macroscopic fibrosis in myocardial tissue can lead to a better understanding of the strain curve. It would allow a low cost and precise characterization of this tissue and an improvement in diagnostic. Then, the fusion of speckle tracking echocardiography and the LGE magnetic resonance (LGE-MR) sequences should be considered to establish and describe the aforementioned relationship.

The static registration of the LV surface from LGE-MR image (routinely acquired at mid-diastole) with its corresponding STE contour is difficult because of the lack of dissimilarity in LV geometry (i.e. LV smoothness and symmetry). In fact, a dynamic registration approach (2D+t / 3D+t) leads to a better registration [11]. Although some iconic registration approaches as been reported [5], a surface-based approach was selected here given the available STE data. In this approach, different methods could be used to describe shape information like in [12]. The representation of LV contours by their Fourier descriptors (FDs) was selected because the comparison of surfaces issued from different modalities becomes straightforward. Therefore, we use the FDs of both STE contours and corresponding contours extracted from 3D+t LV surfaces on MR short-axis-view (MR-SAX), to perform their registration. The temporal alignment is computed with the dynamical time warping (DTW) method [10]. DTW alignment allows to compare the two dynamic Fourier representations.

This paper presents a 2D+t to 3D+t surface-based registration method aiming to fuse mechanical (strain) and tissue information from STE and inversion recovery (IR-MR) sequence, respectively. It is organized as follows: the methods are presented in Section 2 for (i) the representation of US and MR-SAX contours, (ii) their Fourier decomposition, (iii) the DTW alignment and metric computation, and (iv) the optimization of the similarity metric. Finally, the results obtained on four HCM patients are presented and discussed in Section 3 to then derive a conclusion and present some perspectives.

2 Methods

The general scheme of the registration method is shown in Fig. 1. It aims to find the position of the US-plane in the MR-SAX space. For this purpose, a set of parameters (ν), defining the position of the US-plane, is optimized. This plane cuts the LV dynamic surface (\mathbf{S}) obtained from MR-SAX images. It also locates the input STE contours (\mathcal{U}) in MR-SAX space. \mathcal{U} and \mathbf{S} are registered performing a spatio-temporal alignment that includes the dynamical information (i.e., LV deformation). This is achieved as follows: first, a plane $P(\nu)$ is defined to extract a set of LV contours from \mathbf{S} . Next, the Fourier decomposition of both \mathcal{U} and the extracted contours are computed. Then, a spatio-temporal similarity metric between the two Fourier decompositions is calculated using the temporal alignment (p') obtained with the DTW method. These steps are iterated by a gradient descent procedure that changes the parameters ν of the US-plane until this metric is minimized.

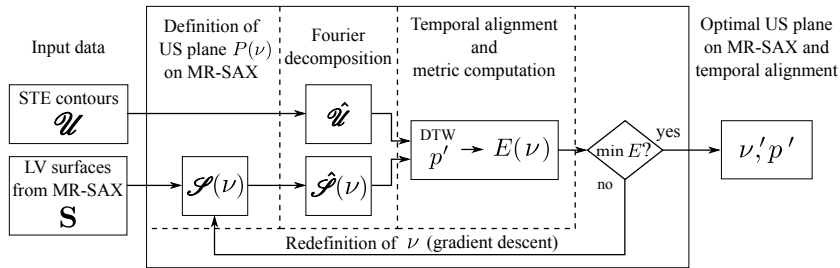


Fig. 1. General scheme of the registration method.

2.1 Representation of Input Data

Two sequences are aligned by the registration method: the STE contour sequence \mathcal{U} , and the MR-SAX surface sequence \mathbf{S} . Let $\mathcal{U}_m \in \mathcal{U}$ be the STE contour at the cardiac phase m ($m \in \{0, \dots, M-1\}$). \mathcal{U}_m is a set of $L_{\mathcal{U}}$ ordered points e.g., clockwise. Similarly, let $S_n \in \mathbf{S}$ be the LV surface from MR-SAX image at the cardiac phase n ($n \in \{0, \dots, N-1\}$). The LV contour $\mathcal{S}_n(\nu)$ is then extracted from the surface S_n using the plane $P(\nu)$, with ν the plane parameters. Since US and MR acquisitions are ECG-gated, $m = n = 0$ are the peak of the R-wave in STE and MR-SAX ECGs, respectively.

2.2 Fourier Decomposition of a 2D Contour

Each contour $\mathcal{U}_m \in \mathcal{U}$ and $\mathcal{S}_n(\nu) \in \mathcal{S}(\nu)$ is decomposed into its Fourier descriptors $\hat{\mathcal{U}}_m \in \hat{\mathcal{U}}$ and $\hat{\mathcal{S}}_n(\nu) \in \hat{\mathcal{S}}(\nu)$, respectively. Thus, the discrete Fourier transform (DFT) is computed for the sequence of complex numbers that encodes the localization of each vertex in \mathcal{U}_m and $\mathcal{S}_n(\nu)$. These descriptors can be made invariant to translation, scale and/or rotation. Given that the deformation of the LV contours throughout the cardiac cycle contains important information, the translation and rotation invariances seem to be useful to compare these contours that belong to different spatio-temporal coordinate systems.

2.3 Temporal Alignment and Metric Computation

We propose the use of the DTW method to perform the temporal alignment [10]. DTW is depicted in Fig. 2. It is advantageous because the temporal interpolation of the two dynamic contours is not needed. However, both sequences must share the same synchronization. In our case, the latter corresponds to the synchronization using the peak of the R-wave on ECGs. The use of the DTW method is convenient given the non-linear relationship between the ECG and a given variation of the RR-interval [4]. Despite the fact that temporal alignment can be performed using the ECGs that gated the acquisitions [5], ECG from MR acquisition is not always available.

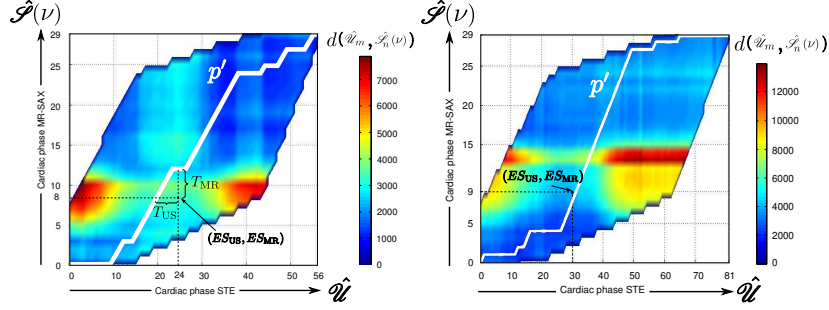


Fig. 2. DTW alignment between STE FDs sequence ($\hat{\mathcal{U}}$) and LV FDs sequence from MR-SAX ($\hat{\mathcal{S}}(\nu)$) using 60 FDs, for patient 1 (left) and patient 2 (right) (optimal path p' is the solid white line). The color indicates the distance between a pair $\hat{\mathcal{U}}_m$ and $\hat{\mathcal{S}}_n(\nu)$. T_{US} and T_{MR} are the distances from p' to the end-systole point (ES_{US}, ES_{MR}), along $\hat{\mathcal{U}}$ and $\hat{\mathcal{S}}(\nu)$ axes, respectively. They are used to evaluate temporal alignment.

The DTW method is performed on a matrix whose entries are the distances between each pair $\hat{\mathcal{U}}_m, \hat{\mathcal{S}}_n(\nu)$ (Eq. (1)). Let $p = \{c_0, \dots, c_i, \dots, c_I\}$ with $c_i = (m_i, n_i)$ be a warping time function. c_i is a tuple indicating a temporal correspondence between $\hat{\mathcal{U}}_{m_i}$ and $\hat{\mathcal{S}}_{n_i}(\nu)$ such that $m_i \in \{0, \dots, M-1\}$ and $n_i \in \{0, \dots, N-1\}$. It is well known that FDs of higher order account for fine contour details that, in our case, are more likely due to noise or sharp changes in the surface given the rough thickness of MR-SAX slices. Therefore, the number of descriptors of both $\hat{\mathcal{U}}_{m_i}$ and $\hat{\mathcal{S}}_{n_i}(\nu)$ were limited to L . In addition, the incidence of low order descriptors was emphasized defining a weighted distance:

$$d(\hat{\mathcal{U}}_{m_i}, \hat{\mathcal{S}}_{n_i}(\nu)) = \sum_{k=0}^{L-1} \frac{1}{k+1} \left| \hat{\mathcal{U}}_{m_i k} - \hat{\mathcal{S}}_{n_i k}(\nu) \right|, \text{ with } (m_i, n_i) \in p, \quad (1)$$

where $\hat{\mathcal{U}}_{m_i k}$ and $\hat{\mathcal{S}}_{n_i k}(\nu)$ are the k -th FD of the m_i -th STE contour and of the n_i -th LV MR-SAX contour, respectively. The DTW method aligns $\hat{\mathcal{U}}$ and $\hat{\mathcal{S}}(\nu)$ in time searching a p that minimizes the accumulated distance between $\hat{\mathcal{U}}$ and $\hat{\mathcal{S}}(\nu)$ along it:

$$p' = DTW(\hat{\mathcal{U}}, \hat{\mathcal{S}}(\nu)) = \underset{p}{\operatorname{argmin}} \sum_{i=1}^I d(\hat{\mathcal{U}}_{m_i}, \hat{\mathcal{S}}_{n_i}(\nu)), \text{ with } (m_i, n_i) \in p, \quad (2)$$

p' was computed using dynamical programming. In addition, the search of p' was constrained using a mask. Fig. 2 shows the optimal paths p' obtained at the last iteration of the registration process for two patients. The color codes the distance between a pair of Fourier decompositions (Eq. (1)). Finally, the spatio-temporal similarity metric between $\hat{\mathcal{U}}$ and $\hat{\mathcal{S}}(\nu)$ was defined as:

$$E(\nu) = \sum_{i=1}^I d(\hat{\mathcal{U}}_{m'_i}, \hat{\mathcal{S}}_{n'_i}(\nu)), \text{ with } (m'_i, n'_i) \in p', \quad (3)$$

2.4 Optimization of US-plane parameters

An optimal US-plane ($P(\nu')$) is extracted at the end of the optimization process. $P(\nu)$ is defined by the parameters $\nu = [\mathcal{O}, \vec{n}]$ with $\mathcal{O} = [x_{\mathcal{O}}, y_{\mathcal{O}}, z_{\mathcal{O}}]$ its origin and $\vec{n} = [x_{\vec{n}}, y_{\vec{n}}, z_{\vec{n}}]$ its normal vector. Thus, the parameters that minimize $E(\nu)$ are:

$$\nu' = \underset{\nu}{\operatorname{argmin}} E(\nu), \quad (4)$$

This leads to a rigid registration with an underlying non-rigid temporal alignment (p' in Eq. (3)). Eq. (4) was minimized using a constrained gradient descent procedure initialized by the spatial centroids of \mathcal{U} and $\mathcal{S}(\nu)$, the long axis of the LV extracted from the direction matrix of MR-SAX image, the apex of LV at $n = 0$ and an estimation of \vec{n} . Note from Fig. 1 that the DTW is computed at each iteration. The gradient descent parameters were constrained as follows: a sphere of 20mm around the apex for the origin, a cone angle of 10° around the long axis (vertex at the apex), a cone angle of 10° around the initial \vec{n} (vertex at the apex), and a ratio of 300:1 for the step size of \mathcal{O} to the step size of \vec{n} .

3 Results and Discussion

The proposed registration process was evaluated on data from four HCM patients. The diagnosis of HCM followed the recent guidelines in [2]. Besides, patients have some degree of fibrosis in LV myocardium assessed from IR-MR.

US four-chambers-view (4CAVX) images were acquired at rest on a GE Vivid 7 station (GE Healthcare, Horten, Norway). The end-systole (ES) phase was determined using the ECG and the closure of the aortic valve. Then, the STE output contours were exported for the RR-interval (using the peak of R-wave). STE contours resolution varies from 50 to 63 points and from 56 to 80 frames.

Cine-MR sequences (SAX, 4CAVX and long-axis-view LAX) of the left ventricle were also acquired (ECG gated, 30 phases, gadolinium enhanced). ES phase was determined on MR-SAX images as well. Besides, jointly IR-MR images were acquired at mid-diastole for the same views. They were used to assess the fibrosis. The resolution for MR-SAX is $256 \times 256 \times 12$ pixels. Voxel spacing is $1.25 \times 1.25 \text{ mm}^2$ for x and y , and from 8 mm to 10.01 mm along z .

Temporal alignment Fig. 2 shows the p' computed from the distance matrix between \mathcal{U} and $\mathcal{S}(\nu)$ at the last iteration of the optimization process. Both, the misalignment of ES_{US} (T_{US}) and the misalignment of ES_{MR} (T_{MR}) were used as performance indicators, with ES indicating the end-systole phase. T_{US} and T_{MR} are shown in Fig. 2(left). These misalignments were normalized as a percentage of their corresponding RR-interval (0% being the best value). Table 1 contains the performance for four values of L (number of FDs), and best per patient are bold. The mean and standard deviation are also included.

It is observed in Table 1 that the number of FDs has an influence on performance. The best alignment was obtained for $L=60$ which is lower than the

Table 1. Evaluation of DTW alignment using $L \in \{30, 50, 60, 80\}$ (Pn°X: a given patient). T_{US} and T_{MR} are the misalignments of ES for US and MR as the percentage of their RR-interval, respectively. The mean values (\bar{T}_{US} , \bar{T}_{MR}) and standard deviations ($\sigma_{T_{US}}$, $\sigma_{T_{MR}}$) for each test are at the right.

| L | P1 | | P2 | | P3 | | P4 | | Mean | | Std. deviation | |
|-----|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------|-----------------------|-----------------------|--------------------------|--------------------------|
| | T_{US} (%) | T_{MR} (%) | T_{US} (%) | T_{MR} (%) | T_{US} (%) | T_{MR} (%) | T_{US} (%) | T_{MR} (%) | \bar{T}_{US} (%) | \bar{T}_{MR} (%) | $\sigma_{T_{US}}$ (%) | $\sigma_{T_{MR}}$ (%) |
| 30 | 12.5 | 16.7 | 11.1 | 26.7 | 5.5 | 10 | 4.3 | 10 | 8.4 | 15.9 | 4.1 | 7.9 |
| 50 | 16.1 | 13.3 | 3.7 | 10 | 0 | 0 | 8.7 | 16.7 | 7.1 | 10 | 7.0 | 7.2 |
| 60 | 10.7 | 13.3 | 0 | 0 | 3.6 | 6.7 | 5.8 | 13.3 | 5.0 | 8.3 | 4.5 | 6.4 |
| 80 | 5.4 | 10 | 7.4 | 20 | 1.8 | 3.3 | 7.2 | 16.7 | 5.5 | 12.5 | 2.6 | 7.4 |

maximum number of points. We took $L=50$ as the second performance because it ranks second for \bar{T}_{MR} . Given that STE contours do not have high frequency geometrical components as MR contours (STE contours are already smooth), then these results show that contour sequences should be compared using their low frequency FDs. However, this does not apply for P1. In that case, MR-SAX images have non negligible movement artifacts that could bias the alignment. Finally, US sequences are better aligned than MR sequences. This suggest that the search of p' should be constrained according to the length of input sequences.

Spatio-temporal alignment Given the lack of gold standard, the alignment of \mathcal{U} and $\mathcal{S}(\nu)$ was rated by one cardiologist at both the peak or R-wave and ES_{US} phases. For this purpose, STE contours (color coded by segment) were superimposed to the reformatted MR-SAX and MR-4CAVX. Fig. 3 exemplifies this on one patient. Each segment was rated as exploitable or non-exploitable (1 or 0). The addition of exploitable segments was used as performance indicator. Output ratings are in Table 2 for $L \in \{50, 60\}$. Best result was obtained for $L=50$.

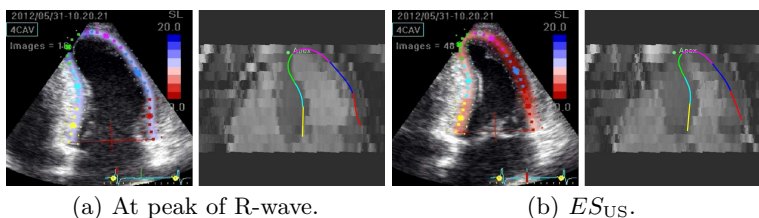


Fig. 3. P2: Images used for qualitative evaluation ($L = 60$). 3(a) images at the peak of R-wave, and 3(b) corresponding images at ES_{US} . Yellow: septal-basal, cyan: septal-mid, green: septal-apical, magenta: lateral-apical, blue: lateral-mid, red: lateral-basal.

Apical segments accounted for all the non-exploitable segments in the spatio-temporal alignment evaluation in Table 2. This can be explained by the low

Table 2. Exploitable segments/total segments after the spatio-temporal registration of the four patients (P1 to P4). The score is the addition by row.

| L | P1 | | P2 | | P3 | | P4 | | Score |
|-----|-----|-----------|-----|-----------|-----|-----------|-----|-----------|--------------|
| | R | ES_{US} | R | ES_{US} | R | ES_{US} | R | ES_{US} | |
| 50 | 5/6 | 6/6 | 6/6 | 6/6 | 4/6 | 4/6 | 5/6 | 6/6 | 42/48 |
| 60 | 5/6 | 6/6 | 5/6 | 6/6 | 4/6 | 4/6 | 5/6 | 6/6 | 41/48 |

quality of apical segment representation in US images. This would also explain that the best performance was obtained for $L = 50$ which is not the best after temporal evaluation. Finally, Fig. 4 contains the superimposition of resulting registration at mid-diastole for IR-MR-4CAVX image and corresponding STE-4CAVX contour for P1 and P2. Longitudinal strains (SL) are also included. Fig. 4 highlights that the change in the magnitude of the regional SL minima could be related with the presense of fibrosis. These first results suggest a relationship between myocardial fibrosis and the modification of the strain curve.

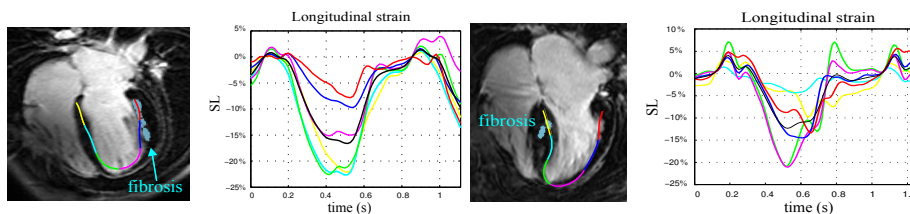


Fig. 4. STE contour superimposed with IR-MR-4CAVX image and SL curves for P1 (left) and P2 (right). Black curve is the global SL. Areas with fibrosis are in cyan.

4 Conclusion

We proposed a method to register US and MR images aiming to fuse mechanical and tissue information from HCM patients. It is based on a dynamic approach which allows to have an improved metric compared to a static approach. Results show that the FD spatio-temporal alignment using the DTW allowed a satisfactory alignment of STE-4CAVX contours and MR-SAX images. Moreover, the results obtained by the proposed method allowed the cardiologist to link the longitudinal regional strain with the tissue characteristics assessed from IR-MR image. In addition, a possible correlation between myocardial fibrosis and the change of the strain curve was observed.

This study will be continued including more HCM patients with and without fibrosis to validate the strain/fibrosis correlation. This would improve the understanding of the strain curve from STE.

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