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Combined passive detection and ultrafast active imaging of cavitation events induced by short pulses of high-intensity ultrasound

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Abstract

The activation of natural gas nuclei to induce larger bubbles is possible using short ultrasonic excitations of high amplitude, and is required for ultrasound cavitation therapies. However, little is known about the distribution of nuclei in tissues. Therefore, the acoustic pressure level necessary to generate bubbles in a targeted zone and their exact location are currently difficult to predict. In order to monitor the initiation of cavitation activity, a novel all-ultrasound technique sensitive to single nucleation events is presented here. It is based on combined passive detection and ultrafast active imaging over a large volume and with the same multi-element probe.

Bubble nucleation was induced with a focused transducer (660kHz, $f\#=1$) driven by a high power (up to 300 W) electric burst of one to two cycles. Detection was performed with a linear array (4–7MHz) aligned with the single-element focal point. *In vitro* experiments in gelatin gel and muscular tissue are presented. The synchronized passive detection enabled radio-frequency data to be recorded, comprising high-frequency coherent wave fronts as signatures of the acoustic emissions linked to the activation of the nuclei. Active change detection images were obtained by subtracting echoes collected in the unucleated medium. These indicated the appearance of stable cavitating regions. Thanks to the ultrafast frame rate, active detection occurred as soon as 330 μ s after the high amplitude excitation and the dynamics of the induced regions were studied individually.

MESH Keywords Algorithms ; Animals ; Gases ; chemistry ; Gelatin ; Microbubbles ; Muscle, Skeletal ; ultrasonography ; Phantoms, Imaging ; Sheep ; Signal Processing, Computer-Assisted ; Transducers ; Ultrasonography ; instrumentation ; methods

Author Keywords single nucleation events ; ultrafast active imaging ; passive detection

Introduction

Gas nuclei have been shown to exist naturally in human and animal tissues [1]. The origin and persistence of these pre-existing nuclei *in vivo* are still somewhat contentious subjects. Several nucleation mechanisms have been proposed to explain the appearance of transient gas bodies in living systems [1]. However, because of their randomness and the rapid dissolution of the potentially induced nuclei, these nucleation mechanisms are usually insufficient to explain the observed bubble formation, particularly during decompression experiments. Therefore, the stabilization of sub-micrometer gas bodies by intracellular crevices on boundary surfaces [2] or by the absorption of surfactant molecules onto their surfaces [3] was suggested, leading to the idea of persistent gas nuclei [1],[4]. However, none of the above mechanisms currently have strong experimental proof *in vivo*. Consequently, gas nuclei available in the living body are highly unknown. One can nevertheless assume that their spatial distribution within the body is heterogeneous because of the variety of structures and molecular contents of living tissues. Moreover, these stabilized gas bodies are most probably smaller than a few micrometers so as not to be trapped by capillaries in normal living conditions. The high rarefaction pressure necessary to induce bubbles using a short ultrasonic excitation [5] tends to prove that they are even smaller (sub-micrometer sized).

The formation of bubbles *in vivo* can actually be caused by the ultrasonic exposure of tissues. The activation of pre-existing nuclei may either be thermally-mediated and then issued from ultrasonic heating, or mechanically-driven resulting from acoustic negative pressure. Firstly, an increase in temperature may promote the growth of nuclei by raising the vapor pressure or the partial pressure of dissolved gas in the medium [6]. Due to viscous absorption, ultrasound induces local tissue heating so that bubble formation can be assisted by this mechanism during long insonifications and especially during ultrasound thermal therapy using high-intensity focused ultrasound (HIFU) [7]. Secondly, during the rarefaction phase of an ultrasonic wave, pre-existing gas nuclei respond as if the pressure was static, due to their very small size. This means that they grow explosively if the rarefaction pressure exceeds a threshold, as described by Blake [8]. This threshold depends on the size of the nuclei and the surface tension of the surrounding liquid, among other factors, and falls with increasing size of the initial gas body. In order to generate bubbles mechanically and to avoid any effects associated with tissue heating, short ultrasound pulses at a low duty cycle were used in the present work.

The mechanism of bubble formation by transient pressure reduction is of great interest for at least two therapeutic applications of ultrasound: cavitation-enhanced heating [9] and histotripsy [5]. Indeed, in order to achieve cavitation-enhanced heating at low acoustic

intensity, prior to any heating, bubbles have to be generated in tissue by activation of the natural nuclei [10]. The induced bubbles are used for their ability to accelerate tissue heating while they undergo driven cavitation activity. On the other hand, this mechanism of bubble generation is precisely the key mechanism of the initiation phase in the histotripsy process [11]. In this application, high-powered ultrasonic bursts of a few cycles are first used to generate a bubble cloud. Just afterwards, subsequent insonifications, possibly less powerful, sustain the cloud so as to efficiently erode and liquefy the tissue. In short, both of these applications first require the efficient generation of bubbles larger than naturally occurring nuclei. Such bubbles are indeed easier to excite ultrasonically and can undergo stable or inertial cavitation.

The transition from sub-micrometer gas nuclei to a bubble size suitable for ultrasonic therapy is usually called "bubble nucleation" and corresponds to the initiation of cavitation activity in the medium. It is only possible when the nucleation threshold pressure is exceeded. Previous studies [12]–[14] have shown that this nucleation threshold can be extremely high (above 10 MPa rarefaction pressure *in vivo*) in the frequency range usually used in medical ultrasound. However, there is also evidence to show that when a bubble is induced and eventually breaks up (either from collapse or shape instability), the medium becomes seeded with additional gas nuclei that may engender new bubbles and possibly create a bubble cloud after some additional excitations. Similarly, single nucleated bubbles could reflect subsequent ultrasonic excitations and may then contribute to the creation of a high rarefaction pressure that favors the appearance of additional bubble nucleation sites [15]. As a result, the nucleation threshold may locally be lower in a tissue where bubbles have already been generated than in the initial untreated medium. The very first induced bubbles are thus of great importance.

Acoustic techniques developed for the *in vivo* detection of generated bubbles generally have a low sensitivity to single bubbles, and they are mostly aimed, in cavitation therapies, at ensuring that a cloud is efficiently generated and that its location and cavitation activity can be determined. Consequently, standard passive cavitation detection with a single-element transducer [16] and standard B-mode imaging [5] have been used to monitor the histotripsy process. When a bubble cloud has been induced, the energy received on the passive detector suddenly increases, and once the bubbles are large or numerous enough to form a region that scatters incident ultrasound more strongly than its surroundings, a hyperechogenic region can be pointed out on the B-mode images. Such hyperechoes may also appear after sonication in ultrasonic-guided HIFU treatments that generate bubbles [17]. For these latter applications, additional passive imaging techniques using ultrasound arrays were recently developed [18]–[20]. Besides all of these acoustic monitoring techniques, high frame rate optical studies investigated the dynamics of cloud formation in its early stages, showing the evolution from one insonification to another [21]–[22], or for the same multi-cycle excitation cycle after cycle [15]. These optical imaging techniques provide valuable information but they require transparent media, and thus can only be used with transparent tissues mimicking phantoms or liquids. These kinds of materials may not reproduce the nucleation conditions of living tissue. Furthermore, the requirement of optical transparency excludes animal tissues, which are optically diffusive, and limits the application for therapy monitoring at an early stage.

In this study, we present a novel all-ultrasound technique based on combined passive and active detection using a conventional ultrasonic array to determine whether or not the nucleation threshold has been locally exceeded in tissue and to study the individual behavior of the first bubbles induced. Because of the very high pressure amplitude necessary to initiate cavitation, high-amplitude focused ultrasound has to be used for the formation of bubbles. The focusing indeed allows the acoustic energy to be spatially concentrated around the focus. However, even if a favored zone for nucleation is created, the precise location of the nucleation events still remains unknown: this depends on both the applied pressure amplitude and the unknown distribution of gas nuclei in tissues. The detection of these events should then occur, at the same time, over a large volume in the vicinity of the focus, and on a local scale within this volume. The localization of spots where cavitation has been initiated would indeed provide information on the spatial heterogeneities of the nucleation threshold. Likewise, the detection should provide information to discriminate between the different nucleation events that may happen for a single insonification. Therefore, a multi-element transducer with an electronic system allowing simultaneous acquisitions over all the elements was advantageously used here as a detector. Such a detector has already been used *in vitro* for passive imaging of inertial cavitation during HIFU thermal treatment [18]–[20], and for passive detection and localization of the nucleation events induced by short pulses [23]. Passively recording the radio-frequency signals emitted during the nucleation process is also of great interest here in order to obtain information on the early nucleation event. However, passive detection techniques cannot provide information on the temporal behavior over time of the first bubbles induced. Therefore, active detection of the bubbles is also of interest, and we propose to combine it with passive detection in this paper. Bubble nucleation from short ultrasonic pulses will often lead to transient bubbles with a maximum life span of the order of a few milliseconds [21]–[22]. In order to obtain information on the evolution of the induced bubbles from their creation, active detection should occur as soon as possible after nucleation – but not at the same time to avoid interactions [24] – and it should be repeated with a high frame rate to rapidly image the bubble dynamics. Moreover, as each short high power insonification supposedly leads to a different nucleation situation, the detection should be done at one time over the entire volume. A stroboscopic or synthetic aperture detection method, such as conventional B-mode imaging, would provide only partial information since at a specific time only a small portion of space is probed. Years ago, our team developed an ultrafast imaging technique [25] that allows such an active detection by using plane-wave transmission at a high frame rate (up to 20,000 frames/s).

In this paper, combined passive and ultrafast active detection of single bubble nucleation events is demonstrated *in vitro* both in gel and in freshly excised sheep's thigh muscle. Both detection signals indicated that cavitation inception occurred. A passive method was shown to be able to detect the acoustic emission that occurs during a nucleation event: non-linear scattering of the high-amplitude excitation by a nucleus cavitating non-inertially, and/or acoustic emission from an inertially collapsing bubble. On the other hand, an active method was shown to detect nucleated bubbles, using their ability to strongly scatter probing insonifications. Active images here could only detect bubbles in the stable cavitation regime, and passive acquisition was able to detect both stable and inertial cavitation. The correlation between the two kinds of detection enabled the nucleation site locations and their number to be confirmed, but each contained some specific complementary information. The life of a bubble from its nucleation until its disappearance or next excitation was recorded experimentally and presented here.

Materials and methods

Confocal set-up

The technique presented here is based on the combination of a focused therapy transducer and a multi-element imaging probe confocally aligned (see Figure 1). The therapy transducer used in this study was a single-element piezo-composite focused transducer (Imasonic, Besançon, France). It had a central frequency of 660 kHz, a focal distance of 45 mm and an f-number equal to one. This single-element transducer was driven by a function generator (AFG 3101, Tektronix, Beaverton, OR, USA) with a 300 Watt RF power amplifier (A-300, Electronics & Innovation, Rochester, NY, USA). In order to take advantage of the power of the amplifier, an electrical impedance matching circuit was used between the amplifier output and the transducer. The whole system allowed us to generate high-amplitude short ultrasonic bursts of a few cycles in the medium on demand.

A linear array (L7-4, 4.0/7.0 MHz Linear Array Vascular, Philips Medical Systems, Seattle, WA, USA) was used to perform ultrasonic imaging. It was made of 128 elements with a 5 MHz central frequency and a 0.3 mm pitch. It was driven by an ultrasound scanner prototype (V1, SuperSonic Imagine, Aix en Provence, France) programmable per channel both in receiving (64 channels) and in transmitting (128 channels) modes. In the receiving mode, acquisitions of radio frequency (RF) signals were simultaneously made on all receiving channels and the collected data were transferred at a 2 GB/s rate to memory. Data treatments, such as the beamforming process, were made post-acquisition. This allowed a very high frame rate acquisition (up to 20,000 frames/s) by the receiving aperture (64 consecutive elements) with a good spatial sampling. For active detection, the transmitting mode enabled a single plane-wave insonification to be emitted along the entire aperture of the ultrasound array (6 MHz, 1 cycle). The backscattered echoes of the emitted plane-wave were collected by the receiving channels. Therefore, using this method, a full image was obtained using a single transmission within the time a single line would only be acquired using conventional imaging [26]. This ultrafast method, initially developed for transient elastography, leads to frame rates that are only limited by the back and forth propagation of the ultrasonic wave, and are typically around 10 kHz depending on the depth. Both active ultrafast frame rate imaging and passive recording were successively achieved using this ultrasound scanner and linear array. Geometry appropriate for *in vivo* extra-corporeal implementation was selected for the alignment of the two transducers: the imaging probe was positioned on the side of the therapy transducer, as can be seen in Figure 1 . Using a custom-built adjustable transducer holder with two rotation axes that could be independently blocked, and a translation axis (Figure 1), the linear array was manually positioned to place the focal point of the therapy transducer within the median image plan. The alignment procedure was performed as follows. First, the whole system was immersed in a degassed water tank and the position of the maximum pressure resulting after a 3-cycle excitation burst of the single element was found using a 400 μ m aperture needle hydrophone (HNA-400, Onda Corporation, Sunnyvale, CA) and a 3-D positioning system (Newport, Irvine, CA, USA). Then, plane-waves were emitted with the array while it was moved relatively to the single element so as to both maximize the signal measured on the hydrophone and to obtain a good B-mode image of the hydrophone tip. Finally, the position was fixed using screws and the location of the focal point in the median image plan was determined using a conventional B-mode sequence to be at $z_F = 47.9 \pm 0.3$ mm away for the array and in front of the 67th element.

Sample preparation

Two different media were tested *in vitro* : gelatin gel and freshly harvested sheep thigh muscle tissues.

Gelatin gel

The gel phantom was prepared using a 5% (w/v) concentration of gelatin powder (Gelatin powder Technical, VWR BDH Prolabo, West Chester, PA, USA). First, the gelatin powder was melted into stirred hot (~ 90 °C) deionized water until a homogeneous and clear gelatin solution was obtained. The hot solution was then gently poured into a plastic container with an ultrasound absorber at the bottom, so as to obtain a 5 cm thick phantom. The solution stood still at room temperature for one hour so that bubbles potentially created while pouring could move upward and be eliminated. The top end was then sealed off with an adapted lid and the whole container was stored in a fridge overnight so that gelation could occur. The next morning, the lid was removed and degassed water was added on the top of the gel to fill up the container. The transducers were immersed and placed almost in contact with the gelatin gel just before testing began.

Animal muscle tissues

Muscle tissues were harvested from the thigh of a sacrificed sheep. Several tissue pieces about 5 cm thick – the other dimensions being in the order of 10 cm – were prepared. First, the fat tissues were removed with a scalpel. Each piece was then placed with a small quantity of physiologic serum in a plastic bag designed to store fresh food. Using an appropriate vacuum sealer (Figuine, FI.VS50), the air was removed from the bag and the bag was sealed. The experiments were performed less than 24 h after the animal's death. The samples were immersed in a tank filled with degassed water and with an ultrasound absorber at the bottom. The integrated transducer system was then placed in contact with the sample and testing began.

Nucleation detection sequence

The nucleation detection sequence was composed of three main blocks: 1) standard B-mode imaging of the medium, 2) synchronized high-amplitude emission and passive detection, and 3) ultrafast active detection. The whole nucleation detection sequence consisted of these three blocks, followed in succession. First of all, before any bubble nucleation, standard B-mode images were acquired with the linear array and displayed in real time. They allowed the focal zone of the therapy transducer to be positioned within the different structures of the medium. Once the position was chosen, the actual detection sequence (Figure 3) was launched. First, an ultrafast active detection was made so as to provide a reference acquisition of the backscattered echoes from the un-nucleated medium (Figure 3 , first block on the time line, before $t=0$). Then, a synchronized passive detection was performed: a trigger pulse was sent by the ultrasound scanner to the function generator, synchronizing the time lines of the transducers' driving systems ($t=0$) and resulting in both the emission of a high power short burst with the therapy transducer and passive recording with the multi-element transducer (Figure 3 , first white block just after $t=0$). Immediately after this event, a new ultrafast active detection was performed in the potential nucleated medium. The pattern of passive plus active detections (succession of blocks 2 and 3) was then repeated multiple times, and the raw RF data corresponding to each detection acquisition were stored in the internal memory. These data were all collected at the end of the sequence, and signal processing was performed using Matlab (Mathworks, Natick, MA, USA).

The reason for these multiple and successive high-amplitude excitations of the medium following the detection sequences is that nucleation is a random process which might only occur after a great number of short high-amplitude excitations [16]. The pulse repetition frequency (PRF) of high power excitation has an influence on cloud initiation for histotripsy [27], and may thus influence the nucleation conditions and the dynamics of the nucleated bubbles. The upper boundary of the PRF was linked here to the maximum ultrasound frame rate and the minimum number of active images needed to obtain valuable information. Several PRF were implemented in the present study (Table 1).

Active cavitation detection and analysis

The area probed for all of the acquisitions was a rectangular area between 34 mm and 64 mm in depth, and between the 33rd and the 97th element of the array (18.9 mm large). As a consequence, the minimum duration between two ultrafast images was $T_{1\min} = 110 \mu s$. The elevation beam width at -6 dB was measured as 3 ± 1 mm at these depths.

As already mentioned, thanks to the emission of plane-waves, a complete B-mode ultrasound image of the area was obtained at each transmission (no iteration needed). This meant that less energy was sent through the medium than in conventional B-mode imaging, and as a consequence the interactions between active detection and bubble behavior were reduced. However, since the ultrasound beams were not focused in the transmit mode, the signal-to-noise ratio (SNR) and the contrast of the images were also reduced. Recently, Montaldo et al. [28] demonstrated that the SNR and contrast can be regained by combining coherently backscattered echoes from successive compounded plane wave insonifications at different angles. In this study, plane waves with -2 and 2 degree tilts were used to form the images after coherent synthetic recombination. For each plane-wave emission, a single-cycle pulse at 6 MHz was transmitted to each element of the array with the appropriate delay. In the receiving mode, the backscattered signals were sampled at 30 MHz. No time gain compensation (TGC) was applied.

The reference recording, before any bubble nucleation, comprised two acquisitions of tilted plane-waves with opposite angles (Figure 3), whereas the blocks following high-amplitude short excitation bursts consisted of $2.n$ acquisitions with alternately tilted insonification (Figure 3) – n was the number of pairs of active images acquired between two successive high-amplitude excitations; it varies with the PRF of the high-amplitude excitation (Table 1). The time period between two successive acquisitions was set to T_1 and depended on the PRF (Table 1). The same period was chosen between the trigger pulse and the first active detection. The acquisition for the first image after a high-amplitude excitation was then completed as soon as $t_{\text{trigger}} + 3 \cdot T_1$.

Spatial compound raw RF images were obtained by coherent recombination of the backscattered echoes from pairs of successive plane-wave illuminations with opposite tilts and beamforming of the data in the receiving mode [28]. Moreover, change detection (CD) images were produced by an additional coherent subtraction of reference echoes prior to beamforming. This subtraction technique was aimed at detecting the appearance or presence of bubbles in the medium, since induced bubbles were expected to cause the strongest

scatter changes in the medium, either because they appeared or because their size changed due to a high-amplitude excitation. It is worth noting that all of the images obtained here were provided in an absolute linear scale and were not normalized by the most reflective point in the image. Their lateral resolution was 0.9 mm and the axial resolution was 0.26 mm.

Thanks to the linear scale of the images, the scattering amplitude of the nucleated bubbles was measured. Indeed, at the location where a change appeared on the CD images, the value of the local maximum was proportional to the scattering amplitude from the bubbles due to the coherent summation made during the beamforming process. In this study, small areas in the vicinity of the brightest spots on the CD images were manually selected and the local maximum value was computed for each image.

These data illustrated the evolution of the scattering behavior of the bubble over time and between two successive high-amplitude excitations.

Synchronized high-amplitude emission and passive detection ***High amplitude insonification and calibration***

The therapy transducer was calibrated in degassed water by measuring the ultrasonic displacement at focus with a standard heterodyne interferometer. The experimental set-up used was previously described [29], and the digital demodulation scheme was used here. The pressure waveforms were derived from the measured ultrasonic displacement assuming that the phase front of the wave was locally planar. The following equation was used for the pressure evaluation:

$$P(t) = Z \cdot \frac{du}{dt}$$

where Z is the acoustic impedance of the water ($Z = 1.5 \text{ MRay}$) and u is the mechanical displacement induced by wave propagation.

During the bubble nucleation experiments, short bursts of one or two cycles were sent to the therapy transducer. The pressure waveforms measured are presented in Figure 2.

Passive cavitation detection and analysis

Following the high-amplitude excitation of the medium, passive data were recorded with the ultrasound scanner as if an untilted plane-wave had been transmitted by the array. No transmission actually occurred on the array, but during the same time period one was made on the therapy transducer thanks to synchronization. The time boundaries of the receiving mode were set just as if the same probed area as in part C a) had been imaged. The sampling frequency was 30 MHz. Due to the difference between the frequency of the emitted short burst (660 kHz) and the bandwidth of the linear array, high-frequency signals generated in the medium were mainly recorded (Figure 6). An additional digital high-pass filter (FIR, Butterworth high-pass digital filter design, order 3, 3 MHz cutoff frequency) was applied to the raw RF data before beamforming. The passive filtered RF data were beamformed under several assumptions using a beamforming algorithm detailed in the Appendix. First, the response of the bubble was supposed to occur immediately after the high amplitude excitation reached the nucleus. Then, the ultrasonic wave generated by the focused transducer was assumed to be locally planar in the surroundings of the focal point, the wave front being perpendicular to the focused transducer axis. Nucleation events were supposed to occur in the plane containing the axis of the therapy transducer and parallel to the linear array, and in the surroundings of the axis.

On top of this, the wave fronts on the RF signals were more precisely analyzed because the acoustic emissions which occur during bubble nucleation are possibly complex. Alignment of the RF signals was performed using cross-correlations over the channels of the array to determine the time shifts on each element.

Sequence parameters

A total of 530 acquisitions, both passive and active, could be recorded and treated with the parameters described above for a single experiment. Several PRFs were implemented and, for each, a compromise was made between achieving a good time resolution for the active detection and the maximum number of successive high-amplitude excitations. The ultrafast frame rate and the actual number of successive high-amplitude pulses were then adjusted. The set of parameters presented in this paper are summarized in Table 1.

Results

Bubble nucleation in gelatin gel

Gelatin gel is a transparent medium for the ultrasound frequencies at stake in the present study. Therefore, the only scatterers were seldom dust particles and nucleated bubbles. This simplified the understanding of the collected signals.

A typical example of bubble nucleation in gelatin gel is presented in the following paragraphs, including the main features encountered during the tests. The bubbles were nucleated using two-cycle excitations of the therapy transducer at a PRF of 25 Hz. The peak negative pressure at the focal point was evaluated in water as: -6.4 MP. The corresponding pressure waveform is shown in Figure 2.

Since the gel was free of scatterers, the B-mode images at the very beginning of the sequence were just used to check the targeted zone and are not displayed here. Then, the detection sequence was run and the nucleation events were observed from the first high-amplitude insonifications.

Figure 4 shows the data related to the first four high-amplitude insonifications. High-pass filtered passive RF data, both raw (Figure 4(a)) and beamformed (Figure 4(b)), and one active change detection (CD) image (Figure 4(c)) are displayed for each shot. The first CD images were actually noisy due to reverberations of the high power pulse; therefore, the second ones are displayed. In this figure, the appearance of scatterers on the CD images can be seen at the same time as the presence of the high-frequency acoustic wave front on the passive data, except for the second exposure. The fact, that neither active nor passive detection had an input to this second insonification (Figure 4(2)), demonstrates that no nucleation event was detected for this shot and that the scatterers generated by the first shot had disappeared. New scatterers were induced both on the third and the fourth insonifications, and their locations tended to prove that they were independent from the first ones.

Active detection was performed at a high frame rate after each shot. The dynamics of the scatterers were observed when displaying the successive CD images. For the first shot (Figure 4(1)(c)) the scatterer on the right-hand side of the focal point (bubble 0) could no longer be distinguished from the third image (lifespan of ~ 1 ms), while the one on the left-hand side (bubble 1) disappeared more slowly (lifespan of ~ 29 ms). The local maximum on the CD images for this scatterer (bubble 1) is plotted in Figure 5. The same estimation of the scattering amplitude was made for the scatterers that appeared after the third shot – i.e. bubble 2 (Figure 4(3)(c) and Figure 5) – and the one that was generated above the latter by the fourth shot – i.e. bubble 3 (Figure 4(4)(c) and Figure 5). The generation of these two scatterers resulted in a dramatic increase of the local maximum on the CD images. After each shot, all of the scattering amplitudes decreased with the passing of time, which is consistent with free bubble dissolution: bubbles 1 and 3 totally disappeared before the following shot while bubble 2 remained and even increased its scattering amplitude – so probably grew – due to the fourth shot. The reception of high-frequency signals during passive recording (Figure 6(a)) is also in good agreement with the fact that bubbles were generated. Indeed, acoustic emissions, such as spherical shock wave ones, are likely to occur during bubble nucleation events. Furthermore, once they are formed, bubbles are highly non-linear scatterers when driven by high-power pulses. It can be seen that for the second shot the main spectral component was the fundamental frequency of the excitation (660 kHz).

The spatial resolution of the active images was not sufficient enough to be able to distinguish between an individual bubble and a small cavitating region comprising multiple bubbles. However, it is convenient to refer to a region as “bubble X”.

The correspondence between the beamformed passive images and the CD images (Figure 4(b) and (c)), respectively) allows a better understanding of the passive images and the acoustic emission that occurred during the bubble nucleation event. The main difference between the two kinds of images is that more spots can be seen on the beamformed passive images, particularly for depths greater than 52 mm. For example, for the third high-amplitude exposure, a first spot (spot #1) close to the rhombus, can be seen in the passive image (Figure 4(3)(b)). Its location agrees with the so-called bubble 2 in the active image (Figure 4(3)(c)). But a second spot (spot #2) can be seen at the depth of $z = 57$ mm in the passive image (Figure 4(3)(b)) without a corresponding spot in the active image. The same observations can be made of the fourth shot (Figure 4(4)(b)). A closer look to the position of spot #2 shows that it has the same lateral position as spot #1. In order to determine whether this was accidental or whether both spots had the exact same lateral position, further analyses of the passively recorded data were performed. First, the curvatures of the wave fronts that led to the different spots were compared. A cross-correlation algorithm was used to determine the time delay laws that correspond to the wave fronts displayed in Figure 4(a). These time delays were then used to align the filtered RF data. For the first shot, two different delay laws were extracted, corresponding to the two brightest wave fronts displayed in Figure 4(1)(a). These are displayed in Figure 7(c) and are referred as ‘first’ and ‘second’ time delay laws. The curvatures of these delay patterns are similar, indicating that the emissions came from the same axial location. More precisely, according to the delay laws, the emissions originated from the point located at the respective lateral positions of bubble 0 and bubble 1 on the active image. The acoustic emission corresponding to the first delay law was likely to have originated from the location of bubble 1, and the second one from the location of bubble 0. The corresponding aligned RF data are displayed in gray in Figure 7(a) (with the first delay law) and Figure 7(b) (with the second delay law). In order to verify whether or not the delay laws correctly aligned the RF signals, the averages of these RF signals are also displayed in Figure 7(a) and (b) (black line). The aligned filtered RF data show that several pulse-shape signals actually had the same time delay law but were well separated in time: $2\ \mu\text{s}$, $4.3\ \mu\text{s}$ and $11\ \mu\text{s}$ in Figure 7(a) and $4\ \mu\text{s}$ and $6.5\ \mu\text{s}$ in Figure 7(b). This means that these signals were all emitted from the same location. Therefore, the successive signals could be interpreted as the acoustic emissions which occurred during the different phases of the bubble nucleation process. The acoustic emission of a nucleating bubble happens to be relatively complex. The first shot was chosen to illustrate the extraction of the delay laws (Figure 7(c)) because two cavitation events occurred at positions close to one another (bubble 0 and bubble 1).

For the sake of simplicity, the acoustic behavior will be examined in more detail for the third shot for which only one event was visible in Figure 4(3) (c) (bubble 2), and only two high-frequency wave fronts could be identified from the RF data (Figure 4(3) (a)). These two wave fronts were determined to have the same time delay law (not shown here). The time-domain data for one element can be seen in

Figure 8 (third shot curve). The first spherical wave recorded reached all of the elements of the array before 25 μ s. The magnitude of the Fourier transforms for the signals before and after 25 μ s (from the beginning of passive recording) are presented in Figure 6(b). Its spectrum analysis reveals a broadband noise component (above 2.5 MHz) and a second harmonic one (around 1.3 MHz). The second acoustic wave coming from the same location contained a similar broadband noise component above 2.5 MHz but the second harmonic one was much lower (1.3 MHz). The broadband noise can be the result of a violent process such as an inertial collapse which generates a shock wave [30], while the second harmonic of the excitation frequency is likely to indicate non-linear scattering. Therefore, if one assumes that the signal originated from a single bubble, the first pulse signal may then be a result of the combination of non-linear scattering and a violent size change of the bubble, whereas the second acoustic emission may be the consequence of its inertial collapse.

A comparison in the time domain of the passive data corresponding to the third and four shots showed another noticeable result which was observed in many experiments. For these two acquisitions, the same scattering spot (bubble 2) was visible on the CD active images (Figure 4(3-c) (4-c)). For the passive data, the first high-frequency wave front recorded for the fourth shot was found to have the same time delay law as the one for the third shot. Therefore, these two acoustic emissions are likely to have originated from the location of bubble 2, but for different shots. However, the arrival time of the high-frequency pulses differed from one shot to the other (Figure 8). The first pulse (in the time interval: 18 μ s to 21 μ s, in Figure 8) was shifted forward to around 1.3 μ s, which is approximately the period of the excitation pulse ($1/660$ kHz = 1.5 μ s), whereas it can be seen that before the first pulses (before 17 μ s in Figure 8) the passive signals match. The first “non-linear scattering and acoustic emission” event of the bubble most probably occurred on the second cycle of the first excitation (third shot), and on the first cycle of the following one (fourth shot), where a bubble was already formed and still present in the medium (Figure 5). This is consistent with the idea that, for the first excitation, the gas nuclei were only activated with the peak negative pressure which belonged to the second cycle of the excitation, whereas the bubbles which were already formed could be driven by the first cycle. It could then be assumed that, in an un-nucleated zone, the first “non-linear scattering and acoustic emission” event occurred during or shortly after bubble formation.

Since the passive beamforming algorithm was directly derived from an active beamforming algorithm it takes into account the arrival time of the wave front in order to compute the passive image. As a consequence, the successive wave fronts originating from the same location and corresponding to the different acoustic emissions from a bubble led to different spots on the passive image. Because the lateral position of the source remained the same, the spots corresponding to one source were aligned axially (Figure 4(b)).

If two different cavitation regions were formed with a close lateral position but at a different axial one, aligned spots on the passive image could belong to one or the other. For the fourth shot acquisition, two bubbles were identified on the CD active images (bubble 2 and bubble 3 in Figure 4(4-c)), and three axially aligned spots appeared on the passive image (Figure 4(4-b)). The uppermost and lowest spots were found to correspond to the same time delay law, and the middle one (around $z = 52$ mm) to a time delay law with a larger curvature. The source for this spot was higher up than for the other two and was identified as bubble 3 (Figure 4).

In summary, this example of bubble nucleation in gelatin gel showed that passive data recorded during the nucleation process contained information on both the dynamics of the nucleation process through the non-linear scattering signals and broadband acoustic emissions and also on the location of the nucleation event. Beamforming this passive data led to a complex image which was more difficult to directly interpret than the CD active images, particularly as far as the number and location of the cavitating regions were concerned. The backscattered echoes from the active imaging wave were more easily readable.

Bubble nucleation in sheep thigh muscle tissues

Thick and uniform muscle tissue samples were taken from sheep thighs, as can be seen in the B-mode image recorded before high-amplitude excitation (Figure 9). Scattering induced by the muscular fibers led to a dense and continuous speckle pattern on the image. As a consequence, echoes from scatterers other than the nucleated bubbles might be dominant in this medium.

Two examples of bubble nucleation in muscle tissues are presented here. For the first one, bubbles were nucleated using one-cycle excitations of the therapy transducer at a PRF of 101 Hz and a peak negative pressure of -6.4 MPa (measurement in water, Figure 2). This example shows the efficiency of the technique in a scattering medium. An overview of the detection images obtained for the first three high-amplitude excitations of the sequence is presented in Figure 10. The raw RF active images, corresponding to the CD images, are also displayed (Figure 10(b)). No variation in the speckle pattern or the appearance of hyperechogenic regions are detectable on these raw RF images, whereas nucleation was clearly detected from the second shot, both on the passive beamformed data and the CD images (appearance of scatterers).

A spot was already detectable on the passive beamformed RF image for the first shot (Figure 10(1a)), which indicates the emission of a high-frequency pulse locally in the medium. Several phenomena could explain this. First, a bubble might have nucleated and emitted a signal before it disappeared too fast to be seen on the CD images. Secondly, the generated bubble might have been too small to sufficiently backscatter the imaging plane-wave. Finally, as the passive images were not change detection images, since no reference RF signal was first subtracted, the high-frequency emission might also be caused by a scatterer from the medium. In this case, the fact that a spot was

present at the same location for the second shot (Figure 10(2a)) indicates that the bubble nucleation hypothesis was more relevant. Moreover, the spectrum analysis of the passive data revealed a broadband component. Axially aligned spots were also distinguished on the passive images, such as in the gelatin example (Figure 10(1a)).

As for the gelatin experiment, the local maximum was computed on the CD images in both areas where a scatterer appeared, showing dramatic increases after the second high-amplitude insonification (Figure 11). Similar increases occurred after the third shot, and each sudden increase was followed by a slow decrease.

A second example (Figure 12 and Figure 13), acquired at a higher PRF, shows bubble nucleation and also the early steps of a bubble cloud formation in muscle tissues. One-cycle excitations of the therapy transducer were used at a PRF of 1010 Hz and a peak negative pressure of -7.6 MPa (measurement in water, Figure 2). Data corresponding to the first four high-amplitude excitations are presented in Figure 12 . As for the previous example, no hyperechogenic region or speckle variations were seen on the raw RF active images (Figure 12(b)), but some scatterers appeared on the CD images. After the first shot a single cavitating region was detected (bubble 1). During the second shot, two others were generated: one upper and on the left-hand side (bubble 2), and the other deeper and also on the left (bubble 4). Two more were induced by the third shot: bubble 3 just above bubble 2 and bubble 5 just below bubble 4. Bubble 2 disappeared after the fourth shot. The evolution of the local maximum at each bubble location is plotted in Figure 13 . For bubble 2, the maximum could not be computed after the fourth pulse because of the expansion of the adjacent cavitating regions. Due to the high PRF, the time interval during which active detection was performed was highly reduced compared to the previous examples. Therefore, the dramatic increase in the scattering amplitude could be observed when bubbles had just appeared, but the decreasing phase between the two shots was not so clear (Figure 13). Secondary spots were also observed on the passive images, but they were outside the display zone of the images.

In summary, passive and active detections of bubble nucleation were performed in scattering tissues. Active detection using CD images allowed direct observations and detection of the location of the induced bubbles, but this was only possible when nucleation led to a cavitating region or bubbles large enough to produce an echo above the noise level and that last several images in the medium. Passive detection provided an indication of the acoustic emissions of the bubbles over their lifespan.

Discussion

With this technique, active images of *in situ* nucleated bubbles were obtained with a spatial resolution of the order of the imaging wavelength. Therefore, single nucleation events over a large volume were actively detected and discrete nucleation events were spatially separated. It is worth noting that this detection was only possible thanks to the fact that a post-nucleation residual bubble was present in the medium, and provided that this bubble had a lifespan of the order of milliseconds. The fact that a bubble larger than the initial nuclei remained after the explosive growth and potential collapse was expected since a bubble cloud was still observed after the emission of a histotripsy pulse [21], but it was not obvious for single nucleation events. Nevertheless, a theoretical study of a nucleus exposed to shock waves [31], which are also high-amplitude excitations, confirmed that after collapse and ringing a larger bubble might be obtained.

Since the same probe was used for both targeting and detecting active cavitation inception, superimposition of the B-mode and CD images would lead to the immediate localization of the nucleation events within the tissue structure. The location of the events within the pressure field of the therapy transducer was not straightforward since the imaging array was positioned on the side of the therapy transducer. The position of the focal point was however displayed on the images (marked with a rhombus). Having the imaging probe embedded in the single-element transducer so that the former median imaging plan includes the latter symmetry axis would greatly simplify the localization process and should be considered for future work.

Thanks to the successive and ultrafast active detections between the high-amplitude excitations, the time evolution of each nucleated bubble's scattering amplitude could be followed individually through measuring the local maxima on the CD images. Information about the dissolution rate and lifespan could be retrieved: the lifespan of bubble 1 was longer than 20 ms (Figure 11). Chen et al. [32] showed that the initial size of a nucleated bubble could actually be assessed from these data thanks to a model accounting for both the dissolution rate and the dependence of the scattering cross-section with the bubble's size at the imaging frequency.

Here, the imaging frequency was chosen so as to be appropriate for *in vivo* tissue imaging. Active detectors working at a higher frequency, such as the one described by Roy et al. [33] (focused 30 MHz detector), have the advantage of being insensitive to the high-amplitude pulse, so they can even be used during nucleation. Furthermore, the emitted frequency is *a priori* far above the bubble resonance, so the probing signal would not drive the induced bubble. However, the penetration depth in tissue at such a frequency is very small (less than a centimeter at 30 MHz), which limits the *in vivo* application of such detectors, and the use of high frequencies was actually shown to affect the cavitation process [24]. The potential effect of the imaging pulse on the bubble behavior was limited here for two reasons. First, active detection and the high-amplitude excitation were not simultaneous, so that interactions between the two signals were reduced. Secondly, the transmission signal for active detection was very short (1 cycle) and had a low intensity thanks to the use of plane-waves (lower intensity than conventional focused waves at the focal zone). Nevertheless, the sensitivity was enhanced by the

acquisition of the backscattered echoes on the array: on the one hand it allowed coherent summation of the signals in the beamforming process, and on the other hand it allowed an additional coherent combination of compounded insonifications with the sequence used here. As a result, the sensitivity of reception was similar to a focused singleelement detector but over an extended volume [28]. This sensitivity combined with a subtraction technique is the key aspect of this active method for distinguishing nucleated bubbles among other scatterers in diffusive media such as biological tissues.

For the technique as a whole, the short duration of the high-amplitude insonification is a crucial feature. First, for the active detection, and in particular for the CD images, it actually reduced the reverberation time of the high-power pulses, and then it reduced interference with the backscattered echoes of the imaging wave. Besides this, the acoustic radiation force resulting from this insonification was too small to induce any significant push in the medium: no shear wave was able to propagate and degrade the detection images. Secondly, for the mechanism of nucleation itself, the short duration of the excitation ensured that bubble generation was not due to boiling [34]. Furthermore, longer insonifications just above the nucleation threshold might lead to the generation of multiple bubbles from a single natural nucleus. A bubble nucleated on a cycle might collapse, fragment and seed the medium with new nuclei that would potentially nucleate bubbles in the following cycles. As a result, a bubble cloud would immediately be formed and the analysis in terms of natural nuclei spatial distribution, density and destabilization threshold would be more difficult than with discrete bubbles. The successive short excitations used in the present study allowed the evolution of the number and size of the nucleated bubbles to be followed pulse after pulse until a bubble cloud formed. Lastly, the emission of only a few high-amplitude cycles allowed rich passive RF data to be recorded. Pulse shape and coherent signals were collected on the array. Analysis of the wave fronts for the gelatin gel sample showed that at least two pulse shape signals originating from the same location could be identified. It can be hypothesized that they were actually emitted by a single bubble during its nucleation process. Spectrum analysis of the first signal emitted showed that this may have resulted from both non-linear scattering and shock wave emission filtered by the bandwidth of the imaging transducer. Since no bubble could be detected in the medium before the high-amplitude excitation, the shock wave could either have resulted from the explosive growth of a nucleus or from the collapse of an activated nucleus. Several studies demonstrated experimentally that a bubble nucleated using a laser pulse (laser optical breakdown) [35]-[36] does emit a shock wave whilst it expands. However, the authors could not find strong evidence in the literature that the same phenomenon occurs for acoustically generated bubbles. Nevertheless, the collapse of an acoustically generated bubble was found to emit shock waves [30]. Moreover, theoretical and experimental studies [31], [37]-[39] showed that when a bubble is submitted to a lithotripsy pulse, i.e. a shock wave starting with a peak positive pressure followed by a negative pressure, it first collapses because of the high compression and then re-expands to collapse again. Therefore, a nucleus insonified with the high-amplitude excitation used in this paper could grow without radiating much recordable signals and then undergo a first collapse before expanding again. Furthermore, this approach was confirmed by the fact that the first pulses recorded for a nucleating bubble and an already formed bubble had very similar pulse shapes in the time domain (Figure 8), implying that the nucleus had already grown before it emitted the pulse. A model developed by Church [31] suggests that, when driven by a lithotripter pulse, a bubble first collapses, then undergoes a “first bounce” (emitting a pressure pulse), after which the bubble undergoes a sustained expansion phase before collapsing again and, on the second bounce, emits a second pressure pulse. In our case, this second collapse may explain the second pulse recorded in the passive data. After the second collapse, the model predicts that the bubble (after rebounding) attains a stable radius larger than the initial radius, and then slowly dissolves. This is also what was observed in our experiments and it explains why active imaging might exhibit a change in echogenicity after a passive signature of the bubble (Figure 5 and Figure 10-2c and Figure 10-3c). Assuming that the observed phenomena followed Church’s model, the period between the first two pulses would then be the time of collapse [31].

The above analysis suggests that passive data can be interpreted as acoustic emissions from single nucleated bubbles. Additional simultaneous optical investigations and further modeling using the high-amplitude waveform measured here are needed to test the hypothesis and should be considered for future work.

Passive cavitation imaging techniques with ultrasonic arrays have been previously introduced [19]-[20], and they succeeded in detecting cavitation by beamforming the array element signals and calculating their energy in time. These techniques do not require any triggering as they do not use the time of arrival but rather differences in the time of arrival [19]. Integration over time is performed in the beamforming process to form the passive image [19]-[20]. The lateral and axial resolutions are given by the classical Rayleigh-Sommerfeld diffraction theory. For a linear array of aperture D imaging a point source at a depth F, the -3dB transverse and axial resolutions are given, respectively, by [40]:

$$\Delta x \approx \lambda \frac{F}{D}$$

and

$$\Delta z \approx 7\lambda \left(\frac{F}{D}\right)^2$$

where λ is the mean wavelength of the source.

The technique presented in this paper uses the same time delay beamforming, but with additional triggering. Consequently, the transverse resolution is exactly the same, but the axial resolution is linked to the duration τ of the received signals (like the standard pulse-echo imaging techniques used by medical scanners):

$$\Delta z = c \frac{\tau}{2}$$

In the experimental set-up used in the current article, the location of the focal point of the therapy transducer was 48 mm away from the array ($F = z_F = 48$ mm) and the aperture D of the array (64 successive elements) was equal to 19.2 mm. The central frequency of the array was 5 MHz, corresponding to a 0.3 mm wavelength. The use of (eq. 2) gave the lateral resolution: 0.75 mm. The duration of the received signals was typically equal to 0.5 μ s (Figure 8). The axial resolution was thus equal to 0.38 mm. The axial and lateral resolutions were thus of the same order of magnitude. If the same image reconstruction as used in [19] and [20] had been performed with our set-up, we would have obtained a lateral resolution of 0.75 mm (eq. 2) and an axial resolution of 13 mm (eq. 3). In this particular application of detecting cavitations events induced by short pulses of high-intensity ultrasound, the use of synchronized detection improved the axial resolution by a factor of 35. It should be noted that in the case of continuous insonification, as is the case in HIFU thermal treatment, such an improvement would be impaired.

As can be seen in Figure 8, the synchronization was not perfect due to the statistical nature of the cavitation occurrence: cavitation occurred during the first period of the excitation pulse for the third shot and during the second period of the excitation pulse for the fourth shot. This gave rise to a 1.3 μ s shift in the arrival time. As the duration of the signals were recorded for the third and fourth shots, the resolution remained the same but the precision of the location of the nucleation event was affected: it corresponded to an axial shifting of 1 mm.

In summary, the use of multi-element acquisitions allowed us to separate the different coherent pulse acoustic emissions on the passively recorded data. The passive detection here was shown to be sensitive toward single cavitation events. Moreover, it was effective over an extended volume and simultaneous events could be detected. The passive images obtained by the use of a beamforming technique based on an active beamforming algorithm could be more difficult to interpret in the case of several nucleation events occurring in the same image because of secondary pulses which do not correspond to the physical position of a another nucleation event, but rather to a second emission originating from the same bubble.

The active images could be used to discriminate between the spots on the passive images since no secondary pulse appears on the active ones and because they have a good axial resolution (0.3 mm). However, the formation of a bubble large enough to be observed actively is then required. Because of the high amplitude used here and the small size of the nuclei in the medium, all nucleation events were expected to give rise to an acoustic emission. However, an induced bubble can disappear or reach an undetectable size before the first active image. In this case, it would not appear on the active images, but it would be visible on the passive images. This was observed during our experiments (Figure 10(a)). Conversely, if a lower amplitude (and most probably longer) exposure was used and managed to form bubbles, they may not have undergone a violent size change and would not emit any high-frequency pulses. However, they would be detectable on the active images (not shown). Consequently, the combination of passive synchronized detection and ultrafast active imaging is the strength of the method presented here.

Multi-shot acquisitions can be performed using this developed technique, which has two major advantages. First, as the distribution of natural nuclei is unknown and might evolve, it increases the likelihood of inducing bubble nucleation. Each separate shot is a new attempt to destabilize the present nuclei and therefore they contribute to the determination of the nucleation threshold. Secondly, once a bubble has been nucleated, depending partly on the PRF, it might either dissolve totally or only partially before the subsequent shot. In the latter case, the remaining bubble would be driven by the shot and could lead to the formation of a bubble cloud. This sequence is more likely to occur at a high PRF, such as in the presented example of a PRF of 1 kHz where new bubbles were generated on the first three shots (Figure 13). In future work, this technique could be used to understand the dynamics of bubble cloud formation in biological tissues.

Finally, this technique might also be useful for determining *in vivo* the nucleation threshold of vaporizable particles such as perfluorocarbon droplets [41]–[44] in tissue. Furthermore, it could be used to control and monitor the vaporization and then the delivery of the conveyed drugs or molecules, shot after shot.

Conclusion

A novel all-ultrasound method able to detect and locate single nucleation events in scattering media is presented here. It is based on combined passive and active detection over a large volume and using the same multi-element probe. Besides detection, the behavior of individual generated cavitating regions was observed thanks to active imaging at an ultrafast frame rate. The use of ultrasound frequencies common in conventional ultrasonic imaging makes this technique appropriate for *in vivo* implementation. It could provide useful information for the determination of the nucleation threshold in various tissue structures and for a better understanding of the spatial and size distribution of gas nuclei *in vivo*.

Furthermore, the high frame rate capacity of the active detection allows pulse rate frequencies to be reached in the kHz range for the high-amplitude excitation. This makes a study of the steps of bubble cloud formation possible. Therefore, this method is expected to be of great interest for a better understanding and monitoring of the initiation phase of cavitation therapies in living tissues.

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Appendix

The algorithm used to beamform the passive data is based on the algorithm used for active images with an untilted plane-wave transmission. However, because of the angle between the single-element axis and the median imaging plan of the array, the travel time to point A (x,z) and then to the element of the array placed in x_n is given by:

$$\tau(x_n, x, z) = \frac{1}{c} \left(F_c - \frac{z_F}{\cos(\theta)} \right) + \frac{1}{c} \frac{z}{\cos(\theta)} + \frac{\sqrt{(x - x_n)^2 + z^2}}{c}$$

where c is the speed of sound assumed to be constant in the medium, F_c is the focal length of the therapy transducer, z_F is the depth of the focal point in the imaging plan and θ is the angle between the array axis and the z axis of the imaging plan (Figure 14).

Each point (x,z) of the image is obtained by coherently adding the contribution of each acoustic emission, i.e. delaying the radio-frequency signals $RF(x_n, t)$ received on the array by $\tau(x_n, x, z)$ and adding them in the array direction.

$$s(x, z) = \sum_{n=1}^{64} RF(x_n, \tau(x_n, x, z))$$

The angle θ was set equal to 45°.

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Figure 1

Experimental set-up. Drawing (a) represents a schematic side view of the integrated high-amplitude focused ultrasound and imaging system and a schematic diagram of the driving electronics. The interrogation path (---) of the linear array is coaxial with the single element transducer focal spot. Picture (b) shows the integrated system.

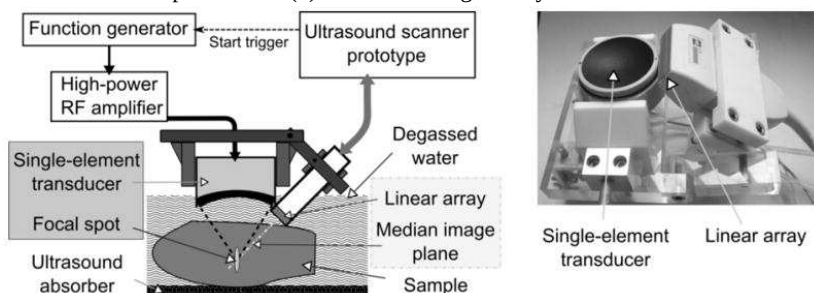


Figure 2

Pressure waveforms of the therapy pulse at the focal point of the therapy transducer. The signals shown are the averages of 15 acquisitions low-pass filtered below 50 MHz (FIR, Butterworth high-pass digital filter design, order 3, 50 MHz cutoff frequency). Each waveform corresponds to a different excitation used in this paper: a two-cycle excitation for the gelatine gel, and two different one-cycle excitations for the muscle samples. The measurements were recorded in degassed water. The peak negative pressure is indicated on the pressure axis.

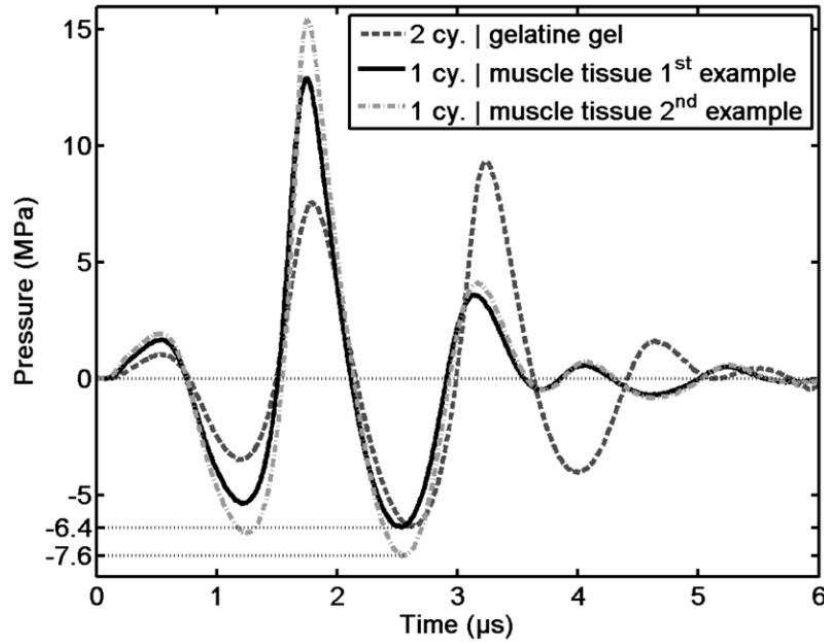


Figure 3

The nucleation detection sequence. The two time lines represent the timing sequence for (A) the ultrasound scanner driving the linear array and (B) the high power channel driving the single-element transducer. The synchronization of the time lines occurs at $t=0$ with the triggering event (trig.). The blocks “synchronized high-amplitude emission and passive detection” are marked by the white rectangle including the triggering event, and the blocks “ultrafast active detection” are indicated by light gray rectangles. The time period between two successive plane wave transmits is T_1 ; it is also the duration between the triggering event and the first transmission by the array. The reference acquisition before any nucleation is circled in gray. Each attempt to nucleate a bubble with a high-amplitude excitation was followed by the union of a passive and an active detection block. This combined detection is circled by a black dashed line and lasted for a time period T_2 . $1/T_2$ is the pulse rate frequency (PRF) of the high-amplitude excitation.

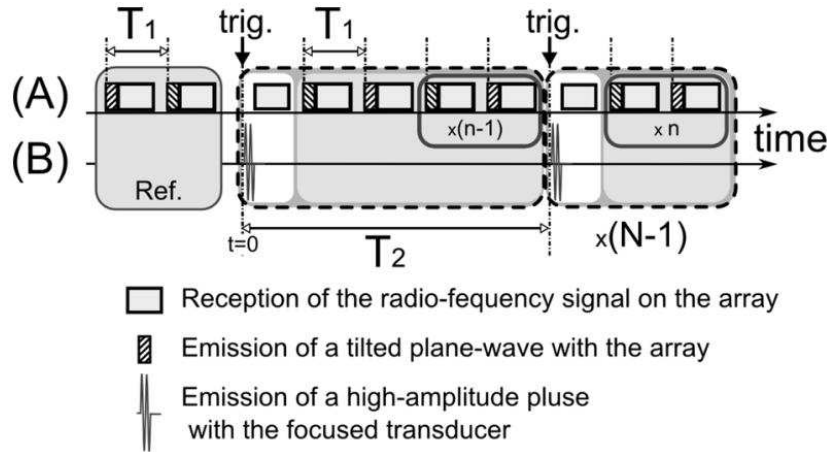
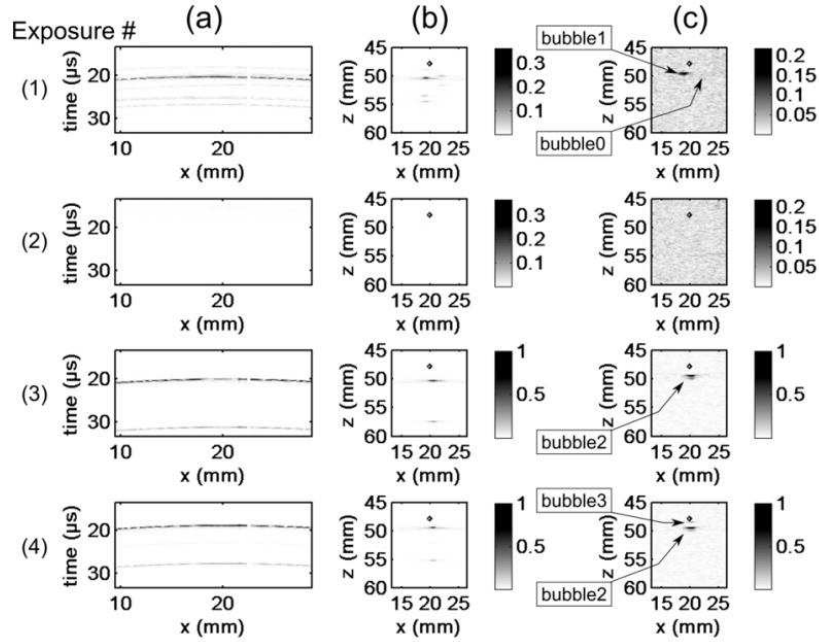


Figure 4

(Gelatin gel) Images of the different detection acquisitions for the first four highamplitude exposures. Each line corresponds to a different shot: (a) high-pass filtered passive radio-frequency data, (b) the corresponding passive beamformed image, (c) the second active change detection image for each shot. The x axis origin is set to the first element of the array. For (b) and (c), the focus point of the single-element transducer is marked with a black rhombus ($z = 47.9$ mm, $x = 19.8$ mm). The beamformed data are normalized to the brightest point of the series for (b) and (c).

**Figure 5**

(Gelatin gel) Evolution of the scattering amplitude of the cavitating regions identified in Figure 4. The vertical dash dotted lines indicate the high-amplitude shots.

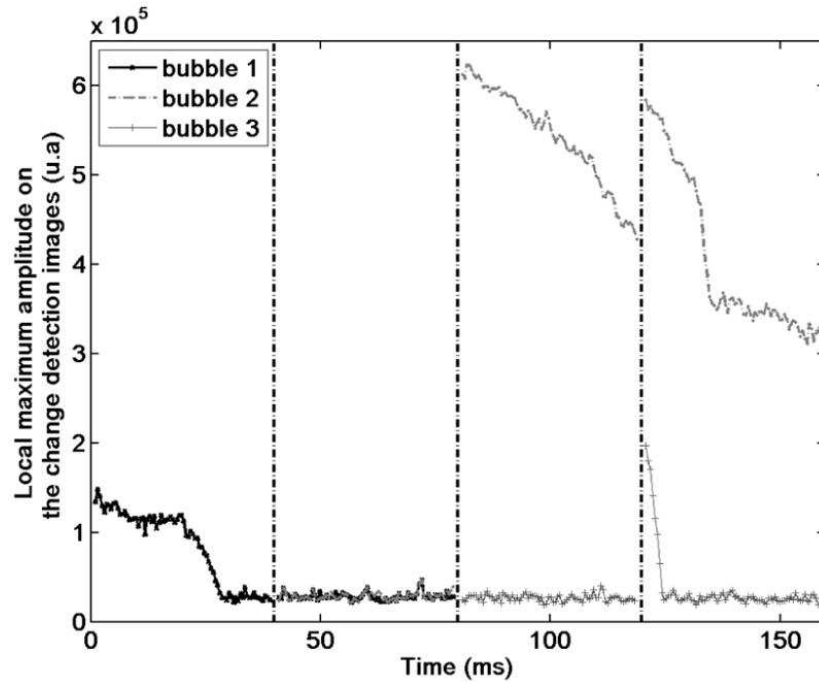
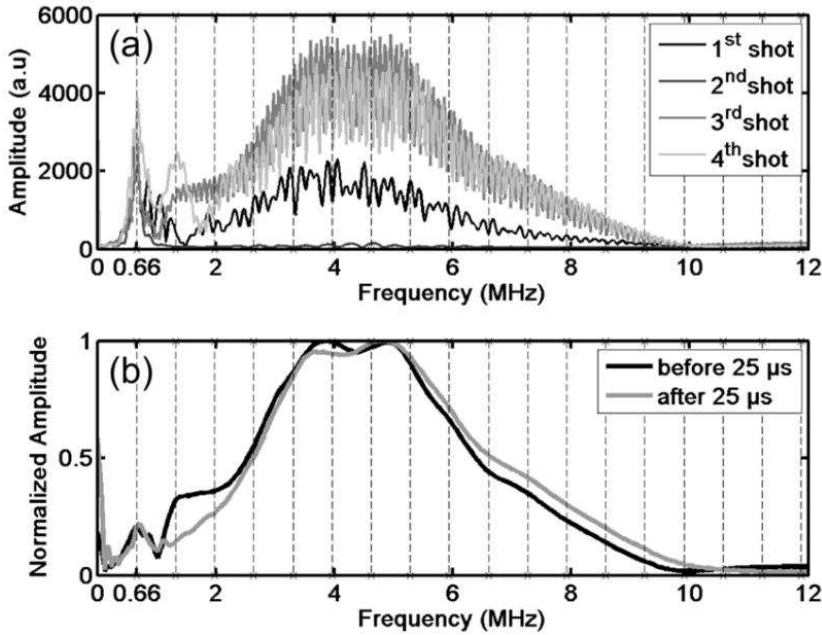


Figure 6

(Gelatin gel) Magnitude of the Fourier transform of the unfiltered passive radio-frequency data for (a) all of the different shots and the whole duration of the recorded signals, (b) the third shot analyzed in two separate parts: before and after 25 μ s from the beginning of passive recording. The spectral traces shown are averages over the 64 channels. For (b), the spectral traces are normalized to their maximum. The vertical dashed lines indicate the integer multiples of the central frequency of the high-amplitude excitation pulse (660 kHz).

**Figure 7**

(Gelatin gel) Alignment of the filtered passive radio-frequency (RF) data for the first shot, (a) and (b) display the alignment of the RF data corresponding to the first and second time delay laws plotted in (c), respectively. For (a) and (b), the superimposed gray curves are the 64 delayed passive signals received on the elements of the ultrasonic array, and the thick line shows their averages.

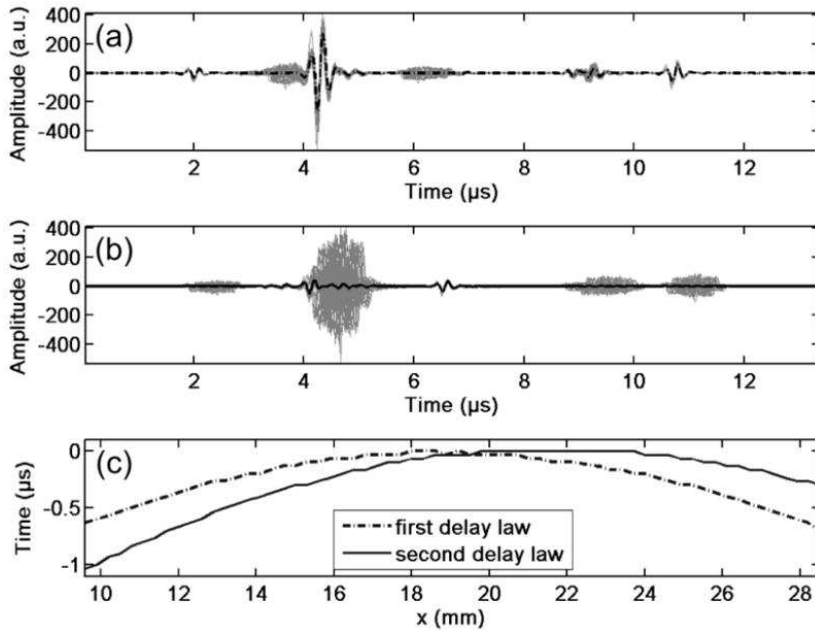


Figure 8

(Gelatin gel) Unfiltered passive radio-frequency signals recorded with the 65th element of the array for the third and fourth shots.

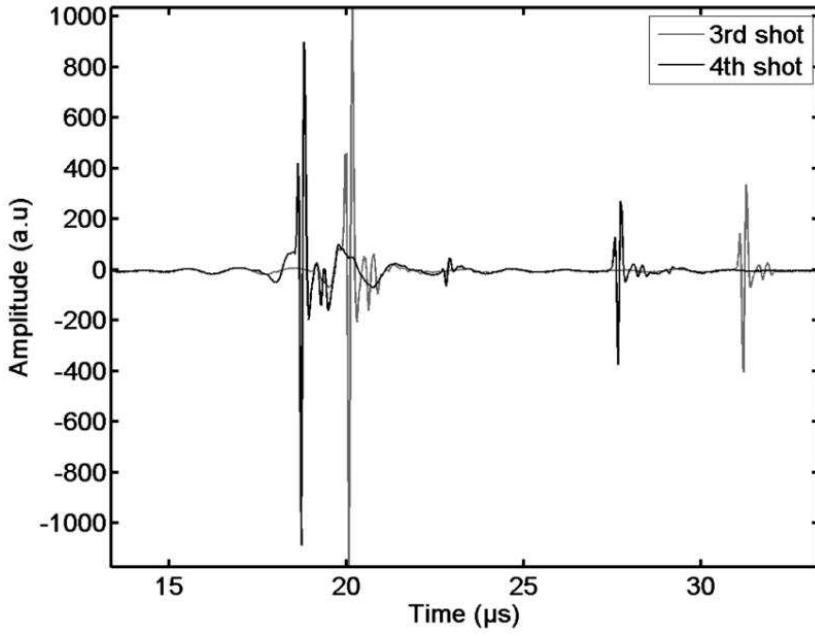


Figure 9

(First sheep thigh muscle sample) B-mode image corresponding to the acquisition presented in Figure 10 and Figure 11 . Nucleation detection occurred in the area between the vertical white dashed lines. The focus point of the single-element transducer is marked with a white rhombus ($z = 47.9$ mm, $x = 19.8$ mm).

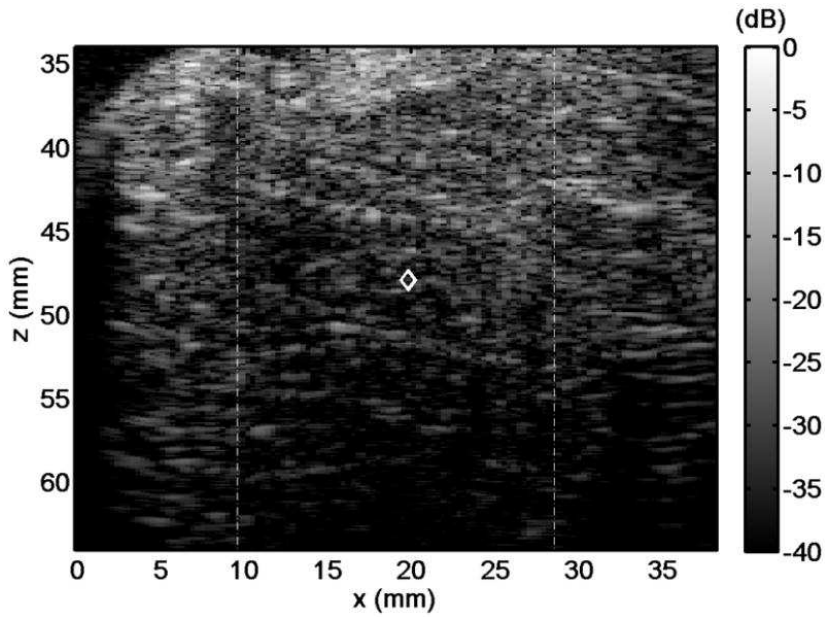
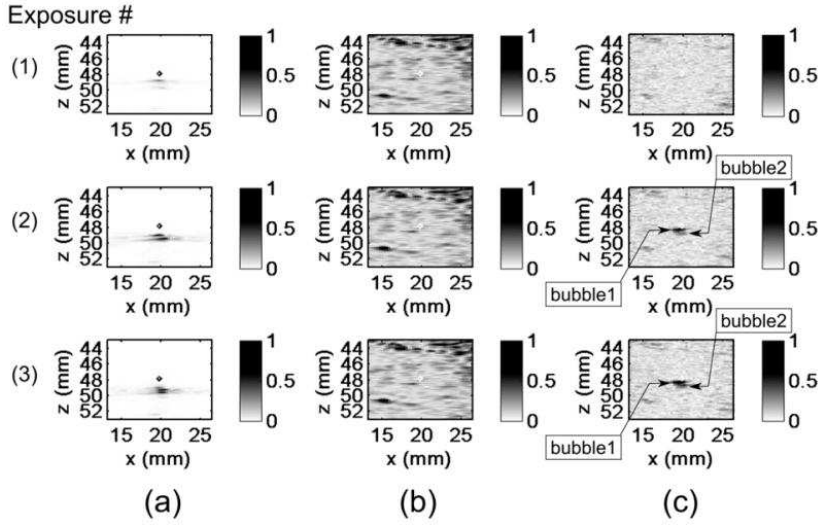


Figure 10

(First sheep thigh muscle sample) Images of the different detection acquisitions for the first three high-amplitude exposures. Each row corresponds to a different shot: (a) the beamformed image corresponding to the high-pass filtered passive radio-frequency (RF) data, (b) second raw RF active image for each shot, and (c) the corresponding change detection image. The x axis origin is set to the first element of the array. For columns (b) and (c), the focus point of the single-element transducer is marked with a white rhombus ($z = 47.9$ mm, $x = 19.8$ mm). The beamformed data are normalized to the brightest point of the series for (b) and (c).

**Figure 11**

(First sheep thigh muscle sample) Evolution of the scattering amplitude of the cavitating region identified in Figure 10 . The vertical dash-dot lines indicate the high-amplitude shots.

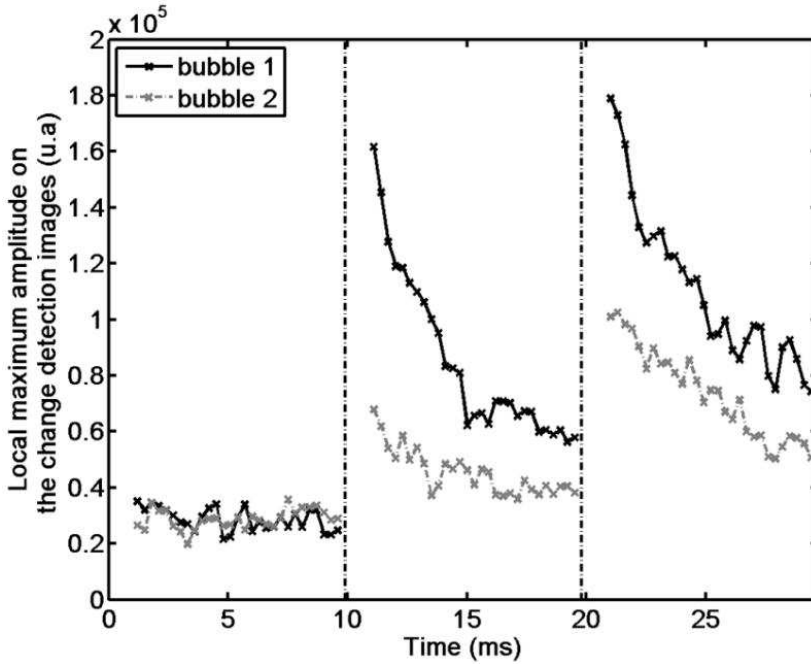
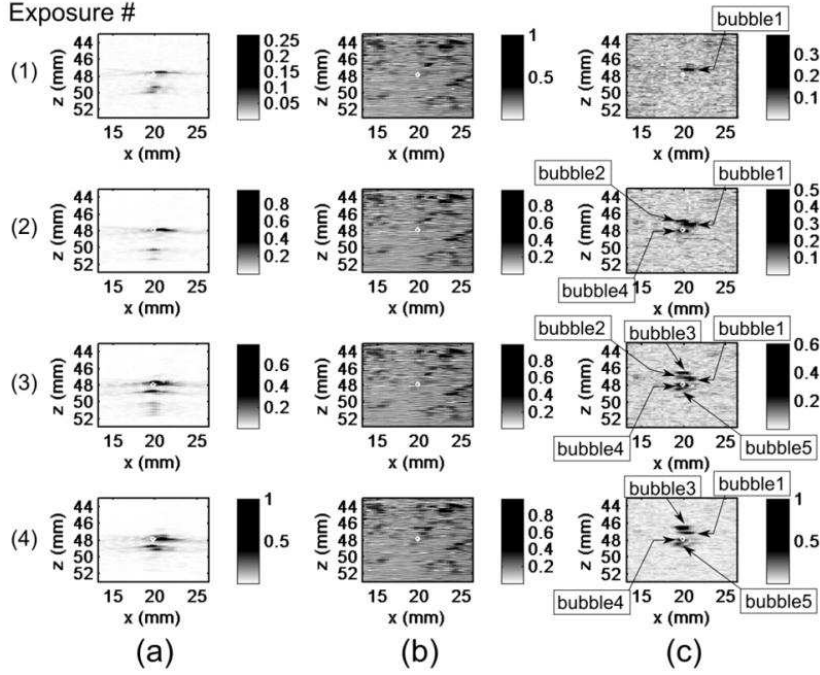


Figure 12

(Second sheep thigh muscle sample) Images of the different detection acquisitions for the first three high-amplitude exposures. Each row corresponds to a different shot: (a) the beamformed image corresponding to the high-pass filtered passive radio-frequency (RF) data, (b) second active raw RF image for each shot, and (c) the corresponding change detection image. The x axis origin is set to the first element of the array. For columns (b) and (c), the focus point of the single-element transducer is marked with a white rhombus ($z = 47.9$ mm, $x = 19.8$ mm). The beamformed data are normalized to the brightest point of the series for (b) and (c).

**Figure 13**

(Second sheep thigh muscle sample) Evolution of the scattering amplitude of the cavitating regions identified in Figure 12. The vertical dash-dot lines indicate the high-amplitude shots.

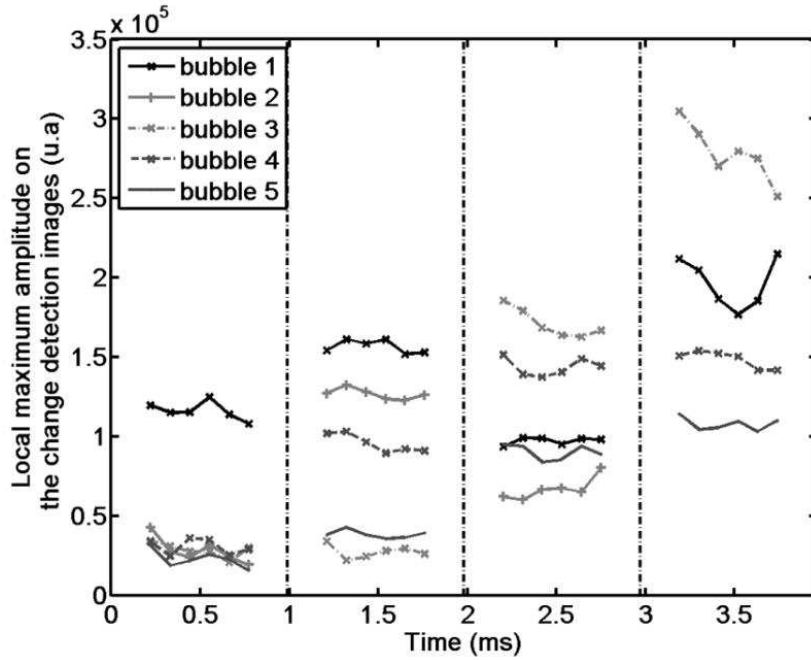


Figure 14

Diagram of the synchronized passive beamforming

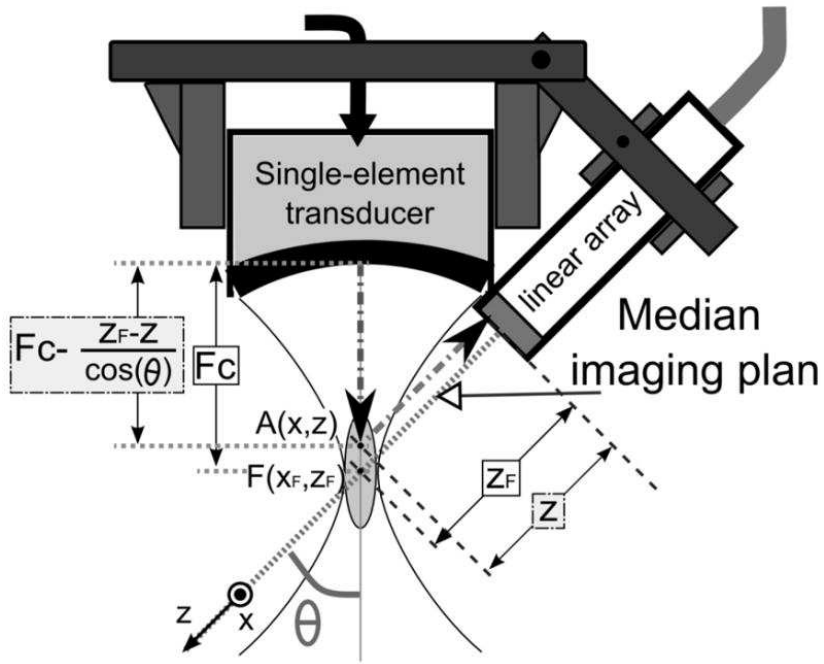


Table 1
Sequence parameters

PRF of the high-amplitude excitation (= $1/T_2$)	Number of successive high-amplitude exposures for an experiment (=N)	Period between images (= T_1)	Number of active images following a high-amplitude short burst excitation (= 2.n)
		Ultrafast frame rate (= $1/T_1$)	
25 Hz	6	493 μ s 2038 Hz	80
101 Hz	16	300 μ s 3333 Hz	32
1010 Hz	60	110 μ s 9091 Hz	8