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Translating visually the reasoning of a perceptron: the weighted rainbow boxes technique and an application in antibiotherapy

Jean-Baptiste Lamy, Rosy Tsopra
LIMICS, Université Paris 13 - Sorbonne Paris Cité, UPMC Université Paris 6, Sorbonne Universités, INSERM UMRS 1142, Bobigny, France
Email: jean-baptiste.lamy@univ-paris13.fr rosytsopra@gmail.com

Abstract—In this paper, we propose a technique for translating visually the reasoning of a perceptron. The artificial neuron, or perceptron, is a simplified model of a biological neuron. It can achieve simple reasoning and solve linearly separable problems. Despite its limited reasoning power, it is enough to deal with several real-life problems. The proposed technique is based on rainbow boxes, a technique for overlapping set visualization, which has been applied to the input vectors of the perceptron. We extended this technique, leading to weighted rainbow boxes. It can visualize several input vectors and output values for a single perceptron. We applied this approach to decision support in antibiotherapy, for the determination of the most appropriate antibiotic in urinary infections, by taking into account the properties of each drug (e.g., efficacy, risk of adverse effects, etc). Finally, a user study with 11 physicians showed that most of them found the visualization interesting and easy to read.

Keywords—perceptron; overlapping set visualization; antibiotherapy; user study

I. INTRODUCTION

The artificial neuron, also called perceptron, is a simplified model of a biological neuron, and it is the base unit for artificial neural networks (ANN) [1]. A perceptron has \( n \) inputs \( I \) and produces one output \( O \) (see example at the top of Figure 3). A weight \( w_1 \) is associated with each input \( I_i \). As a processing unit, the perceptron computes the weighted sum of its inputs, by multiplying the value of each input by its weight and summing them, and then it applies on the result the activation function \( f \). A typical activation function is a threshold function (returning 1 if \( x \) is above the threshold, and 0 otherwise) or a sigmoid function. Consequently, the output can be computed with the following formula: \( O = f(I_1 \times w_1 + I_2 \times w_2 + \ldots + I_n \times w_n) \).

A single perceptron can achieve simple reasoning and solve linearly separable problems. On the contrary, more complex problems require several perceptrons. Although it is limited in terms of reasoning power, a single perceptron is enough to deal with some real-life problems. An example is the application of a lexicographic order or the computation of a (linear) score, e.g. “if input \( I_1 \) is true, increase the score by \( w_1 \), if input \( I_2 \) is true, increase the score by \( w_2 \)”. For example, in antibiotherapy, the physician has to choose an antibiotic drug to prescribe. R Tsopra et al. [2] have shown that the most appropriate antibiotic can be determined by considering several antibiotic properties and then ranking the antibiotics according to their properties, considered in a lexicographic order.

A problem of perceptrons is their “black-box” nature: they
produce an output but they do not explain to a Human user why the result is the obtained one. The visualization of the reasoning of a perceptron, i.e. the representation of the input values, the output value and the relation between them, is a solution to this problem. If we consider a perceptron with Boolean inputs, the representation of several input vectors can be seen as an overlapping set visualization problem (in which the elements are the input vectors, and the sets are the sets of input vectors for which a given input value is true).

In this work, our objective was to improve rainbow boxes, a visualization technique for overlapping sets [3], for the visualization of the input and output values of a perceptron, and for translating visually its reasoning. The paper describes the resulting techniques, called weighted rainbow boxes, and a medical applications in antibiotherapy.

The rest of the paper is organized as follows. Section II presents related works on the visualization of ANN and overlapping sets. Section III describes the extensions we propose to rainbow boxes. Section IV describes an application in antibiotherapy. Section V describes a small user study on this application. Section VI discusses the proposed technique and its application. Finally, section VII concludes the paper with perspectives.

II. RELATED WORKS

A. Visualization of artificial neural networks

Several aspects of an ANN can be visualized: the topology of the network, the weight associated with each connection, the input and output vectors, and the evolution of the learning (which is a time-related feature, considering, for example, the evolution of the weights or of the error surface). The visualization tools proposed in the literature address one or more of these four aspects.

The weights can be visualized with Hinton diagrams [4]. The topology of the network is usually represented as an oriented graph. In addition to the topology, the Bond diagram displays the weights using colored arrows on the arc [5]. Specific tools have also been developed for visualizing the topology of networks in the Human brain (i.e. connectomics) [6]. When considering a single neuron, the input vectors and the output are usually represented using a hyperplane. The (single) output is represented by a color ranging from black to white. Two or three inputs are considered, with one dimension for each. Thus, the hyperplane is a line (for two inputs) or a plane (three inputs). For more inputs, the visualization of the hyperplane is problematic. This approach has been extended to networks made of several neurons, using several hyperplanes organized in a matrix [7].

Learning has led to more complex visualizations. Lascaux [8] displays the topology of the network and represents each neuron by a square cell, showing its current state. It can show the activation of neurons, but also the backward-propagation of error signals during learning. Another approach consisted in applying principal component analysis to the weights [9].

In conclusion, only one of the proposed approaches, the hyperplane, allows reproducing visually the reasoning of an ANN, but it is limited to 2-3 inputs.

B. Visualization of overlapping sets

Overlapping set visualization considers several elements, as well as sets containing all or part of these elements. The sets are overlapping: a given element can belong to more than one set. A typical simple example is the “amino-acid properties” problem. There are 20 amino-acids, which share physical or chemical properties. Amino-acids can be considered as elements and properties as overlapping sets of these elements. B Alsakallah et al. recently reviewed the various methods proposed for overlapping set visualization [10] and distinguished 6 categories: Euler / Venn diagrams, overlays on a map, graphs and node-link diagrams, matrix-based techniques (rainbow boxes fit in this category), aggregation-based techniques, and scatterplot-based techniques.

Last year, we proposed a new technique: rainbow boxes [3]. It targets small structured datasets (Figure 2). It displays the elements to be compared in columns, and the sets in labeled rectangular boxes that cover all the columns corresponding to the elements in the set. Larger boxes are placed at the bottom and two boxes can be side-by-side as long as they do not cover the same columns. A box can have holes, if the elements in the set are not displayed in consecutive columns. The technique is based on two hypothesis: (1) it exists an optimal order of the columns with a small number of holes (or even none at all) and (2) it is possible to find this order. Hypothesis 1 is application domain-dependent but seems to be valid in several situations. For hypothesis 2, the problem complexity is factorial. We proposed a heuristic algorithm to find, in a satisfying time, a near-optimal column order minimizing the number of holes.
III. Weighted rainbow boxes

Weighted rainbow boxes extend rainbow boxes by adding per-set weights, represented graphically by an additional visual variable: the vertical size of the boxes. The weight of a set is represented by the height of the corresponding box. Figure 3 shows an example of weighted rainbow boxes.

Let’s consider a category of perceptron, with (a) Boolean inputs (the false and true values being represented by 0 and 1, respectively), (b) a Boolean or positive real output, (c) strictly positive weights, (d) no bias (if really needed, the bias could still be added as the weight of an additional input which is always true), and (e) one of the two following activation functions: the threshold function \( f_{\text{thres}} \) if the output is Boolean, and the no-op function \( f_{\text{noop}} \) if the output is a real, defined as follows (\( t \) being a fixed parameter): \[
\begin{align*}
  f_{\text{thres}}(x) &= 1 \text{ if } x > t, \quad 0 \text{ otherwise} \\
  f_{\text{noop}}(x) &= x
\end{align*}
\]

The visual representation of the input vectors of a perceptron can be seen as an overlapping set visualization problem: each input vector is an element (i.e. a column in the rainbow boxes), and for each input \( I_i \), we can define the set (i.e. the box) of input vectors for which \( I_i \) is true. These sets are overlapping, because a given input vector can belong to more than one set, if the input vector contains several true values. Consequently, weighted rainbow boxes can be used to visualize the input vectors as overlapping sets, using the weight of the inputs of the perceptron. Standard rainbow boxes use arbitrary “rainbow” colors; for visualizing a perceptron, we propose to use a single hue and a saturation proportional to the weight (as in Figure 3).

The boxes are stacked vertically and their height is proportional to the weights of the perceptron, consequently the total height of the stacked boxes corresponds to the weighted sum of the input values of the perceptron. Thus, it is very easy to compute visually this sum. If the activation function is \( f_{\text{noop}} \), the sum corresponds directly to the output value of the perceptron for the represented input vector (see \( O_x \) in Figure 3). If the activation function is \( f_{\text{thres}} \), the threshold can be represented visually by a horizontal line, whose Y coordinate corresponds to the value of the parameter \( t \). It is easy to determine visually if the weighted sum of the input values is higher or lower than the threshold value, i.e. if the stacked boxes are higher than the threshold line or not. Therefore, weighted rainbow boxes can at the same time provide an overview of the dataset (i.e. the input vectors), display the weights of each input and allow the visual computation of the output value for each input vector.

Gaps and holes can complicate the visual computation of the output value, because in these cases the boxes are not tightly stacked. However, in practice we observed that, at least when a single hole or gap is involved, it does not prevent the visual comparison of the output values, although it can make it more difficult.

IV. Application in antibiotherapy

Doctors frequently prescribe non-optimal antibiotics, despite the associated risks: complications for the patient and emergence of bacteria resistance [11], [12]. In primary care, the antibiotic choice should take into account 6 antibiotic properties we identified in previous studies [2], [13]: the level of efficacy, the complexity of the administration protocol, the risk of emergence of bacteria resistance, the risk of adverse effects, the extent of the bacteria spectrum and the preciosity of the antibiotic class. However, in clinical practice, it is difficult for GPs to choose the best antibiotic to prescribe in a specific indication because: (i) they are not aware of all the properties of all antibiotics, (ii) the value of these properties may evolve quickly [14], (iii) they have to take a decision in a few minutes [15] whereas they don’t have any tool for comparing antibiotics. Helping GPs to compare antibiotics could improve antibiotic prescriptions.

A. Knowledge base

We considered the 6 properties and 7 indications in urinary infections: cystitis in adults with risk of complications, cystitis in children, cystitis in normal situation (i.e. adults without risk of complications), prostatitis, pyelonephritis in adults with risk of complications, pyelonephritis in children, pyelonephritis in normal situation. We designed a knowledge base containing the values of each property for each antibiotic in each indication (the values of some property is indication-dependent). Since the medical reasoning of experts is based on the progressive exclusion of the worst antibiotics, we considered properties in their “negative form”, each property becoming a potential disadvantage: \( I_1 \) moderate efficacy, \( I_2 \) complex protocol, \( I_3 \) risk of emergence of resistance, \( I_4 \) risk of adverse effects, \( I_5 \) broad spectrum, \( I_6 \) precious class (the \( I_x \) labels correspond to the associated
B. Reasoning

For determining the optimal antibiotics for a given indication, experts start with the list of available antibiotics (i.e., potentially efficient in the indication), and then exclude all antibiotics presenting the most important disadvantage (i.e., moderate efficacy). If several antibiotics remains, experts then proceed similarly with the second most important disadvantage, and so on, until the optimal antibiotics are found. Thus, the best antibiotics can be retrieved by ranking the available antibiotics according to disadvantages, in the following lexicographic order: consider $I_1$ (efficacy) first, then $I_2$ (protocol), then $I_3$ (resistance) and finally $I_4$ (adverse effect), $I_5$ (spectrum) and $I_6$ (precious class) with an equal weight for each.

This reasoning corresponds to a single perceptron with 6 inputs (one per disadvantage), one input vector for each antibiotic (i.e., a vector of Boolean values indicating the disadvantages of the antibiotic) and one output, the ranking score (lower score being better). The perceptron remains the same for the various indications, but with different input vectors (depending on the antibiotics available for the indication and the values of the properties for the antibiotics with regards to the indication). We translated the lexicographic order between the disadvantages into the following four domain constraints on the weights:

$w_1 > w_2 + w_3 + w_4 + w_5 + w_6$
$w_2 > w_3 + w_4 + w_5 + w_6$
$w_3 > w_4 + w_5 + w_6$
$w_4 = w_5 = w_6$

Additional visual constraints were added: (1) the minimum weight is 1.0 in order to display the label inside the boxes, (2) the total sum of the weights $\Sigma w_j$ should be kept as minimal as possible to limit the height of the interface, (3) the various weights should be different enough to allow an easy visual distinction between them. Weights were defined manually. Figure 5 shows the resulting perceptron, able to compute a ranking score for antibiotics.

C. Visualization

We used weighted rainbow boxes for visualizing the perceptron and the datasets for the 7 indications. Figures 4 and 1 show examples for pyelonephritis and for cystitis with risk of complications, with respectively 5 and 10 antibiotics. Each antibiotic is an element, displayed in a column, and each disadvantage is a set containing all antibiotics having the disadvantage, and displayed as a box. We colored the boxes in red colors, because they represent the disadvantages of the antibiotics and the red color is usually associated with negative opinion in occidental cultures. The height of each box is proportional to the importance of the corresponding disadvantage, e.g., the “moderate efficacy” box has the higher height. By summing visually the box heights in a given column, it is possible to compute a score; lower scores correspond to better antibiotics for the given indication. Thus it is easy to find visually the antibiotics with the fewest and less important disadvantages, i.e., the lowest scores. It
corresponds to the column with the lowest total box height, e.g. ofloxacin in Figure 4 and nitrofurantoin in Figure 1. Only one hole is present (in Figure 1, at the intersection of the ceftriaxone column and the frequent/serious adverse effect box).

V. USER STUDY

For assessing the simplicity and the utility of the application, we recruited 11 GPs. Three were women. Eight were between 30 and 40 years old, two between 40 and 50, and one more than 50 years old.

GPs had to visualize two datasets using weighted rainbow boxes: one comparing 5 antibiotics (Figure 4), and another comparing 10 antibiotics (Figure 1). For each, they had to score their feeling about 4 affirmations using a 5-level Likert scale. Then, for each dataset, GPs had to mention the antibiotic they will choose for the prescription. Finally, we asked the opinion of the GPs about having this kind of interface in clinical practice, and GPs were also allowed giving free-text comments.

The results are shown in Table I. GPs found the interface simpler for the 5-drug dataset than for the more complex 10-drug dataset (affirmation #1). However, for both datasets, they globally found that the disadvantages were easy to read (affirmation #2). Thus, when the number of drug increases, the interface becomes more complex but still remains easy to read. Displaying the disadvantages of antibiotics was considered as interesting for about 90% of GPs, and useful in clinical practice for more than 90% of them. In both datasets, 8 GPs choose to prescribe the antibiotic with the lowest ranked score, i.e. the one recommended using the knowledge base and the exclusion reasoning we described. Finally, 3 GPs would not like to have this kind of interface in clinical practice whereas 5 would like (3 neutral).

VI. DISCUSSION

In this paper, we described weighted rainbow boxes, a visualization technique derived from rainbow boxes, and we have shown that they enable a visual reasoning with a computing power equivalent to a perceptron. Weighted rainbow boxes can present and compare the various properties of several items, as original rainbow boxes did, e.g. on amino-acids, but it can also translate visually some simple reasoning based on the properties, such as a score computation or a lexicographic order for ranking the items. We also described an application in antibiotherapy. A small user study showed that the weighted rainbow boxes were rather easy to read for GPs.

A. Weighted rainbow boxes

Weighted rainbow boxes allows the visualization of the inputs and the weights of a given perceptron, and the input vectors and the output values of a dataset for this perceptron. In the literature, we have seen that few techniques have been proposed for visualizing input and output values, the most noticeable one being the hyperplane (see section II-A). The hyperplane is limited to 2 or 3 inputs, and does not show the weights explicitly. On the contrary, weighted rainbow boxes can support dozens of inputs, but they are limited to Boolean inputs with positive weights.

Several methods exist for training a perceptron or a neural network made of several perceptrons, such as backpropagation. However, we have seen that visual constraints must be satisfied in addition to the domain constraints, in order to obtain an efficient visualization. The visual constraints were related to the minimum height of the boxes, the limited height of the computer screen, the difficulty of the Human vision to compare very similar heights, and the exclusion of negative weights. Thus, learning methods should be adapted if one wants to learn the weights of the perceptron before visualization. In addition, usual limitations of the perceptron also apply, notably the impossibility to perform exclusive or.

B. Application in antibiotherapy

We presented an application for decision support for the treatment of urinary infections, based on the properties of antibiotics. In medicine, decision support systems are usually not based on treatment properties, but rather implement clinical guidelines developed by health authorities. These guidelines provide recommendations, in particular for prescribing. They are implemented in clinical decision support systems; many such systems exist [17]. However, GPs are often resistant to follow guideline recommendations because they are voluminous texts difficult to read, and they don’t always understand the argumentation of experts underlying the recommendation. This is why we proposed a different approach: a visual interface comparing the different antibiotics rather than giving explicit recommendations. The visual interface we proposed could be integrated in electronic prescribing software and possibly connected to electronic health record (EHR) e.g. WebChart.

The results of the user study are rather promising. GPs seem convinced that the visualization of antibiotic disadvantages is interesting and useful for their practice, but fewer GPs found the proposed interface simple and easy to read. However, it has been shown that usability evaluations often give poor results on radically new interfaces, for which users are not accustomed to [18].

VII. CONCLUSION

In this paper, we presented weighted rainbow boxes. We showed that these techniques can translate visually the reasoning of a perceptron. We also showed that it can be applied in antibiotherapy, with interesting results. A perspective of this work consists in improving the weighted rainbow boxes technique for the visualization of more complex neural networks (e.g. involving several perceptron or hidden units).
### Affirmation Dataset

<table>
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<th>#</th>
<th>Affirmation</th>
<th>Dataset</th>
<th>5-drug</th>
<th>10-drug</th>
<th>5-drug</th>
<th>10-drug</th>
<th>5-drug</th>
<th>10-drug</th>
</tr>
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<tbody>
<tr>
<td>1</td>
<td>I find the interface easy</td>
<td>5-drug</td>
<td></td>
<td></td>
<td>6</td>
<td></td>
<td>3</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>10-drug</td>
<td></td>
<td></td>
<td>3</td>
<td></td>
<td>3</td>
<td></td>
</tr>
<tr>
<td>2</td>
<td>The disadvantages of each antibiotic are easy to read</td>
<td>5-drug</td>
<td></td>
<td></td>
<td>6</td>
<td></td>
<td>2</td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>10-drug</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>3</td>
<td>I find interesting to visualize the disadvantages of antibiotics</td>
<td>5-drug</td>
<td></td>
<td></td>
<td>6</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td></td>
<td>10-drug</td>
<td></td>
<td></td>
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<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>4</td>
<td>It is useful to visualize the disadvantages of antibiotics in clinical practice</td>
<td>5-drug</td>
<td></td>
<td></td>
<td>6</td>
<td></td>
<td></td>
<td></td>
</tr>
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<td></td>
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<td></td>
<td></td>
</tr>
<tr>
<td>5</td>
<td>I would like to have this system in clinical practice</td>
<td>5-drug</td>
<td></td>
<td></td>
<td>4</td>
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<td></td>
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Table I


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### REFERENCES


